



Hydrodynamics of Spinning Holographic Fluids

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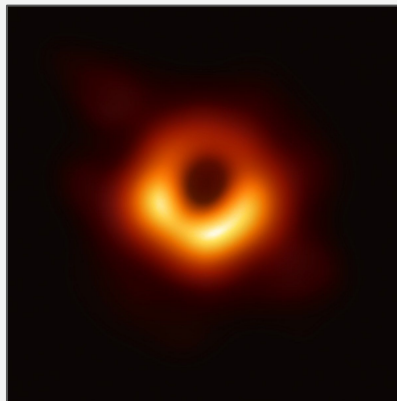
The University of Alabama
in collaboration with Matthias Kaminski

[\[arXiv: 2007.04345\]](https://arxiv.org/abs/2007.04345)

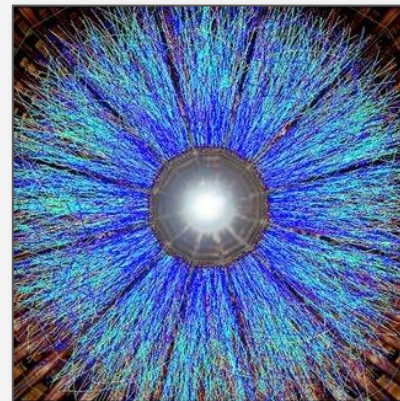
Outline

- Motivation
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- Setup (Background)
 - $a = b$
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- Setup (Fluctuations)
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 - Example Tensor QNMs
 - Scalar Sector
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Credit: Event Horizon Telescope Collaboration



Credit: Brookhaven National Laboratory

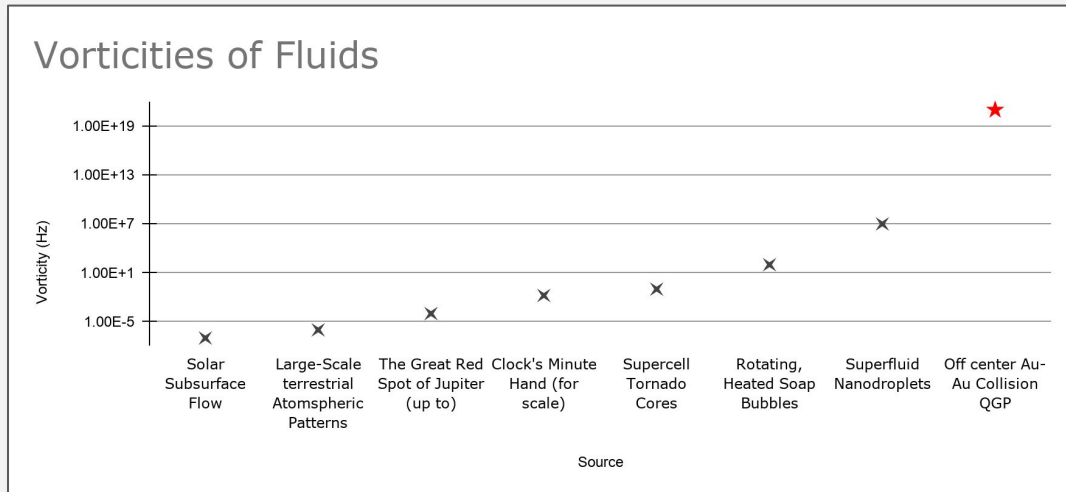


Motivation

Hyperon Polarization [\[2017 The STAR Collaboration\]](#)

Does a spinning 5D black hole correspond to a spinning strongly coupled fluid and what are its hydrodynamics?

Credit: Brookhaven National Labs



Setup (Background) (Rotating)

- [\[1998 Hawking et al\]](#) for 5D
- [\[2004 Pope et al\]](#) for $> 5D$
 - In D dimensions: up to $(D-1)/2$ independent rotation parameters
- For 5D 2 independent rotation parameters $\{a, b\}$
- We set $a = b$ for enhanced symmetry [\[2007 Soda et al\]](#) [\[2009 Murata\]](#)
- Linear superradiant instabilities when for $D = 5$ case [\[2009 Murata\]](#)
[\[2005 Carter et al\]](#) [\[2014 Cardoso et al\]](#) at large enough a to constrain values a will take.

