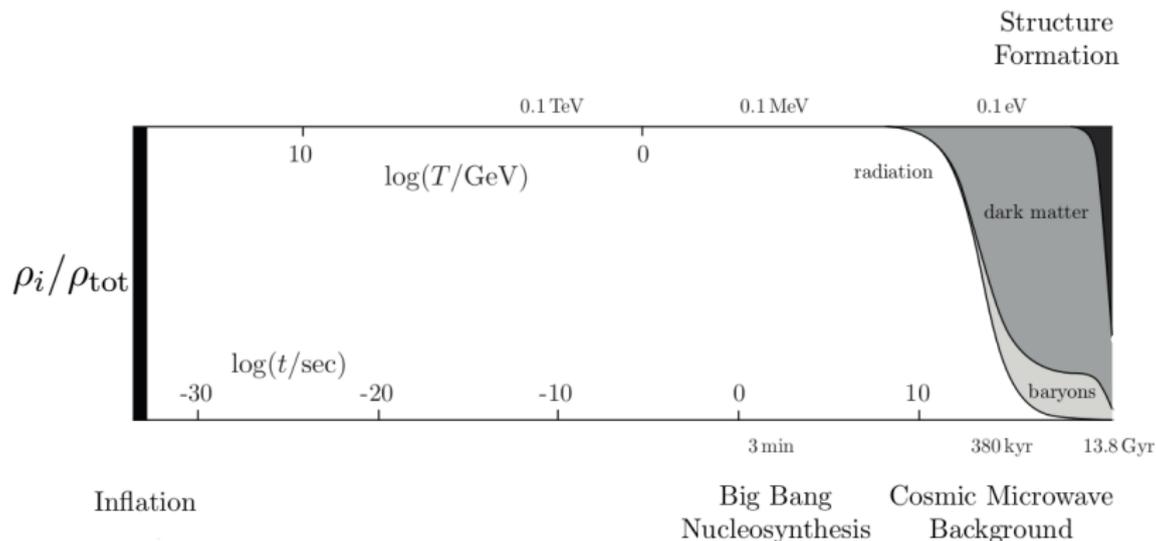


The Cosmic Axion Background

Jeff Dror

JD w/ Rodd & Murayama
2101.09287

...



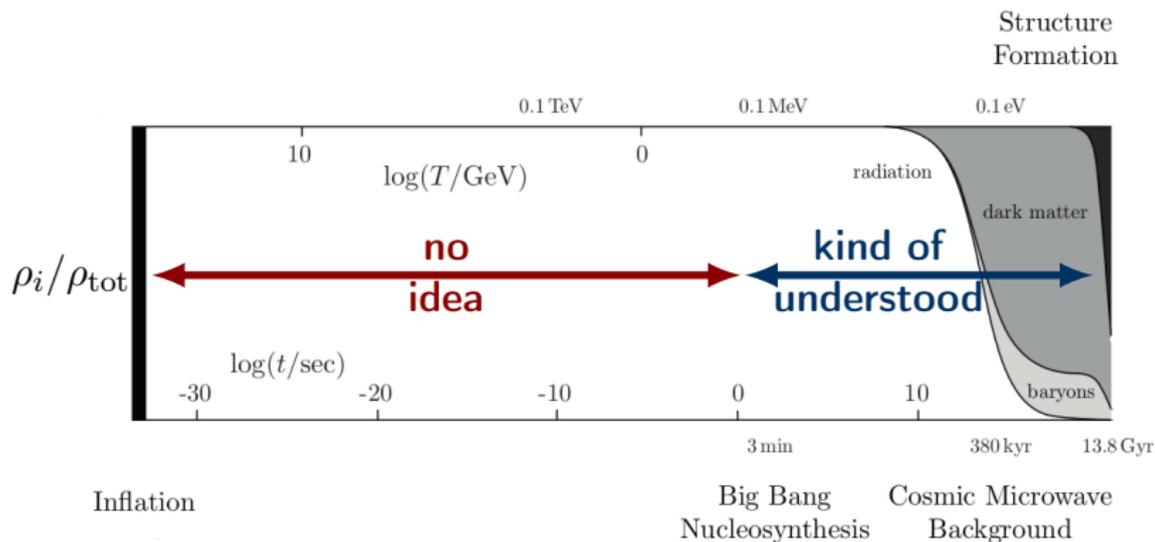
[Bkg photo: Baumann - 2013]

The Cosmic Axion Background

Jeff Dror

JD w/ Rodd & Murayama
2101.09287

...



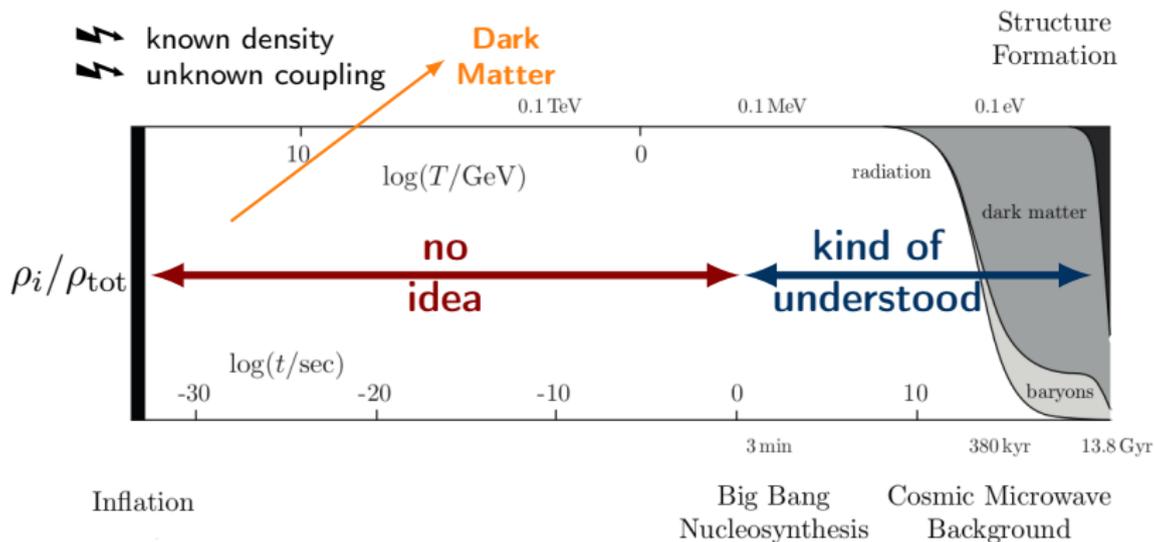
[Bkg photo: Baumann - 2013]

The Cosmic Axion Background

Jeff Dror

JD w/ Rodd & Murayama
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...



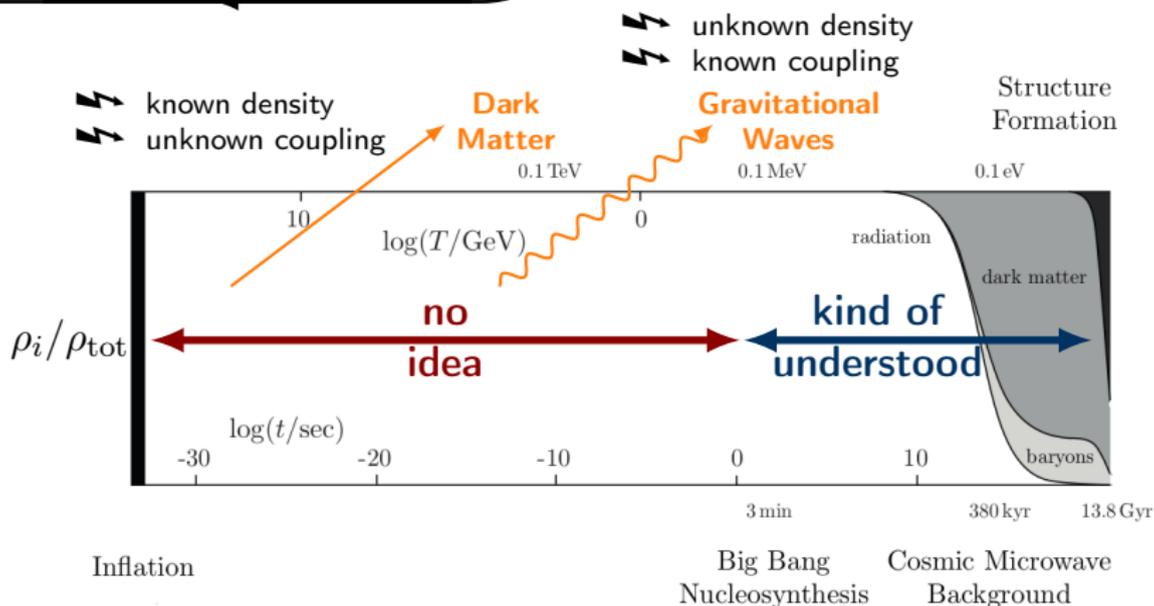
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The Cosmic Axion Background

Jeff Dror

JD w/ Rodd & Murayama
2101.09287

...



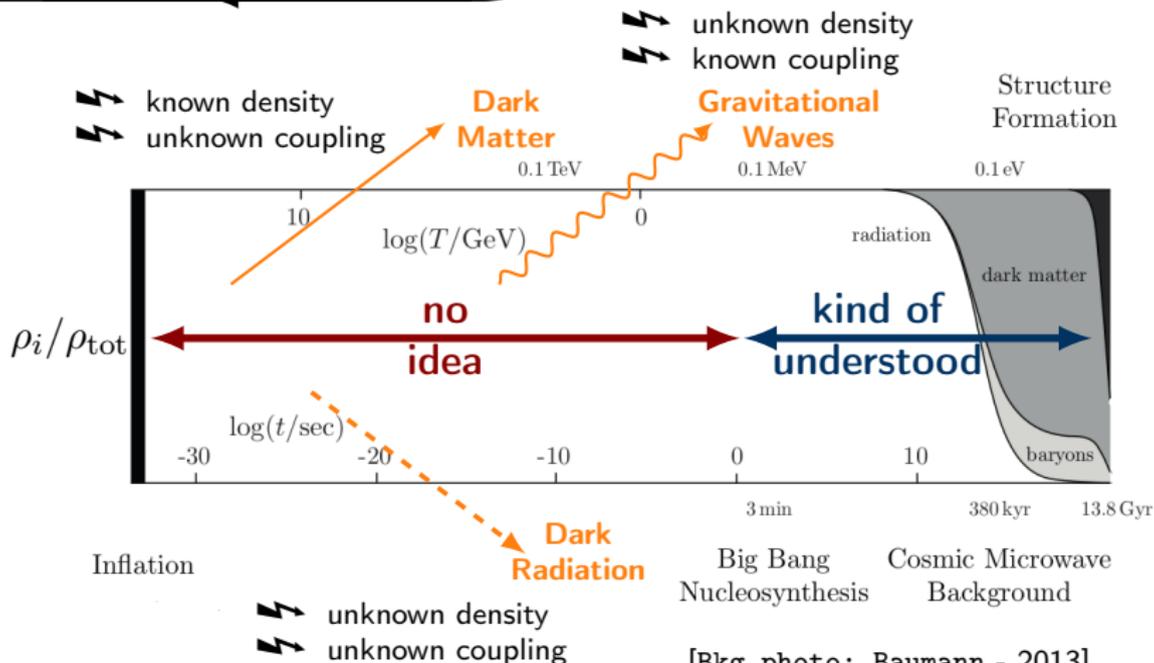
[Bkg photo: Baumann - 2013]

The Cosmic Axion Background

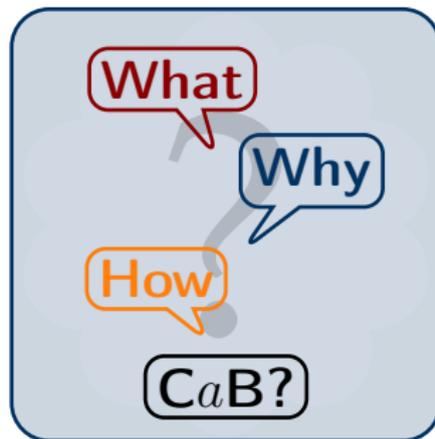
Jeff Dror

JD w/ Rodd & Murayama
2101.09287

...



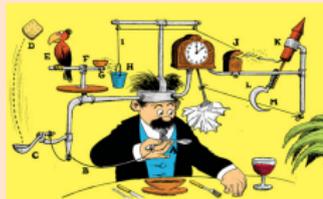
[Bkg photo: Baumann - 2013]



Detection



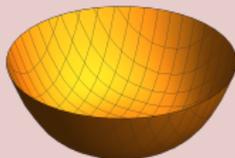
Production



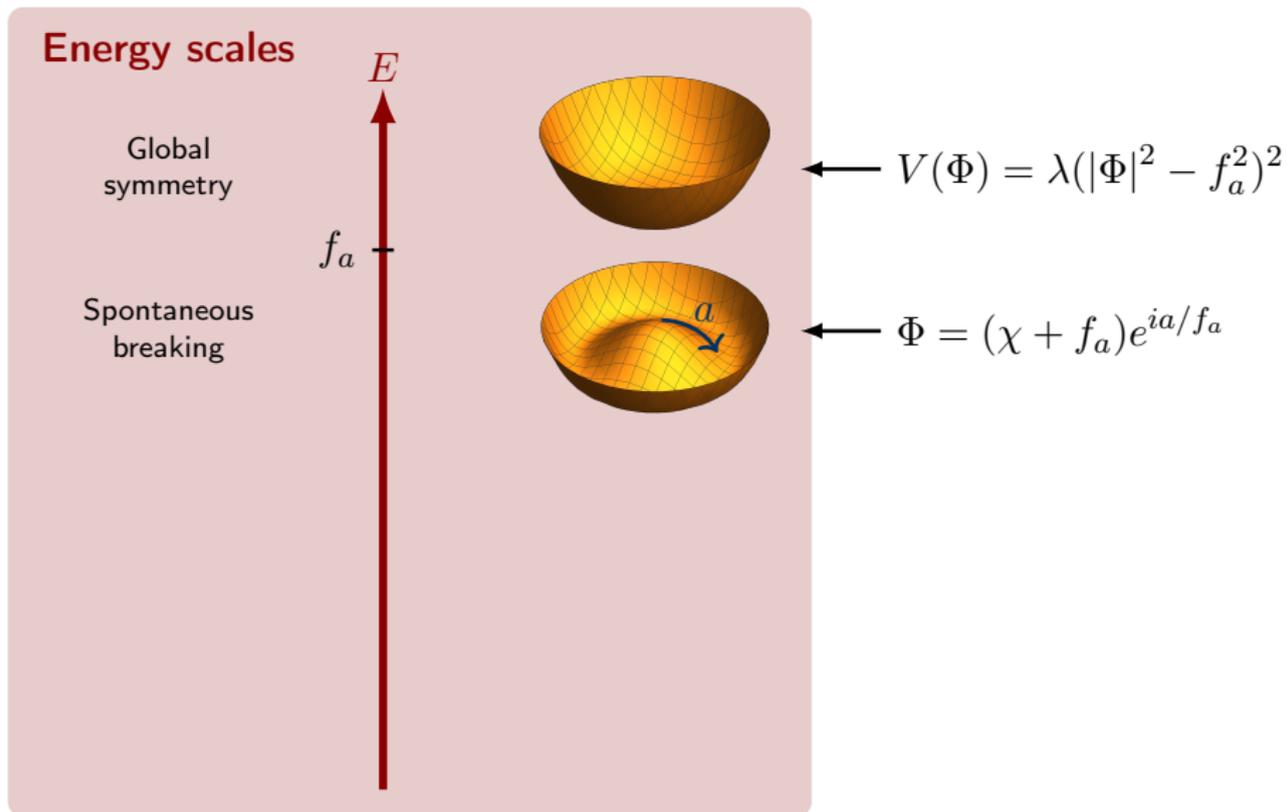
Axions and dark radiation

Energy scales

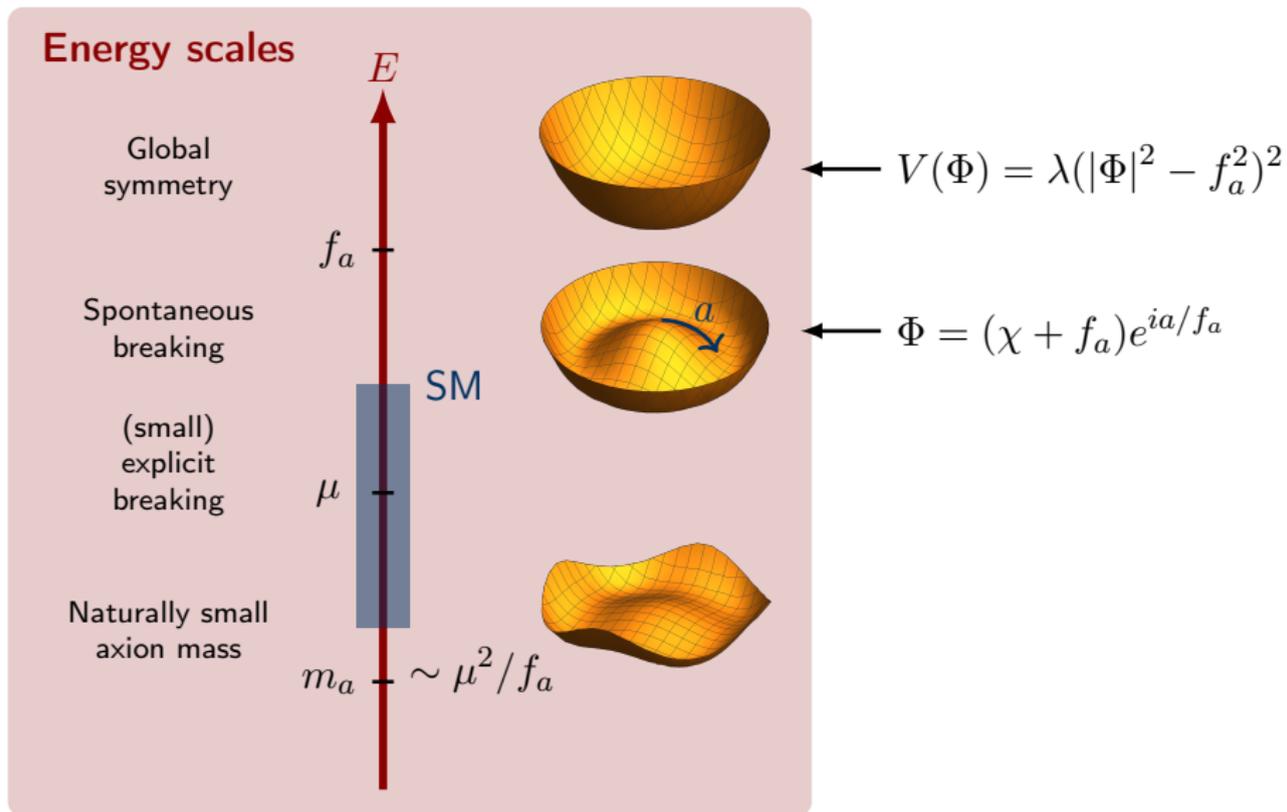
Global
symmetry

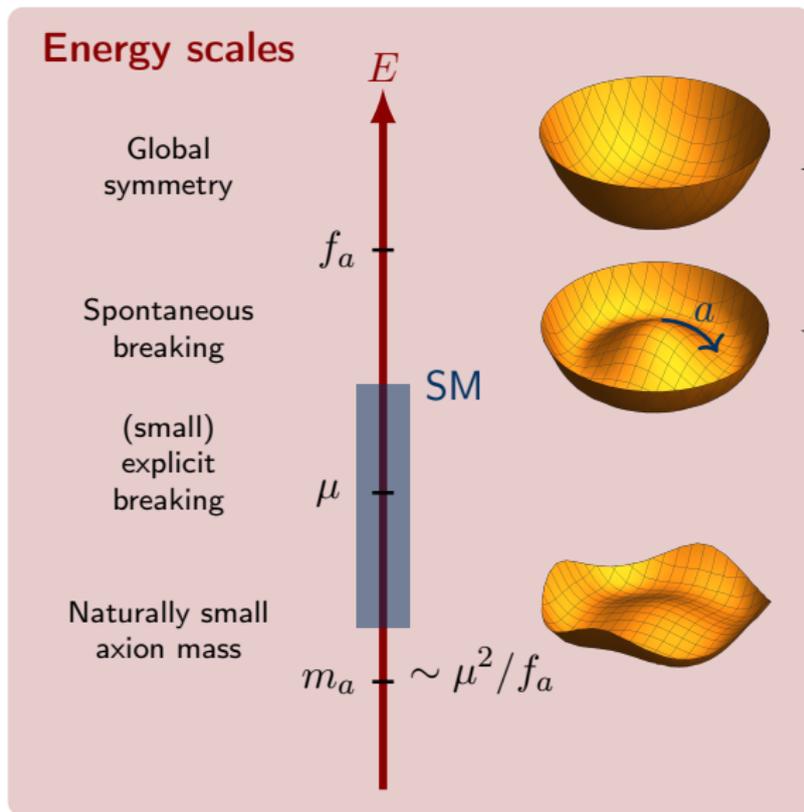


$$\leftarrow V(\Phi) = \lambda(|\Phi|^2 - f_a^2)^2$$



Why axions?





$$\leftarrow V(\Phi) = \lambda(|\Phi|^2 - f_a^2)^2$$

$$\leftarrow \Phi = (\chi + f_a)e^{ia/f_a}$$

**One axion or
an entire
axi-verse?**

[Svrček, Witten - hep-th/0605206]

[Arvanitaki et al - 0905.4720]

[Halverson et al - 1903.04495]

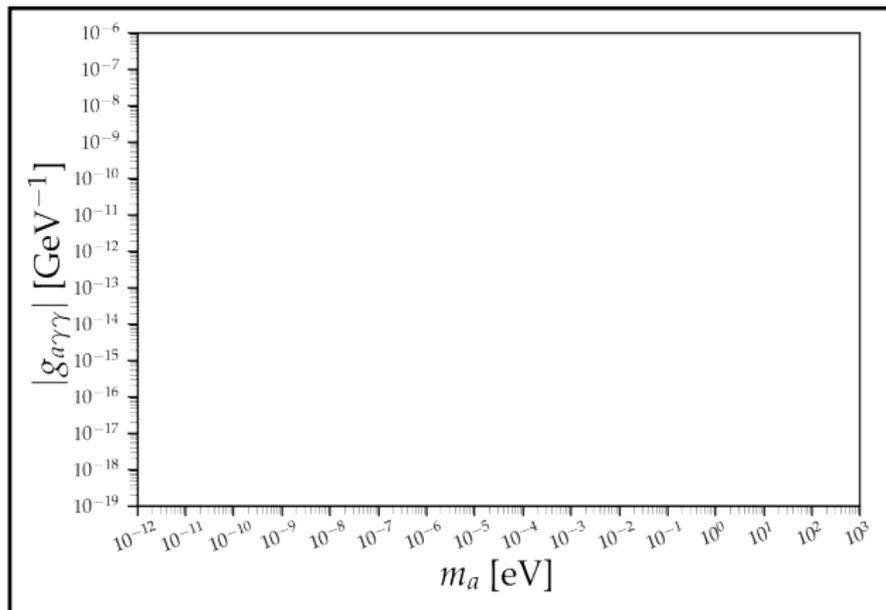
[Halverson et al - 1909.05257]

...



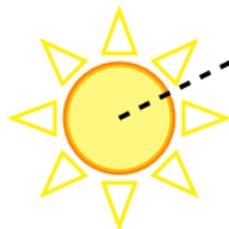
$$\mathcal{L} \supset -\frac{1}{4}g_{\alpha\gamma\gamma}aF_{\mu\nu}\tilde{F}^{\mu\nu} \supset g_{\alpha\gamma\gamma}a\mathbf{E} \cdot \mathbf{B}$$

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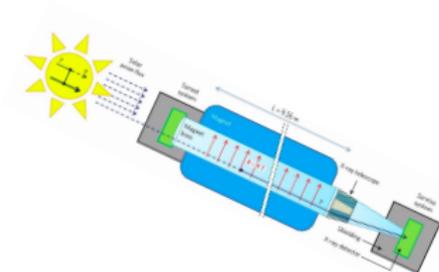


$$\mathcal{L} \supset -\frac{1}{4}g_{a\gamma\gamma}aF_{\mu\nu}\tilde{F}^{\mu\nu} \supset g_{a\gamma\gamma}a\mathbf{E} \cdot \mathbf{B}$$

direct
production



a



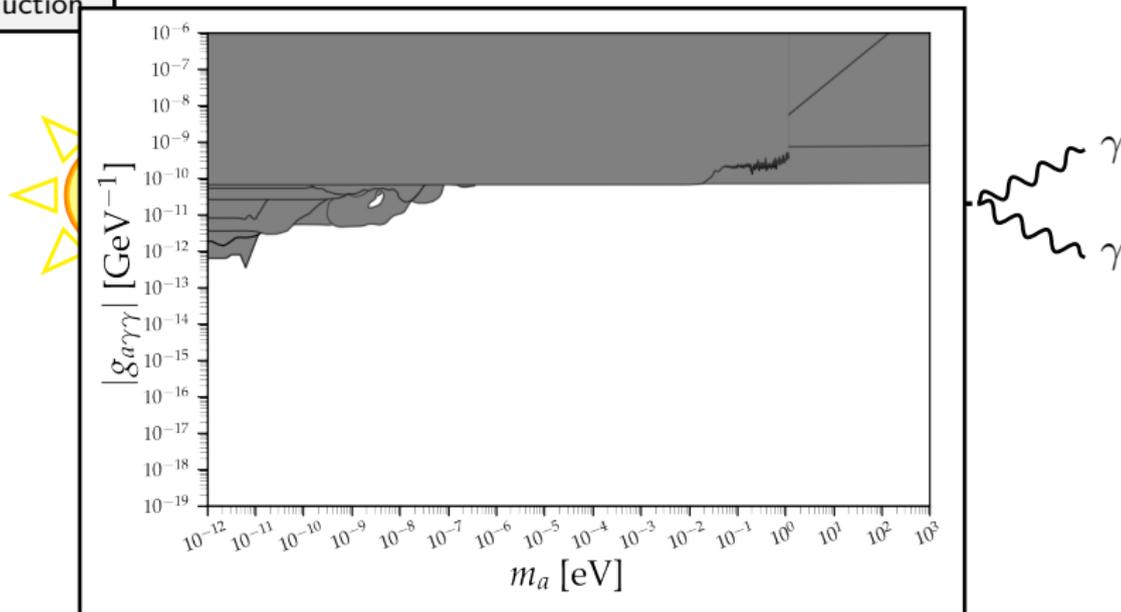
a



[- CAST, 2017]

$$\mathcal{L} \supset -\frac{1}{4}g_{a\gamma\gamma}aF_{\mu\nu}\tilde{F}^{\mu\nu} \supset g_{a\gamma\gamma}a\mathbf{E}\cdot\mathbf{B}$$