Reference Slide (General 5D Myers Perry AdS)

$$\begin{aligned}
 ds^2 = & -\frac{\Delta}{\rho^2} \left(dt_H - \frac{a \sin^2 \theta_H}{\Xi_a} d\phi_H - \frac{b \cos^2 \theta_H}{\Xi_b} d\psi_H \right)^2 + \\
 & \frac{\Delta_{\theta_H} \sin^2 \theta_H}{\rho^2} \left(a dt_H - \frac{r_H^2 + a^2}{\Xi_a} d\phi_H \right)^2 + \frac{\Delta_{\theta_H} \cos^2 \theta_H}{\rho^2} \left(b dt_H - \frac{r_H^2 + b^2}{\Xi_b} d\psi_H \right)^2 + \\
 & \frac{\rho^2}{\Delta} dr_H^2 + \frac{\rho^2}{\Delta_{\theta_H}} d\theta_H^2 + \\
 & \frac{1 + r_H^2/L^2}{r_H^2 \rho^2} \left(ab dt_H - \frac{b(r^2 + a^2) \sin^2 \theta_H}{\Xi_a} d\phi_H - \frac{a(r^2 + b^2) \cos^2 \theta_H}{\Xi_b} d\psi_H \right)^2,
 \end{aligned}$$

[Metric Function Defs](#)

Reference Slide (Metric Functions Hawking)

$$\Delta = \frac{1}{r_H^2} (r_H^2 + a^2)(r_H^2 + b^2)(1 + r_H^2/L^2) - 2M,$$

$$\Delta_{\theta_H} = 1 - \frac{a^2}{L^2} \cos^2 \theta_H - \frac{b^2}{L^2} \sin^2 \theta_H,$$

$$\rho = r_H^2 + a^2 \cos^2 \theta_H + b^2 \sin^2 \theta_H,$$

$$\Xi_a = 1 - a^2/L^2,$$

$$\Xi_b = 1 - b^2/L^2$$

Setup (Background) (a = b 5D Myers Perry AdS) [Sigma Defs](#)

$$ds^2 = - \left(1 + \frac{r^2}{L^2}\right) dt^2 + \frac{dr^2}{G(r)} + \frac{r^2}{4} (4\sigma^+ \sigma^- + (\sigma^3)^2) + \frac{2\mu}{r^2} \left(dt + \frac{a}{2} \sigma^3\right)^2 \quad \text{[2009 Murata]}$$

$$G(r_+) = G(r_-) = 0$$

Round 3-Sphere ie "dΩ²"

Vanishes at $r = \infty$

$\mu \equiv$ Mass Parameter, $a \equiv$ Angular Momentum Parameter

$r_+ \equiv$ Outer Horizon Radius, $L \equiv$ AdS Radius

$$G(r) = 1 + \frac{r^2}{L^2} - \frac{2\mu(1-a^2/L^2)}{r^2} + \frac{2\mu a^2}{r^4} \quad \mu = \frac{r_+^4 (L^2 + r_+^2)}{2L^2 r_+^2 - 2a^2 (L^2 + r_+^2)}$$

$$L = 1$$

Reference Slide (Sigma Definitions)

$$\sigma^1 := -\sin \psi d\theta + \cos \psi \sin \theta d\phi ,$$

$$\sigma^2 := \cos \psi d\theta + \sin \psi \sin \theta d\phi ,$$

$$\sigma^3 := d\psi + \cos \theta d\phi ,$$

$$\sigma^\pm := \frac{1}{2} (\sigma^1 \mp i\sigma^2)$$

$$\sigma^t := dt$$

$$\sigma^r := dr$$

Setup (Linear Perturbations)

$$i\partial_t h_{ab} = \omega h_{ab} \quad -\partial_i \partial_i h_{ab} = \mathcal{J}(\mathcal{J} + 1)h_{ab}$$

$$i\partial_3 \sigma^r = 0 \quad i\partial_3 \sigma^t = 0$$

$$i\partial_3 \sigma^3 = 0 \quad i\partial_3 \sigma^\pm = \pm \sigma^\pm$$

$$i\partial_3 D_{\mathcal{K}}^{\mathcal{J}} = \mathcal{K} D_{\mathcal{K}}^{\mathcal{J}}$$

$$h_{ab} \propto \sigma^{(a} \sigma^{b)} e^{-\omega t} D_{\mathcal{K}-\sigma s' \text{ charge}}^{\mathcal{J}}$$

Find the equations of motion (EOM) at linear order.