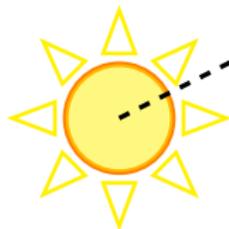
direct
production



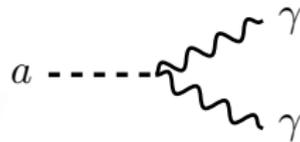
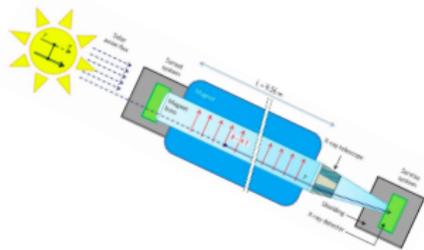
[compiled at - <https://github.com/cajohare/AxionLimits>]

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direct
production



a



[- CAST, 2017]

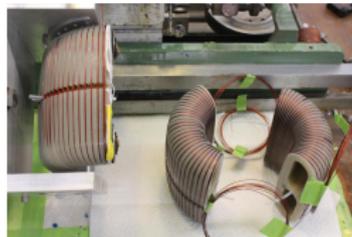
axion
dark
matter

e.g., ADMX



[- Scientific American]

e.g., ABRACADBRA



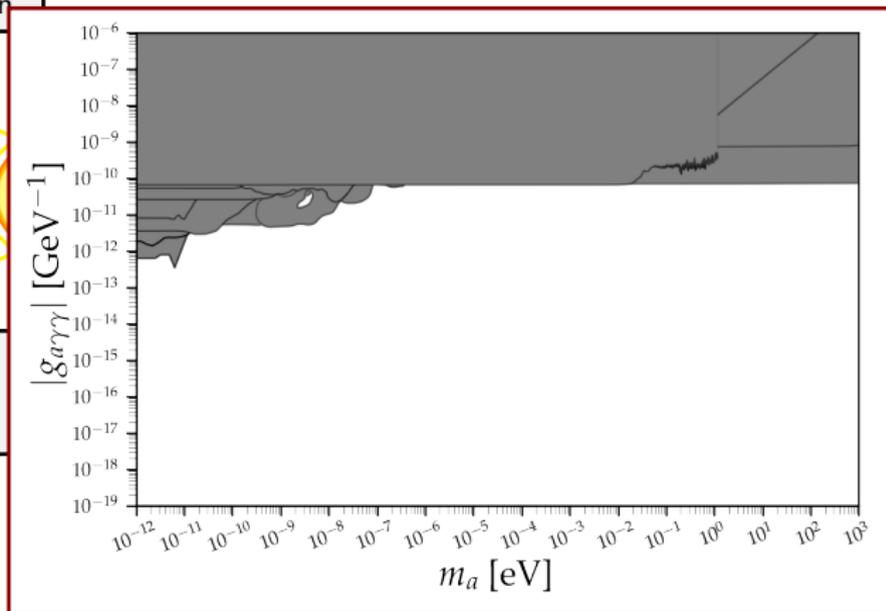
[- abracadbra.mit.edu/]

$$\mathcal{L} \supset -\frac{1}{4}g_{a\gamma\gamma}aF_{\mu\nu}\tilde{F}^{\mu\nu} \supset g_{a\gamma\gamma}a\mathbf{E} \cdot \mathbf{B}$$

direct
production



axion
dark
matter



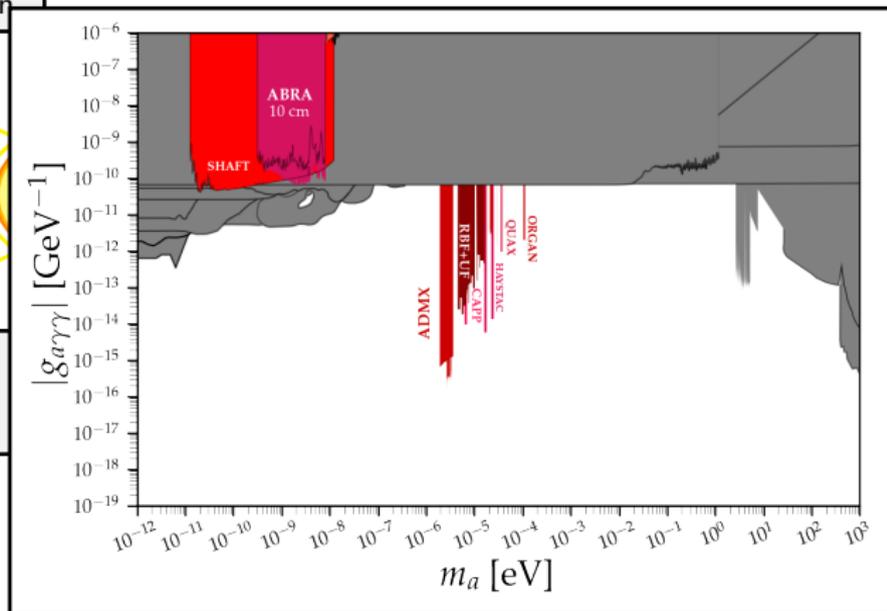
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direct
production



axion
dark
matter



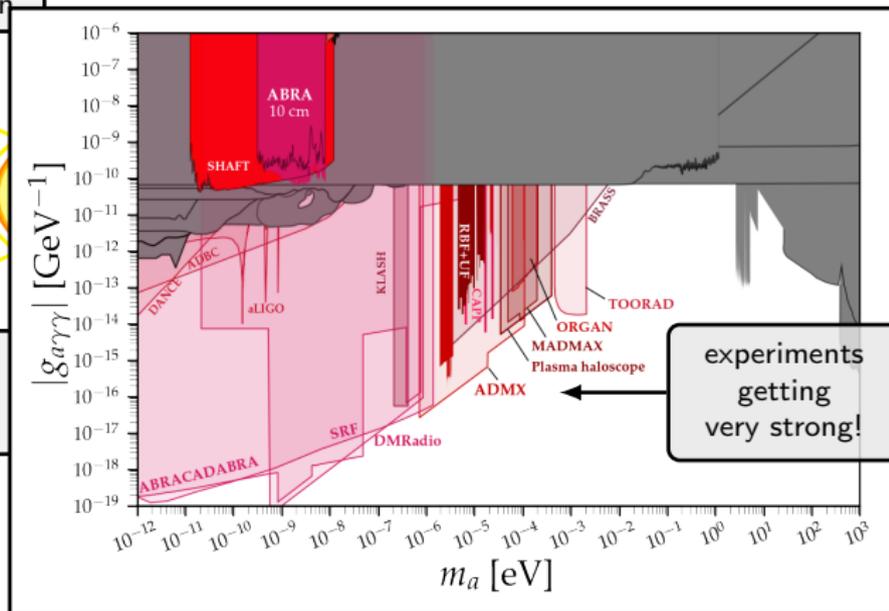
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direct
production



axion
dark
matter



experiments
getting
very strong!

[compiled at - <https://github.com/cajohare/AxionLimits>]



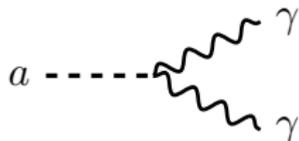
Population of
relativistic
axions?

Copiously produced in
early universe

Population of
relativistic
axions?

Copiously produced in
early universe

Light axions are stable

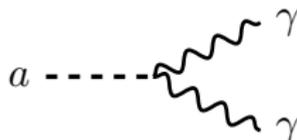


$$\frac{\Gamma}{H_0} \sim \left(\frac{m_a}{100 \text{ eV}} \right)^3 \left(\frac{g_{a\gamma\gamma}}{10^{-10} \text{ GeV}^{-1}} \right)^2$$

Population of
relativistic
axions?

Copiously produced in
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Light axions are stable


$$\frac{\Gamma}{H_0} \sim \left(\frac{m_a}{100 \text{ eV}} \right)^3 \left(\frac{g_{a\gamma\gamma}}{10^{-10} \text{ GeV}^{-1}} \right)^2$$

Could be responsible for
 H_0 -tension (“universe-age” mystery)

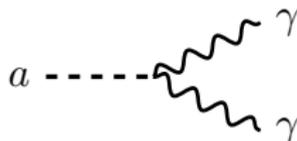
$$\tau_{\text{universe}} = \begin{cases} 12.7 \pm 0.1 \text{ byr} & (\text{late}) \\ 13.7 \pm 0.1 \text{ byr} & (\text{early}) \end{cases}$$

[Verde, Treu, Riess - 1907.10625]
[Planck - 1807.06209]

Population of relativistic axions?

Copiously produced in early universe

Light axions are stable


$$\frac{\Gamma}{H_0} \sim \left(\frac{m_a}{100 \text{ eV}} \right)^3 \left(\frac{g_{a\gamma\gamma}}{10^{-10} \text{ GeV}^{-1}} \right)^2$$

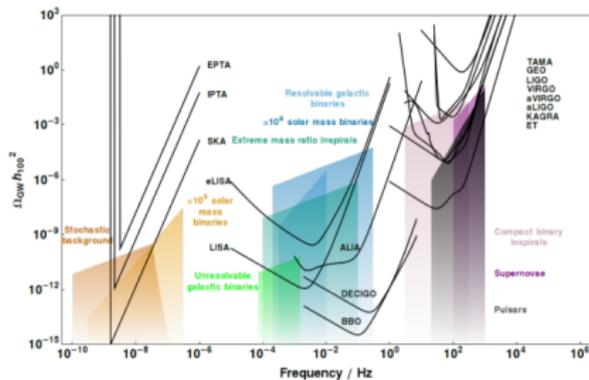
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$$\tau_{\text{universe}} = \begin{cases} 12.7 \pm 0.1 \text{ byr} & (\text{late}) \\ 13.7 \pm 0.1 \text{ byr} & (\text{early}) \\ 14.0 \pm 0.3 \text{ byr} & (\text{early}, \Delta N_{\text{eff}} \neq 0) \end{cases}$$

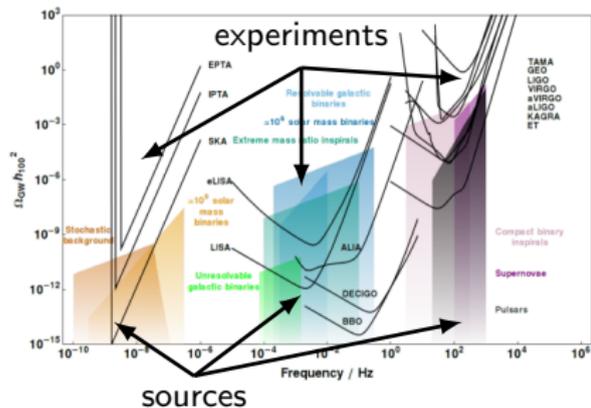
[Verde, Treu, Riess - 1907.10625]
[Planck - 1807.06209]

$$\rightarrow \rho_a \sim \rho_\gamma$$

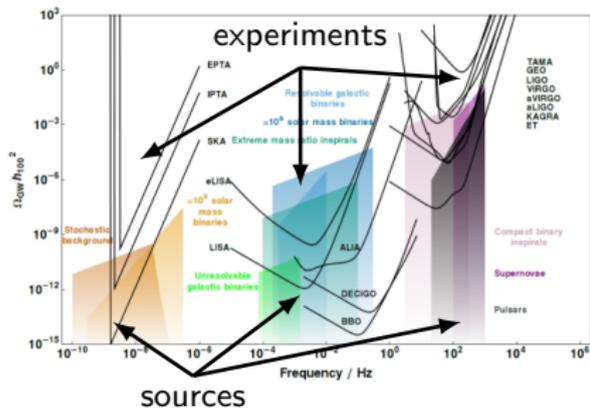
[Moore, Cole, Berry - 1408.0740]



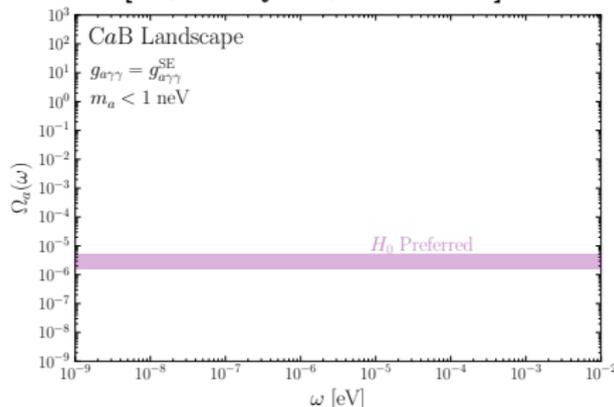
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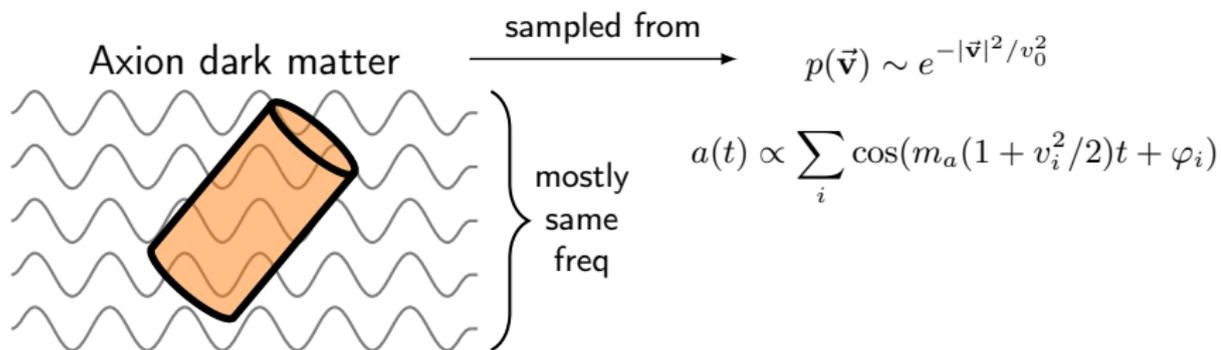