Perform a large [temperature limit](#) on EOMs $r, J, K, r+ \rightarrow \infty$.

Keep the leading order terms wrt r .

Solve for ω , the Quasinormal Modes at given parameters.

Reference Slide (Large Temperature Limit)

$$\omega \rightarrow \alpha 2\nu r_+ / L$$

$$\mathcal{J} \rightarrow \alpha j r_+ / L$$

Rescale

$$r_+ \rightarrow \alpha r_+$$

$$r \rightarrow \alpha r$$

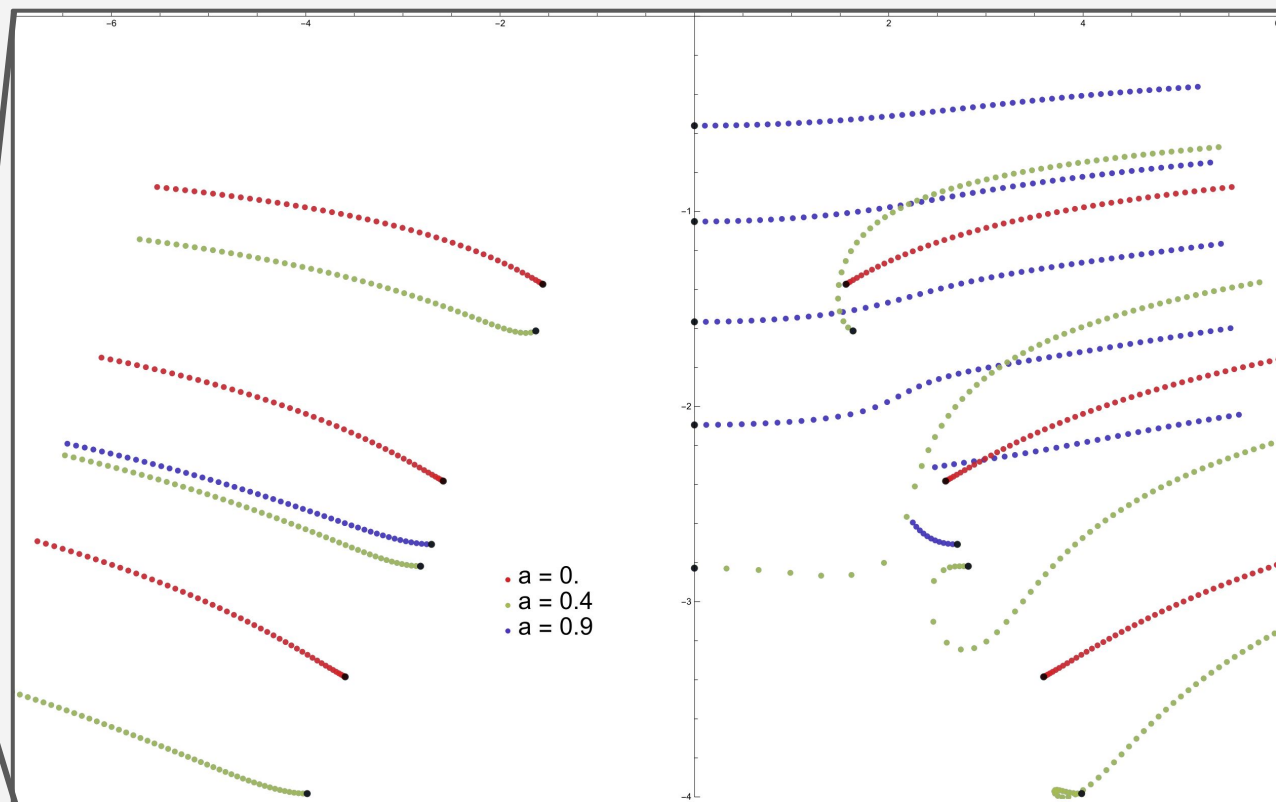
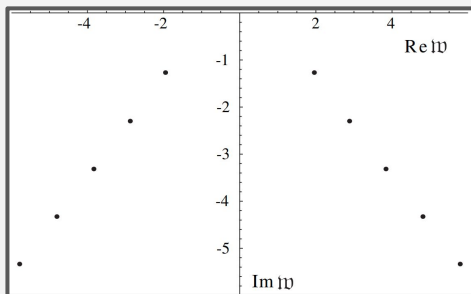
$$\alpha \rightarrow \infty$$