[JD, Murayama, Rodd - '21]

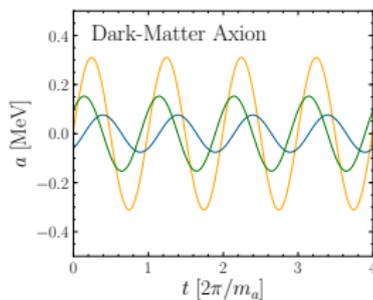


dark radiation analog

Calculating experimental sensitivities



Axion dark matter

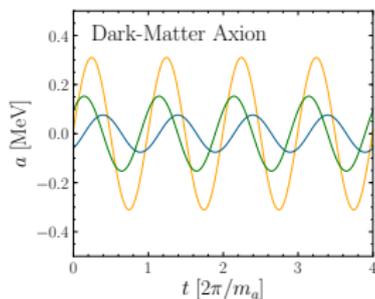


sampled from

$$p(\vec{v}) \sim e^{-|\vec{v}|^2/v_0^2}$$

$$a(t) \propto \sum_i \cos(m_a(1 + v_i^2/2)t + \varphi_i)$$

Axion dark matter



sampled from

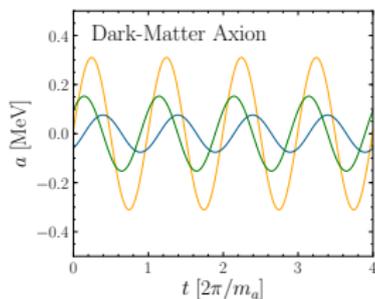
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$$\rho_a(m_a) = Q_a m_a n_a$$

$$\frac{d\rho_a}{d \log \omega} \quad \uparrow \quad \uparrow \quad \mathcal{O}(10^6)$$

Axion dark matter



sampled from

$$p(\vec{v}) \sim e^{-|\vec{v}|^2/v_0^2}$$

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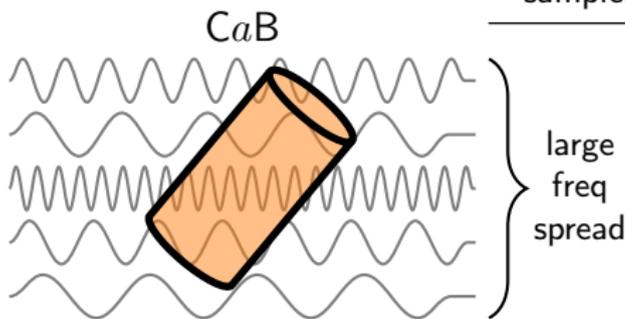
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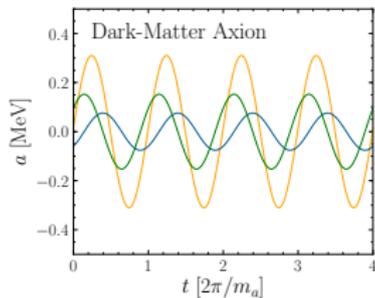
$$p(\omega) = ?$$

$$a(t) \propto \sum_i \cos(\omega_i t + \mathbf{k}_i \cdot \mathbf{x} + \varphi_i)$$

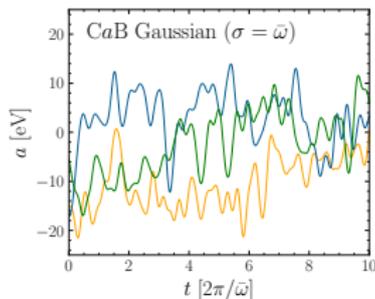


large
freq
spread

Axion dark matter



CaB



sampled from

$$p(\vec{v}) \sim e^{-|\vec{v}|^2/v_0^2}$$

$$a(t) \propto \sum_i \cos(m_a(1 + v_i^2/2)t + \varphi_i)$$

$$\rho_a(m_a) = Q_a m_a n_a$$

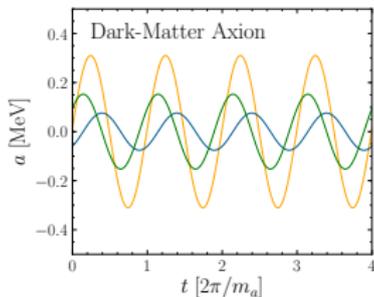
$$\frac{d\rho_a}{d \log \omega} \quad \uparrow \quad \uparrow \quad \mathcal{O}(10^6)$$

sampled from

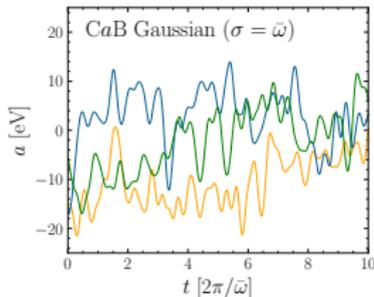
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Axion dark matter



CaB



sampled from

$$p(\vec{v}) \sim e^{-|\vec{v}|^2/v_0^2}$$

$$a(t) \propto \sum_i \cos(m_a(1 + v_i^2/2)t + \varphi_i)$$

$$\rho_a(m_a) = Q_a m_a n_a$$

$$\frac{d\rho_a}{d \log \omega} \quad \uparrow \quad \uparrow \quad \mathcal{O}(10^6)$$

sampled from

$$p(\omega) = ?$$

$$a(t) \propto \sum_i \cos(\omega_i t + \mathbf{k}_i \cdot \mathbf{x} + \varphi_i)$$

$$\rho_a(\bar{\omega}) = Q_a \bar{\omega} n_a$$

$$\uparrow \quad \text{often } \mathcal{O}(1)$$



$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - J_{\mu}A^{\mu} + g_{a\gamma\gamma}a\mathbf{E} \cdot \mathbf{B}$$

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - J_{\mu}A^{\mu} + g_{a\gamma\gamma}a\mathbf{E} \cdot \mathbf{B}$$

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma}(\nabla a) \cdot \mathbf{B}$$

$$\nabla \times \mathbf{E} = -\dot{\mathbf{B}}$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{B} = \dot{\mathbf{E}} + \mathbf{J} + g_{a\gamma\gamma}(\dot{a}\mathbf{B} + \nabla a \times \mathbf{E})$$

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - J_{\mu}A^{\mu} + g_{a\gamma\gamma}a\mathbf{E} \cdot \mathbf{B}$$

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← effective charge

$$\nabla \times \mathbf{E} = -\dot{\mathbf{B}}$$

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← effective current

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$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma}(\nabla a) \cdot \mathbf{B}$$

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$$\nabla \times \mathbf{E} = -\dot{\mathbf{B}}$$

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$$\nabla \times \mathbf{B} = \dot{\mathbf{E}} + \mathbf{J} + g_{a\gamma\gamma}(\dot{a}\mathbf{B} + \nabla a \times \mathbf{E})$$

← effective current

Dark Matter

$$\text{⚡ } \nabla a \propto |\vec{\mathbf{v}}_a| \sim 10^{-3}$$

⚡ only effective current

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - J_{\mu}A^{\mu} + g_{a\gamma\gamma}a\mathbf{E} \cdot \mathbf{B}$$

$$\nabla \cdot \mathbf{E} = \rho - g_{a\gamma\gamma}(\nabla a) \cdot \mathbf{B}$$

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$$\nabla \times \mathbf{E} = -\dot{\mathbf{B}}$$

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← effective current

Dark Matter

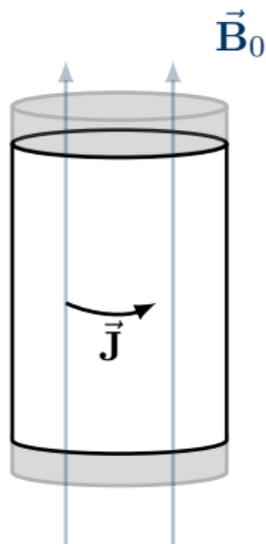
⚡ $\nabla a \propto |\vec{\mathbf{v}}_a| \sim 10^{-3}$

⚡ only effective current

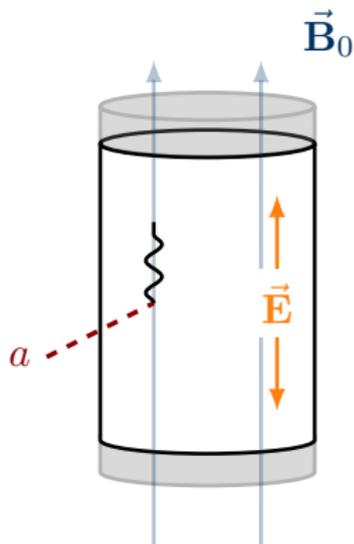
CaB

⚡ current + charge

⚡ dependence on direction

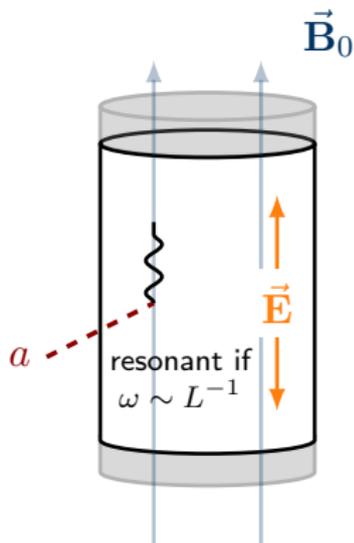


e.g., ADMX,
HAYSTAC



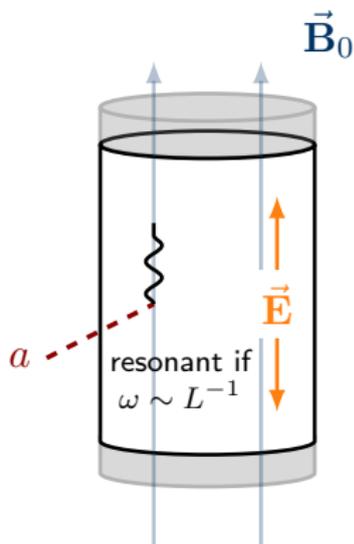
e.g., ADMX,
HAYSTAC

$$(\nabla^2 - \partial_t^2)\vec{\mathbf{E}} = g_{a\gamma\gamma}(\vec{\mathbf{B}}_0\partial_t^2 a - (\vec{\mathbf{B}}_0 \cdot \vec{\nabla})\vec{\nabla}a)$$



e.g., ADMX,
HAYSTAC

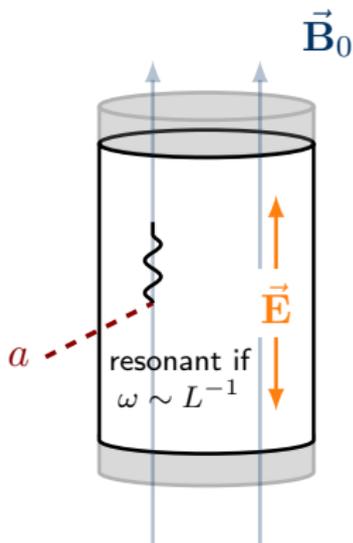
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e.g., ADMX,
HAYSTAC

$$(\nabla^2 - \partial_t^2)\vec{\mathbf{E}} = g_{a\gamma\gamma}(\vec{\mathbf{B}}_0\partial_t^2 a - (\vec{\mathbf{B}}_0 \cdot \vec{\nabla})\vec{\nabla}a)$$

- 1) Solve $\vec{\mathbf{B}}_0 = 0$ modes, $\vec{\mathbf{e}}_n$
- 2) Expand $\vec{\mathbf{E}} = \sum_n A_n \vec{\mathbf{e}}_n$
- 3) Insert and solve for A_n



e.g., ADMX,
HAYSTAC

$$(\nabla^2 - \partial_t^2)\vec{\mathbf{E}} = g_{a\gamma\gamma}(\vec{\mathbf{B}}_0\partial_t^2 a - (\vec{\mathbf{B}}_0 \cdot \vec{\nabla})\vec{\nabla} a)$$

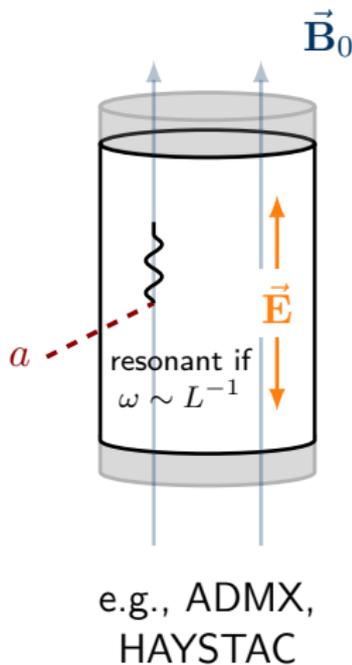
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2) Expand $\vec{\mathbf{E}} = \sum_n A_n \vec{\mathbf{e}}_n$

3) Insert and solve for A_n

$$A_n \propto \int_{\mathbf{x}} \cos(\vec{\mathbf{k}} \cdot \vec{\mathbf{x}}) [(\hat{\mathbf{k}} \cdot \hat{\mathbf{B}}_0)\hat{\mathbf{k}} - \hat{\mathbf{B}}_0] \cdot \vec{\mathbf{e}}_n^*$$

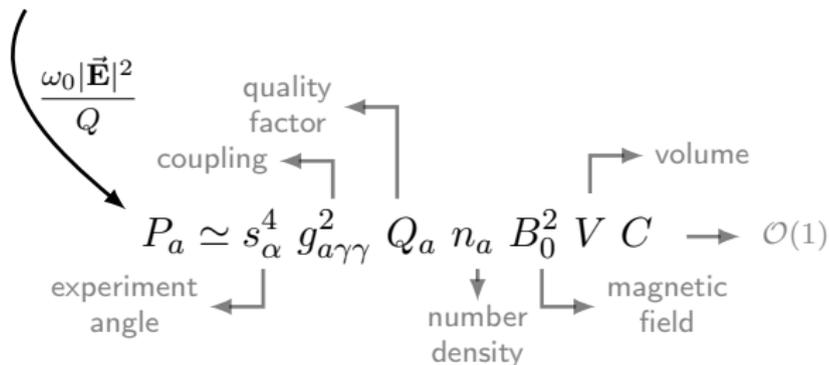
new
term
 $\hat{\mathbf{k}}$ -axion
direction

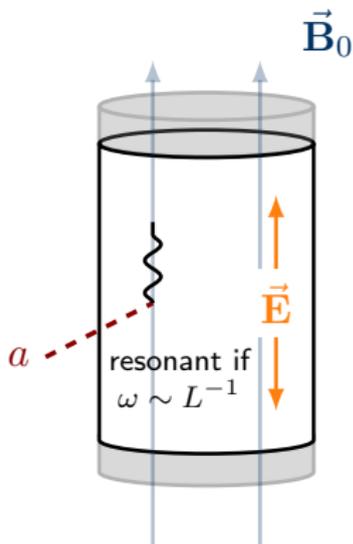


$$(\nabla^2 - \partial_t^2)\vec{\mathbf{E}} = g_{a\gamma\gamma}(\vec{\mathbf{B}}_0\partial_t^2 a - (\vec{\mathbf{B}}_0 \cdot \vec{\nabla})\vec{\nabla}a)$$

- 1) Solve $\vec{\mathbf{B}}_0 = 0$ modes, $\vec{\mathbf{e}}_n$
- 2) Expand $\vec{\mathbf{E}} = \sum_n A_n \vec{\mathbf{e}}_n$
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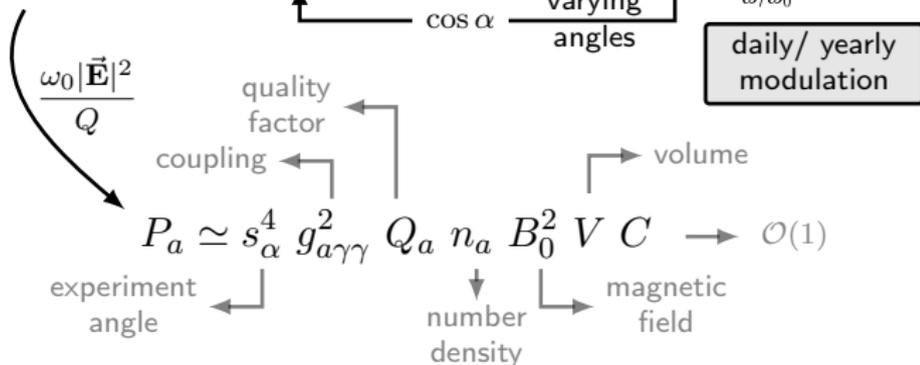
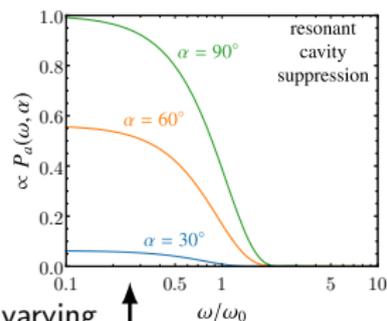


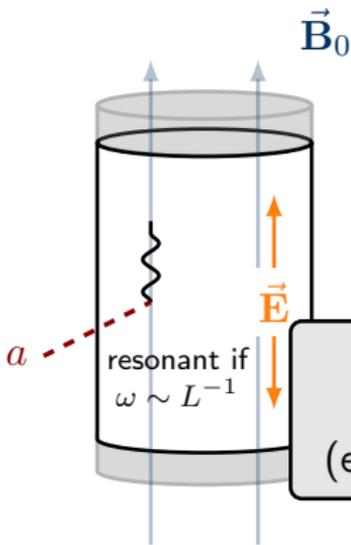
e.g., ADMX,
HAYSTAC

$$(\nabla^2 - \partial_t^2)\vec{\mathbf{E}} = g_{a\gamma\gamma}(\vec{\mathbf{B}}_0\partial_t^2 a - (\vec{\mathbf{B}}_0 \cdot \vec{\nabla})\vec{\nabla} a)$$

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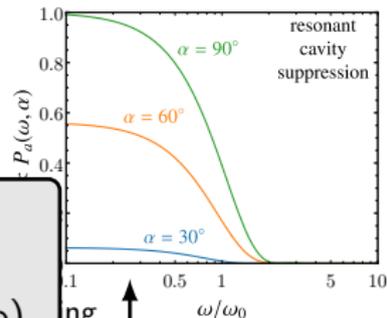


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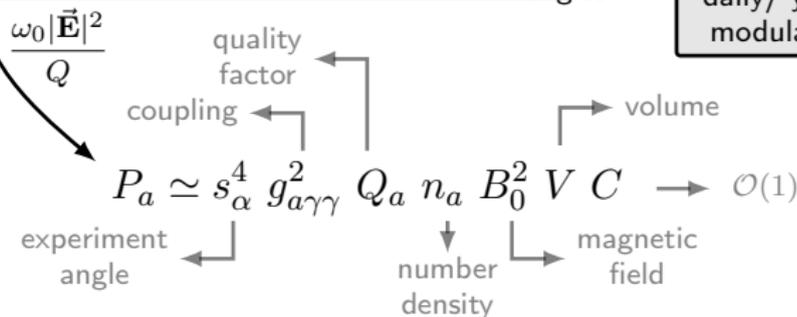
2) Expand $\vec{\mathbf{E}} = \sum_n A_n \vec{\mathbf{e}}_n$

LC circuit readout
allows low frequency detection
(e.g., ABRACADBARA, DM-Radio)



daily/ yearly modulation

e.g., ADMX,
HAYSTAC



simplified
limits

$$P_a^{\text{DM}}(\omega) = P_a^{\text{CaB}}(\omega)$$

caution: DM may
be easier to see

simplified
limits

$$P_a^{\text{DM}}(\omega) = P_a^{\text{CaB}}(\omega)$$

caution: DM may
be easier to see

$$g_{a\gamma\gamma}^2(\omega) \Omega_{\text{DM}} Q_{\text{DM}} = \Omega_a(\omega) (g_{a\gamma\gamma}^{\text{SE}})^2 Q_a$$

simplified
limits

$$P_a^{\text{DM}}(\omega) = P_a^{\text{CaB}}(\omega)$$

caution: DM may
be easier to see

$$g_{a\gamma\gamma}^2(\omega) \Omega_{\text{DM}} Q_{\text{DM}} = \Omega_a(\omega) (g_{a\gamma\gamma}^{\text{SE}})^2 Q_a$$

\downarrow \downarrow \downarrow
 $\sim 10^6$ $\sim 10^{-10} \text{ GeV}^{-1}$ ~ 1

1 bin

$$\Omega_a \simeq \Omega_{\text{DM}} \left(\frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{SE}}} \right)^2 \sqrt{\frac{Q_{\text{DM}}}{Q_a}}$$

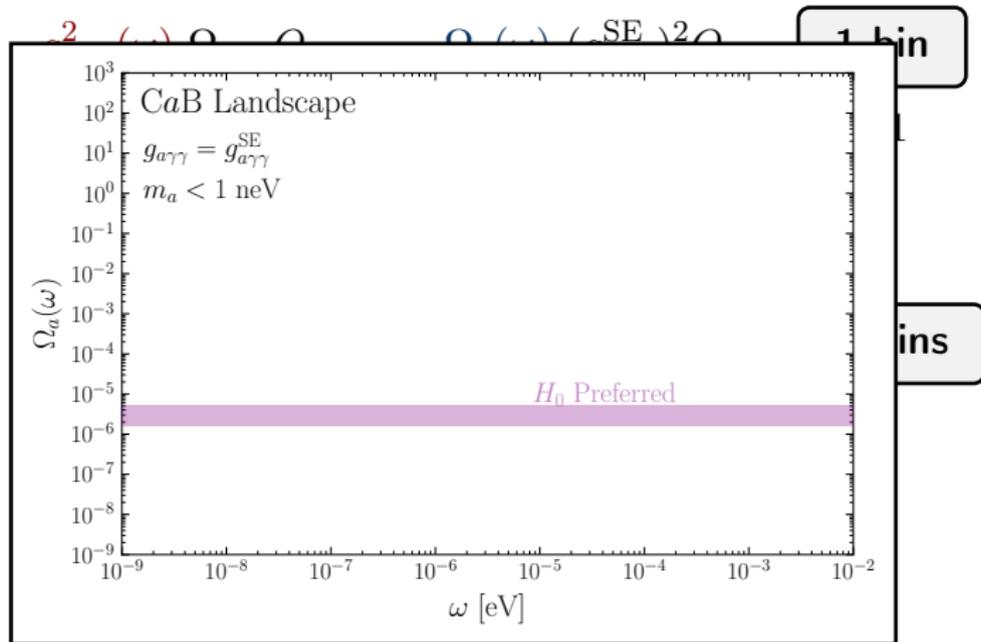
\swarrow lose \searrow win

all bins

simplified
limits

$$P_a^{\text{DM}}(\omega) = P_a^{\text{CaB}}(\omega)$$

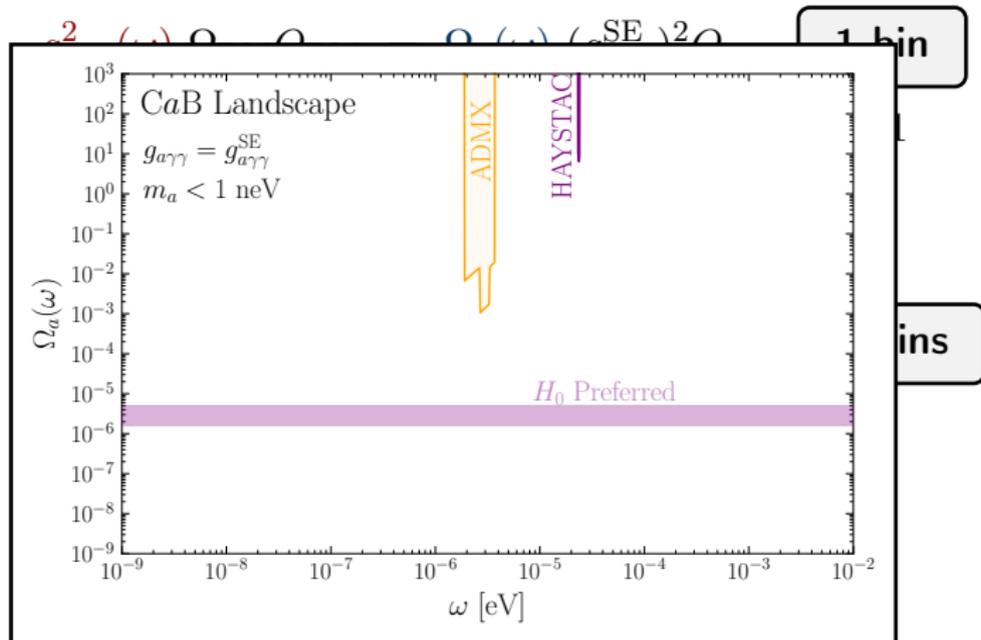
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simplified
limits