Then
perform
the α limit

QNMs Example (Tensor Sector/Scalar Channel)

$$\mathcal{K} = \mathcal{J} + 2$$

compare with the QNM
"Christmas Tree"
[\[2002 Starinets\]](#)



Results (Shear Channel/Vector Sector)

Defines Sector

$$\mathcal{K} = \mathcal{J} + 1$$

Dispersion Relations

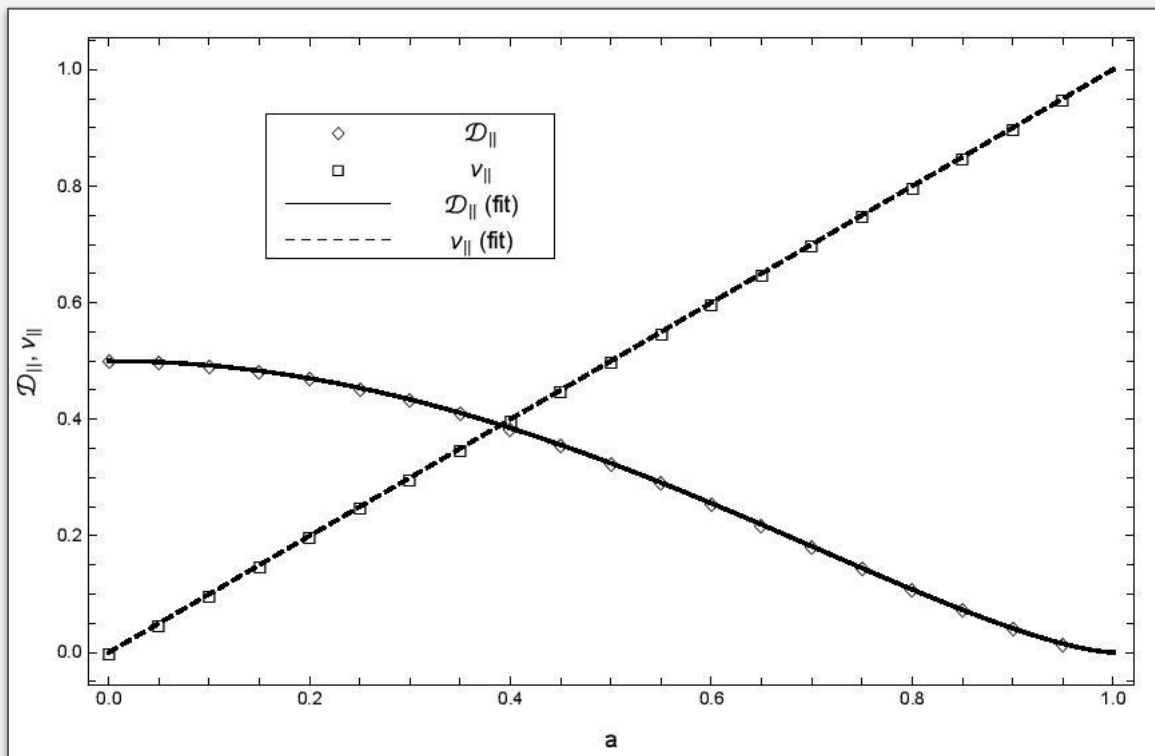
$$\nu = v_{\parallel} j - i \mathcal{D}_{\parallel} j^2$$