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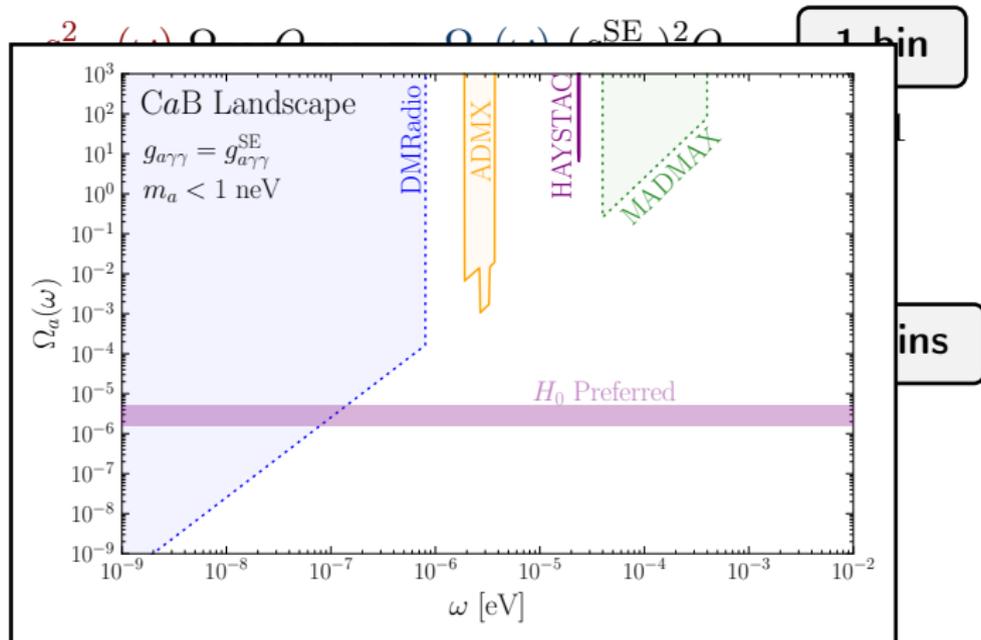
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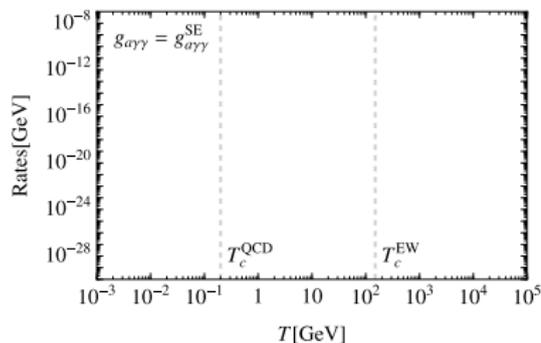
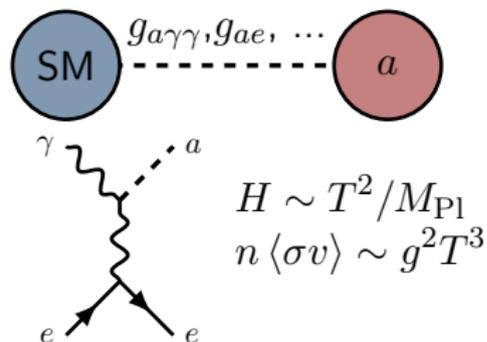


Producing a cosmic axion background

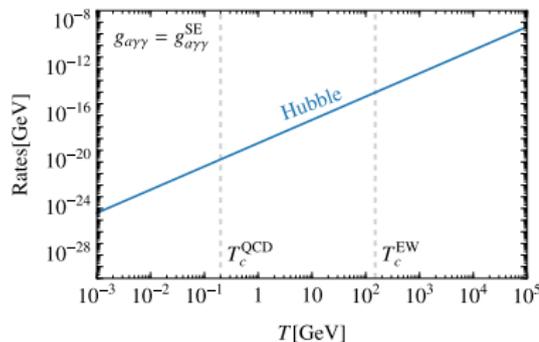
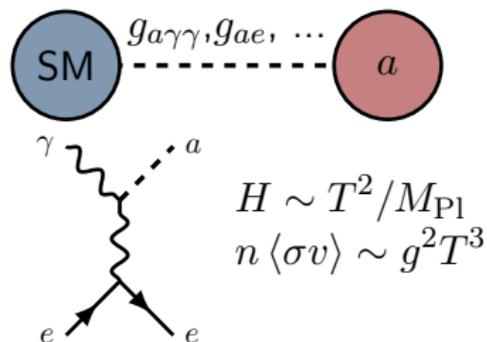


Thermalization with Standard Model

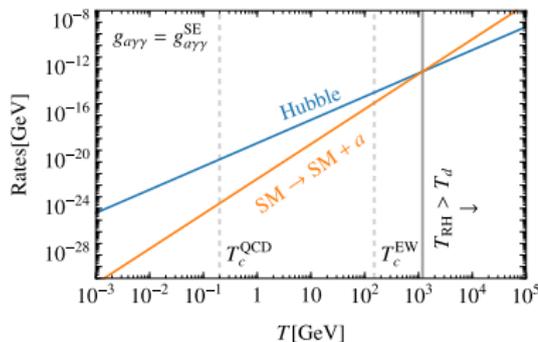
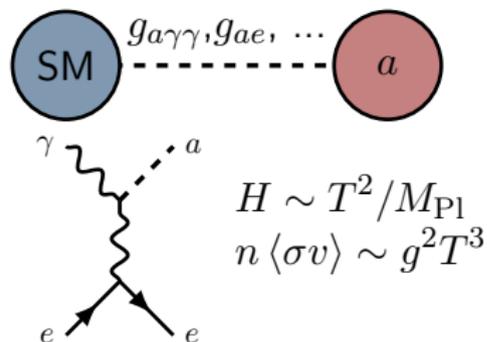
Thermalization with Standard Model



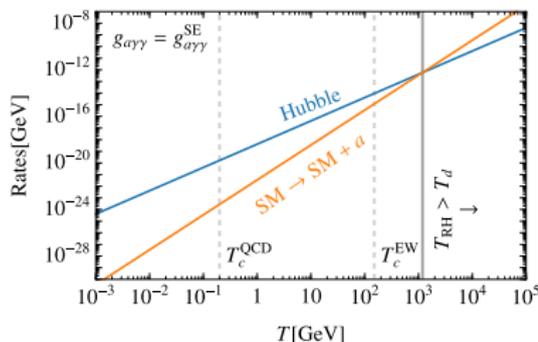
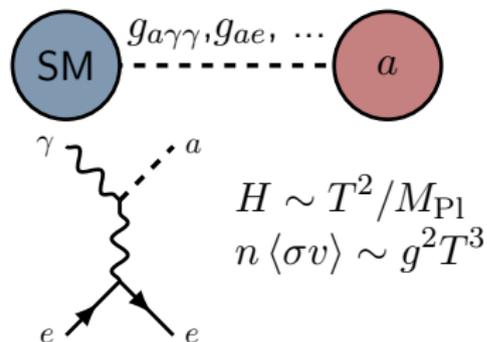
Thermalization with Standard Model



Thermalization with Standard Model



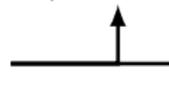
Thermalization with Standard Model



abundance dilutes with
Standard Model evolution

$$\frac{\rho_a}{\rho_\gamma} = \frac{1}{g_*(T_0)} \left(\frac{g_{*,S}(T_0)}{g_{*,S}(T_d)} \right)^{4/3}$$

Decoupling
temperature



other interactions
drive equilibrium?



spectrum (almost) fixed

$$\rho_a = \frac{1}{2\pi^2} \frac{\omega^4}{e^{\omega/T_a} - 1}$$

T_d is free-ish

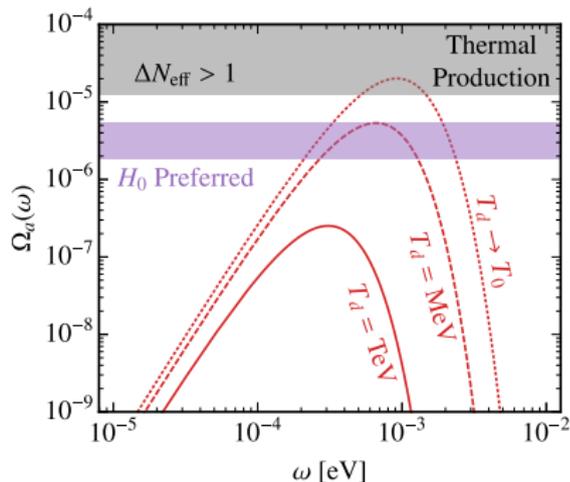
$$T_a \sim T_\gamma \sim 10^{-4} \text{eV}$$

spectrum (almost) fixed

$$\rho_a = \frac{1}{2\pi^2} \frac{\omega^4}{e^{\omega/T_a} - 1}$$

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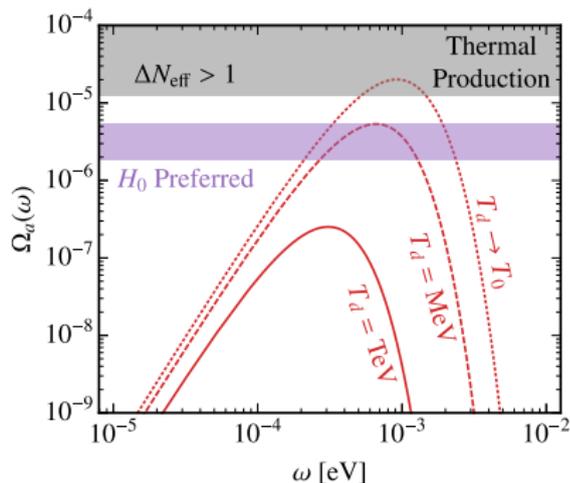


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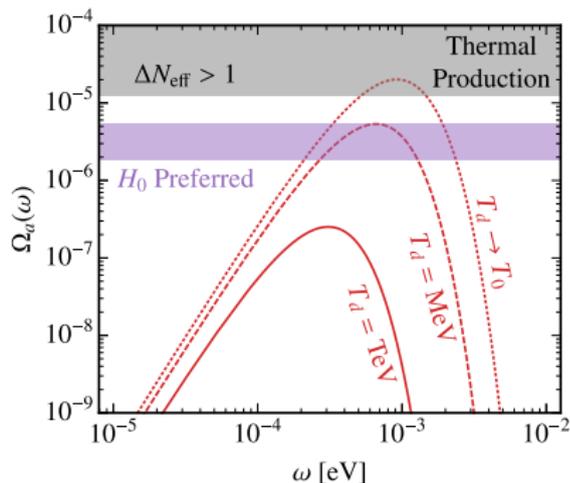
Detection prospects small numbers - $\mathcal{O}(10^3/\text{cm}^3)$
small energy deposits

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Detection prospects small numbers - $\mathcal{O}(10^3/\text{cm}^3)$
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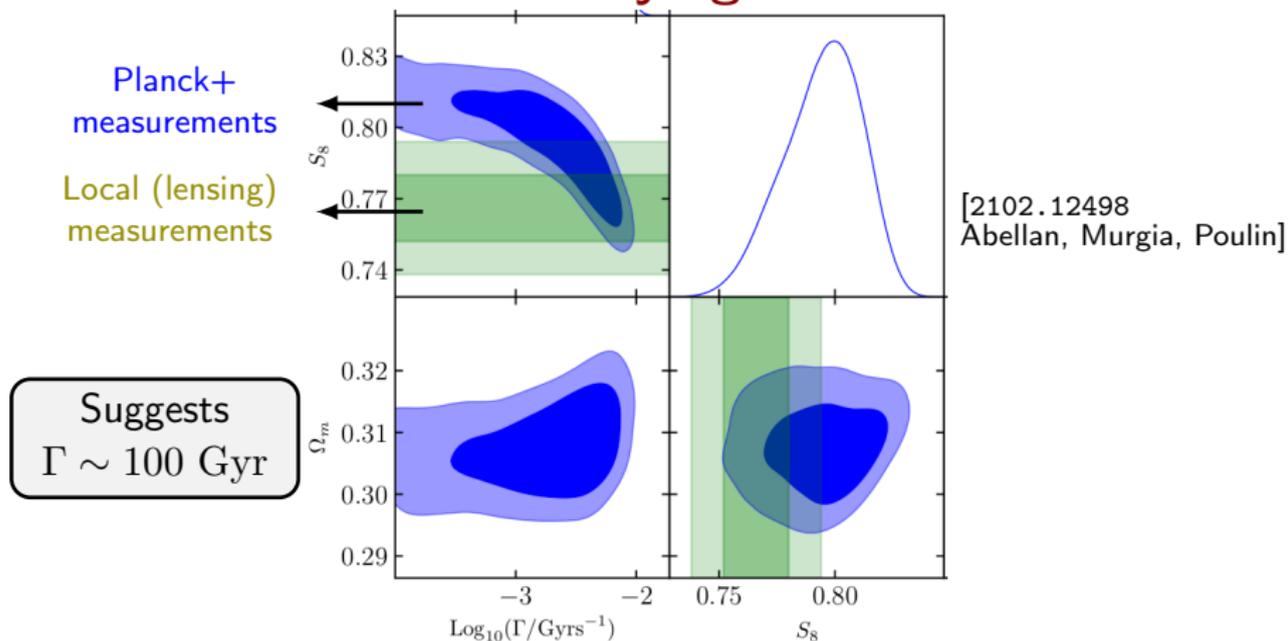
dedicated experiment?

$$N_{a \rightarrow \gamma} \simeq 10^9 \left(\frac{n_a}{100/\text{cm}^3} \right) \left(\frac{g_{a\gamma\gamma}}{g_{a\gamma\gamma}^{\text{SE}}} \right)^2 \left(\frac{B_0}{10 \text{ T}} \right)^2 \left(\frac{L}{10 \text{ m}} \right)^4 \left(\frac{t_{\text{exp}}}{\text{year}} \right)$$