$$v_{\parallel} = a$$

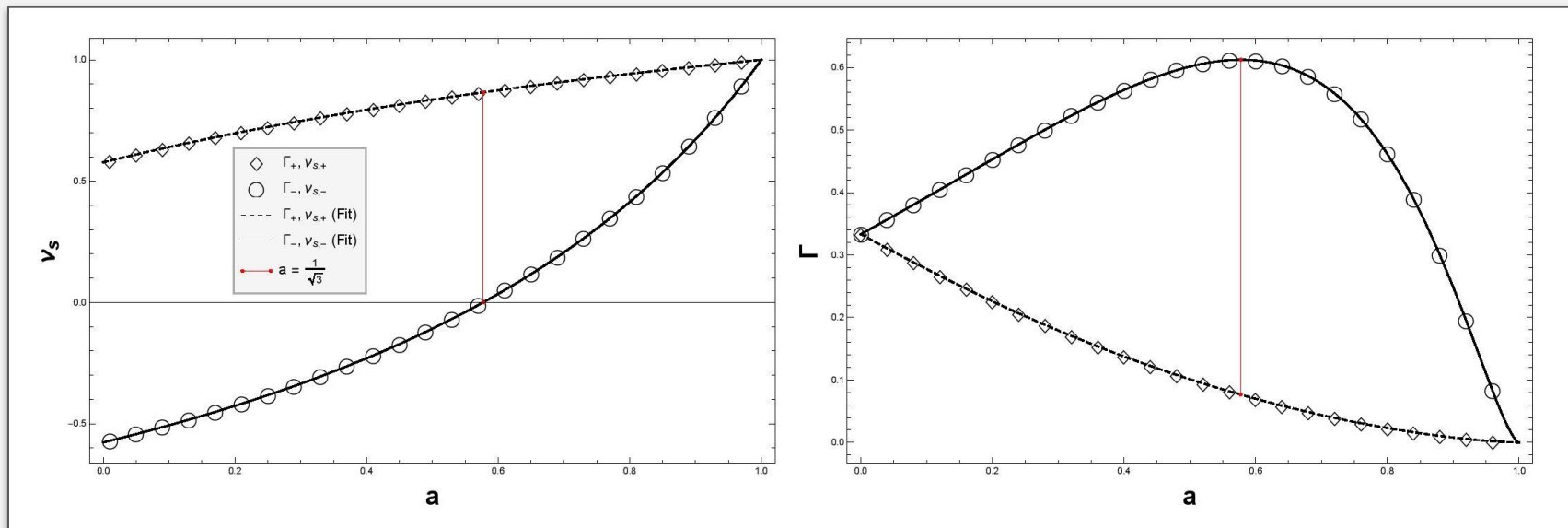
$$\mathcal{D}_{\parallel} = \frac{1}{2} (1 - a^2)^{3/2}$$

compare to [\[2019 Kovtun see eq \(4.4\)\]](#) [\[2020 Hout et al\]](#)

$$\frac{\eta_{\parallel}}{s} = \frac{1}{4\pi} (1 - a^2)$$



Results (Sound Channel/Scalar Sector)



Defines Sector $\mathcal{K} = \mathcal{J}$

compare to [\[2019 Kovtun see eq \(4.16\)\]](#)
[\[2020 Hout et al\]](#)

Dispersion Relations

$$\nu = v_{s,\pm} j - i \Gamma_{s,\pm} j^2,$$

$$v_{s,\pm} = \frac{a \pm \frac{1}{\sqrt{3}}}{1 \pm \frac{a}{\sqrt{3}}},$$

$$\Gamma_{s,\pm} = \frac{1}{3} \frac{(1 - a^2)^{3/2}}{\left(1 \pm \frac{a}{\sqrt{3}}\right)^3},$$

Conclusion

We find that a spinning large temperature black hole has hydrodynamic modes, depending on a .

Should be identified with modes of a relativistic spinning (strongly coupled) fluid.

There are two speeds of sound and two sound attenuation coefficients and two shears.

Transport coefficients are determined by their value at rest: $\eta_{||}(a) = \eta_0 \sqrt{1 - a^2}$.

Outlook: Non-hydrodynamic modes, hydrodynamic convergence radius [\[2019 Grozdanov et al JHEP\]](#) [\[2019 Grozdanov et al PRL\]](#), Complexity?! [\[2020 Balushi et al ArXiv\]](#)

Thank you for listening to my talk!

Credit David Madore