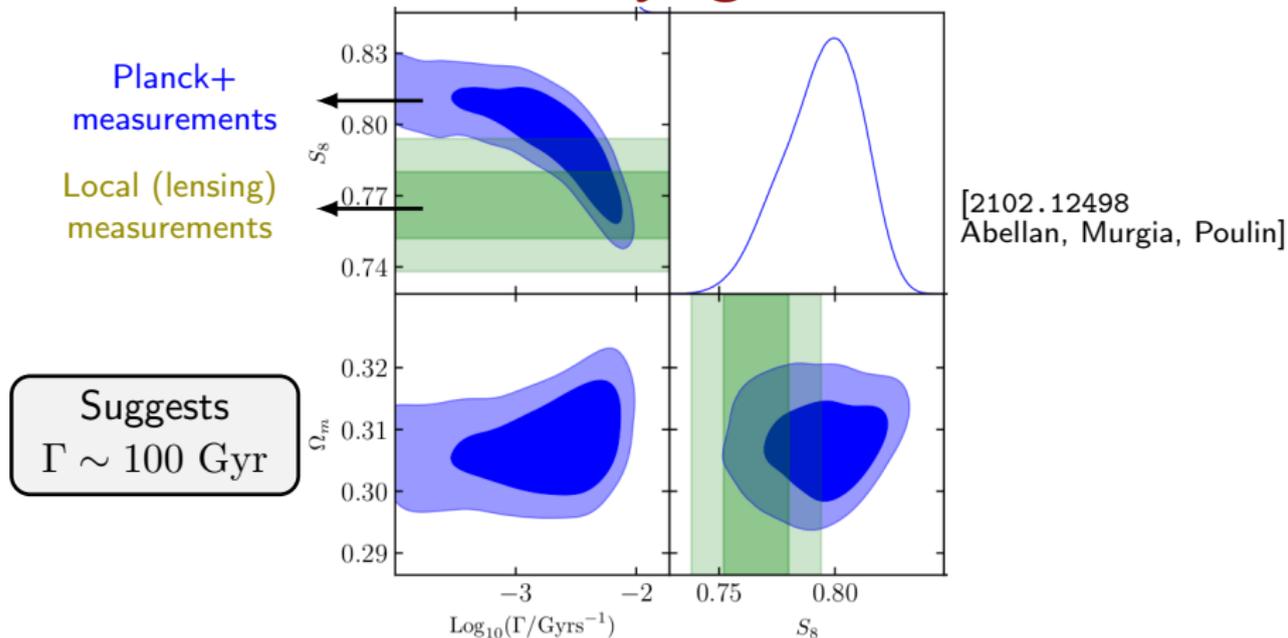


Dark matter decaying into axions?

Dark matter decaying into axions?



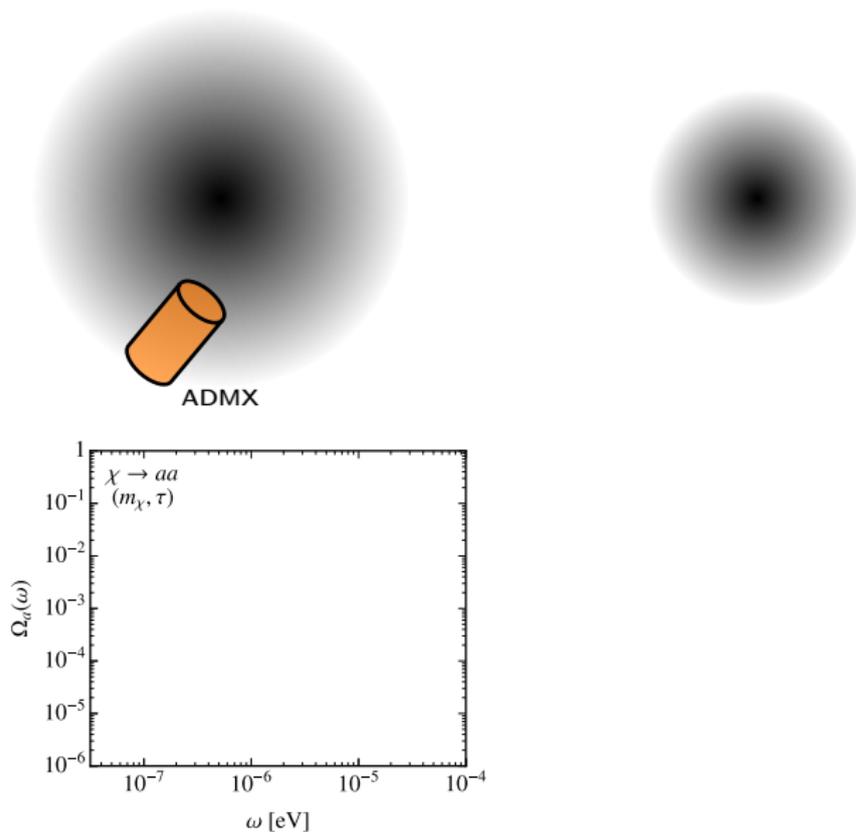
Dark matter decaying into axions?

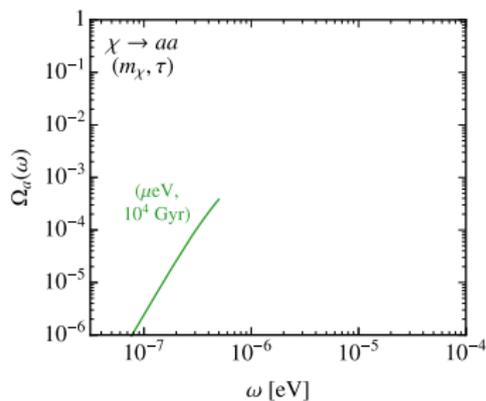
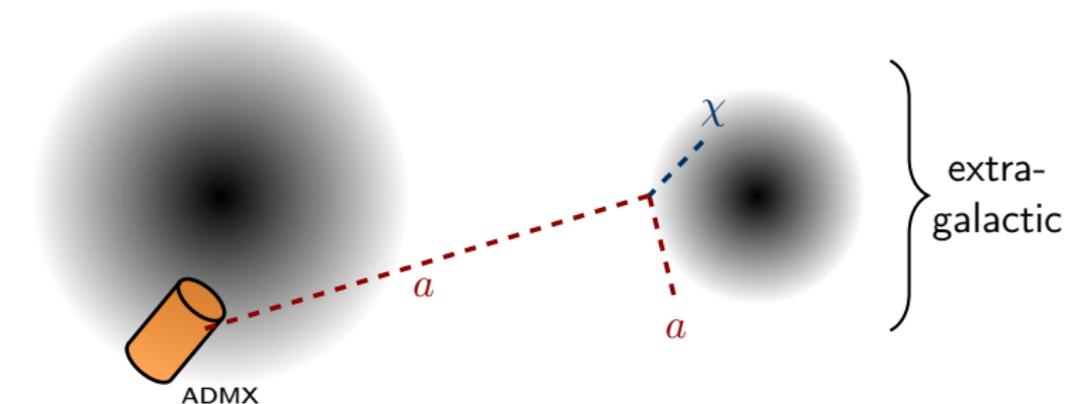


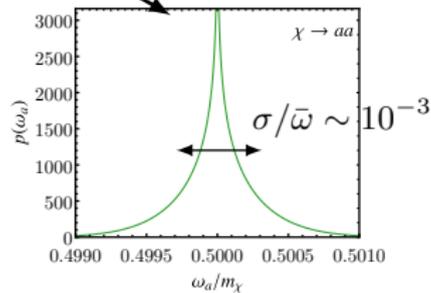
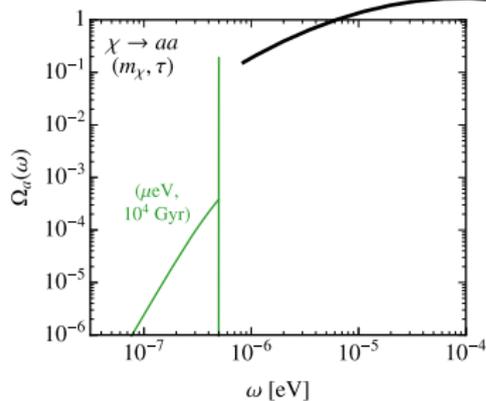
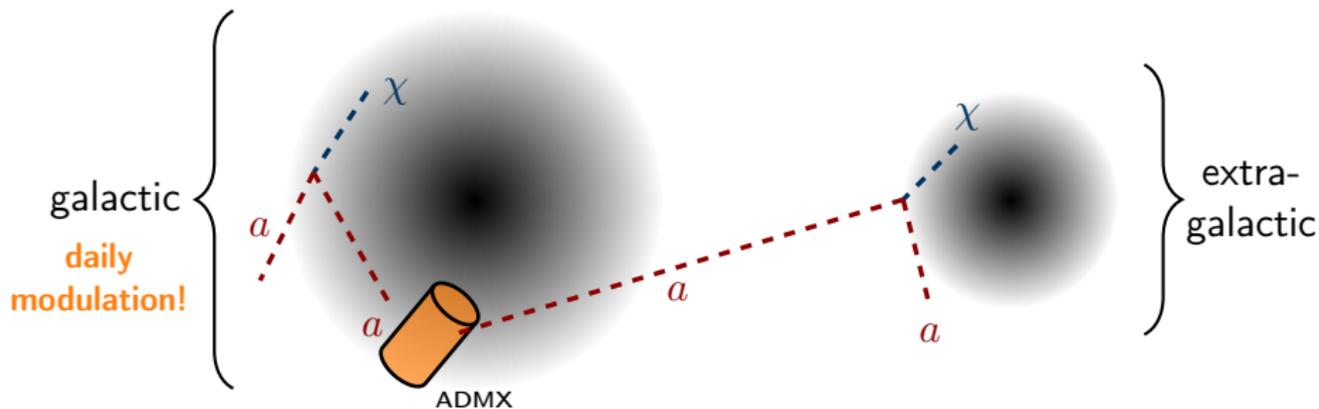
example
model

$$V(\Phi) = \lambda^2 \left(|\Phi|^2 - f_a^2 \right)^2$$

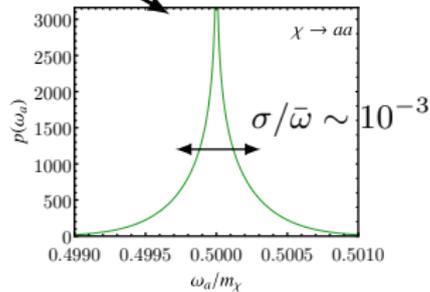
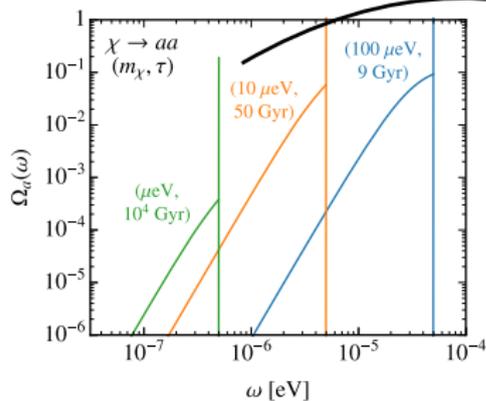
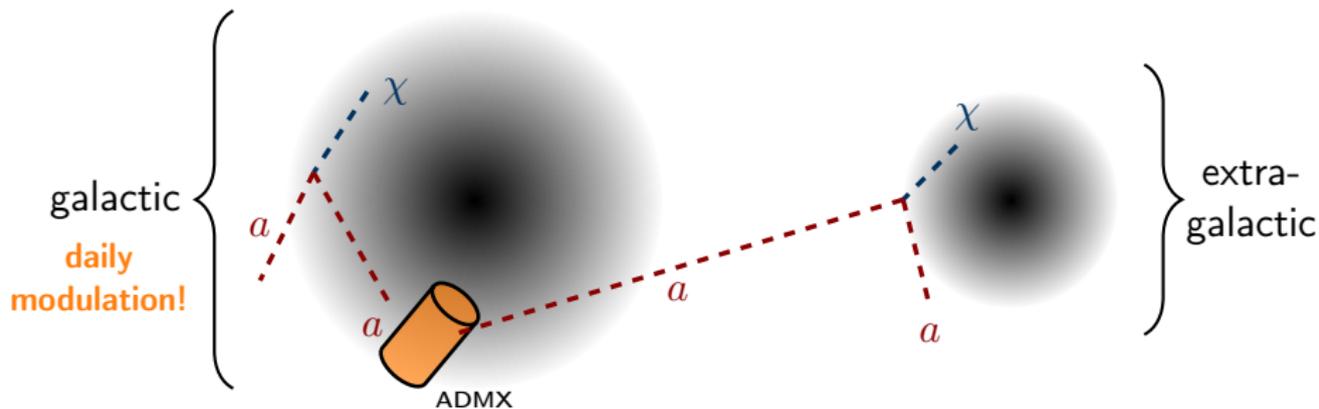
$$\Phi = (\chi + f_a) e^{ia/f_a}$$

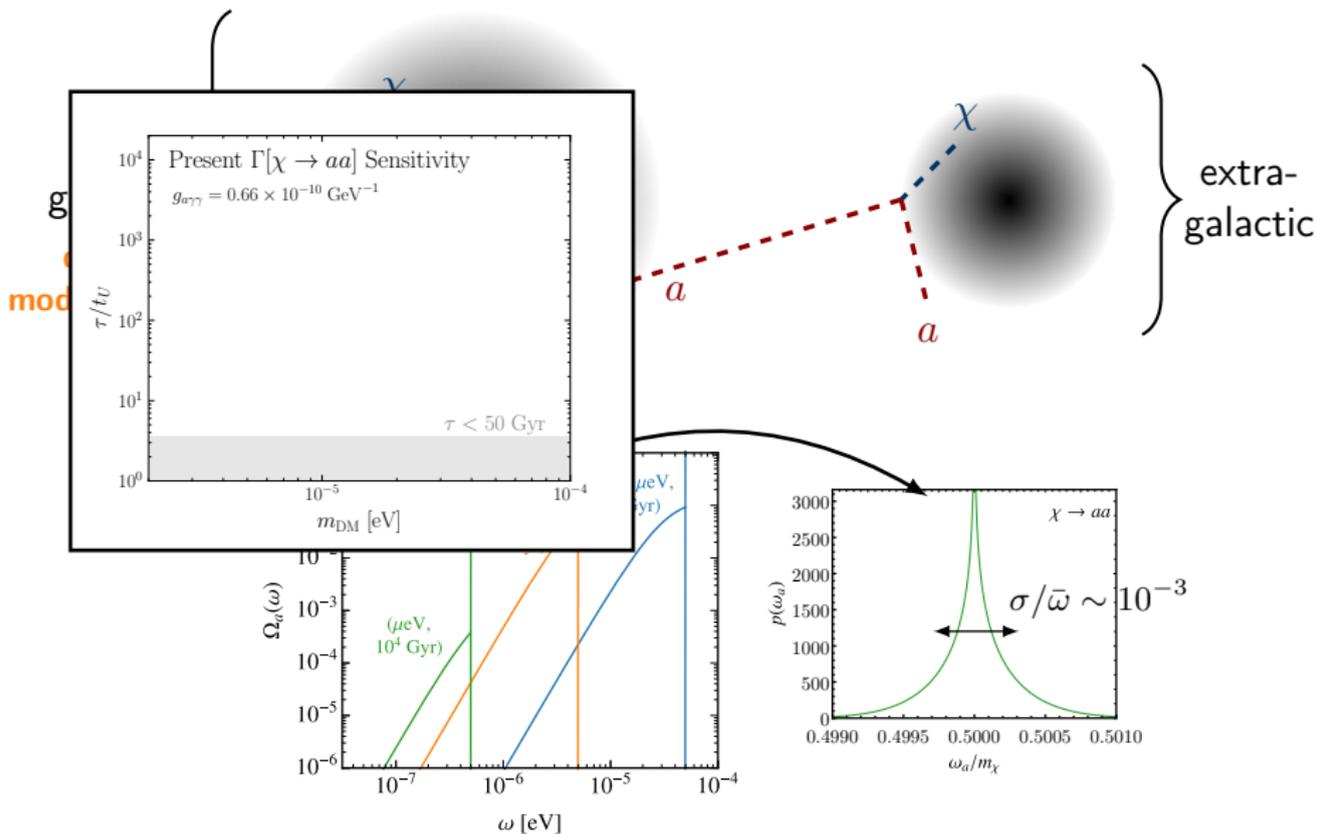


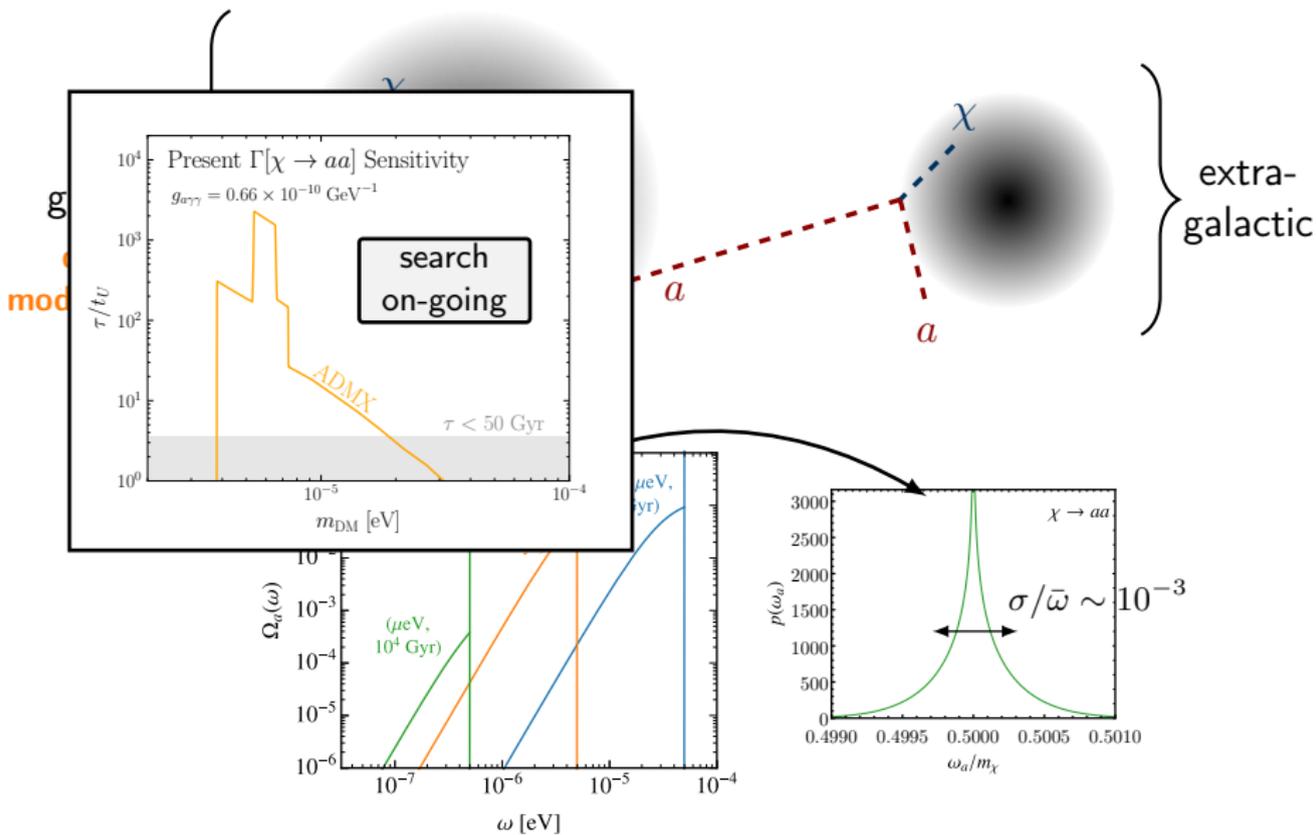


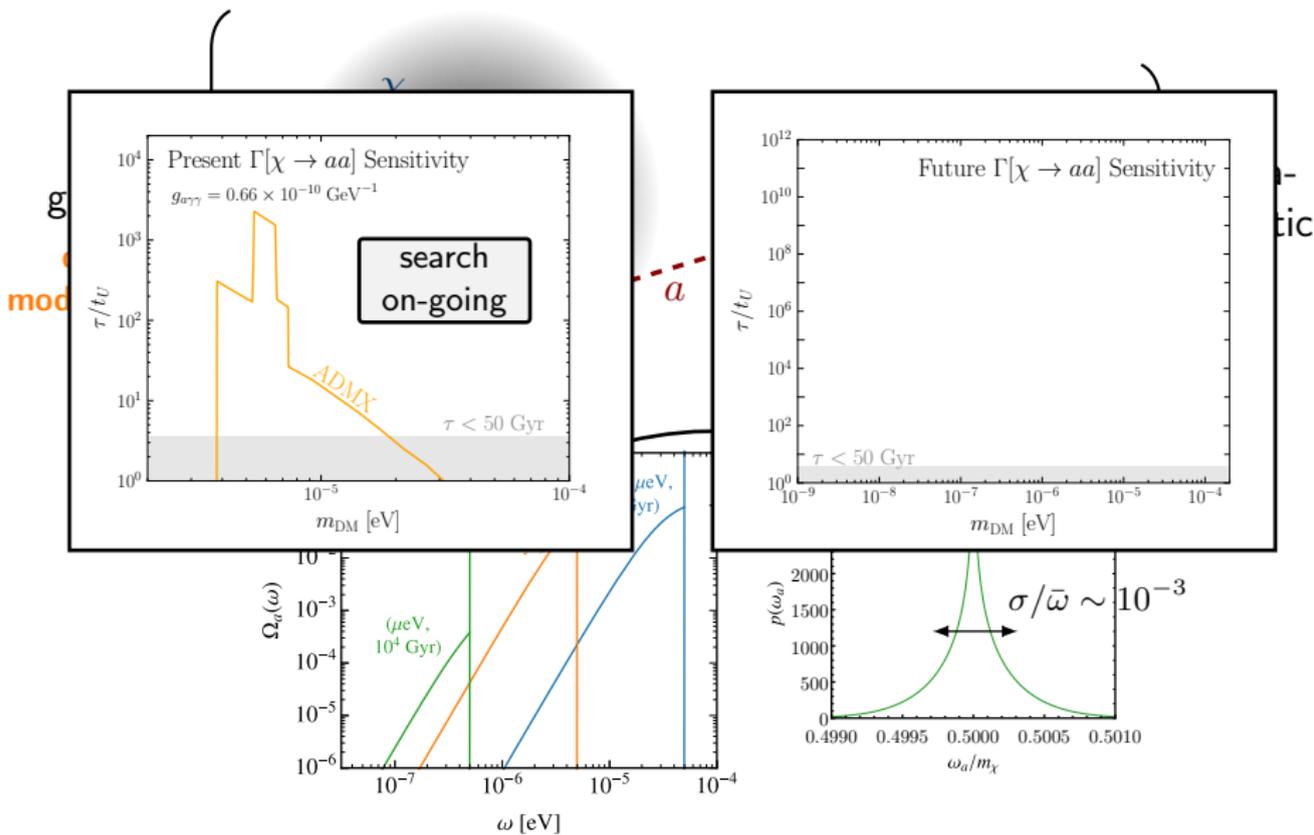


Dark matter decay

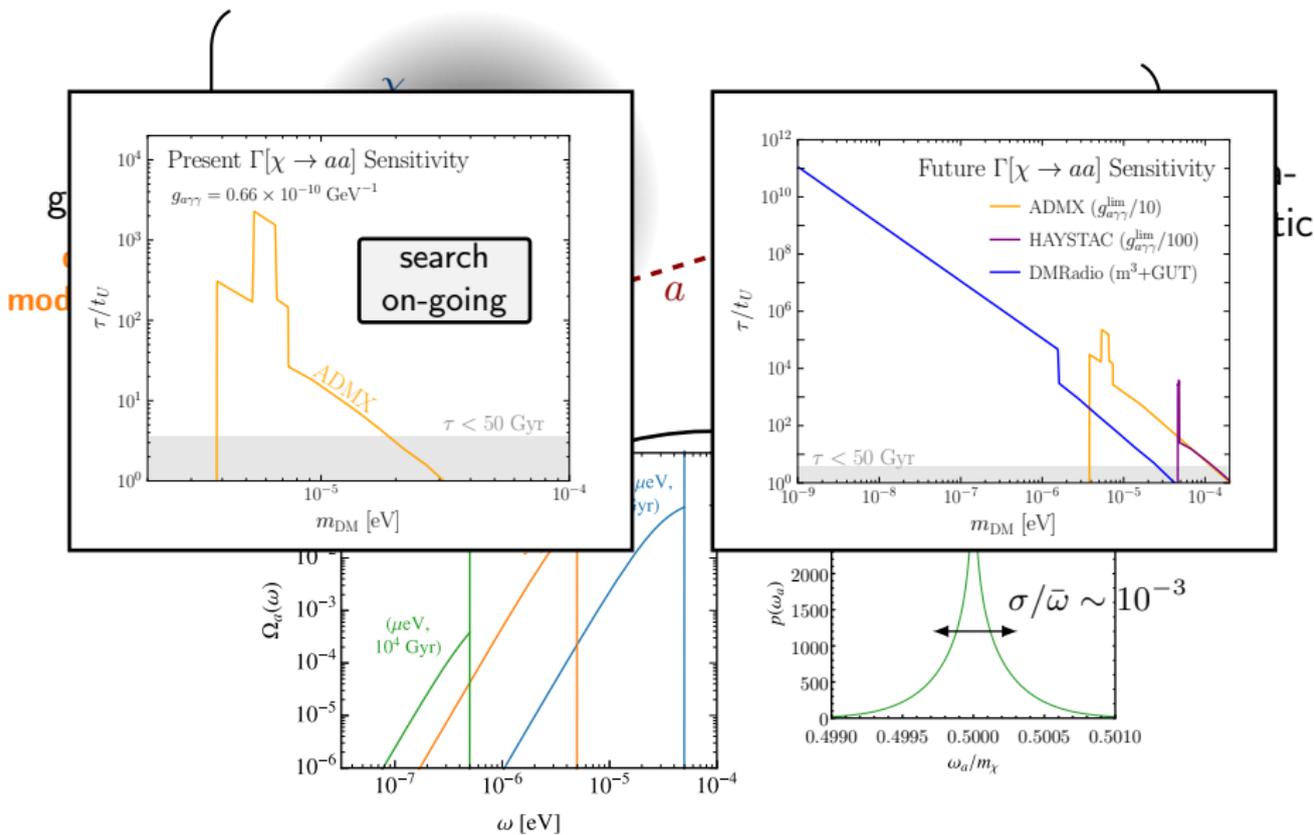


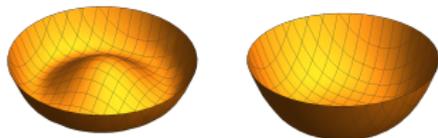




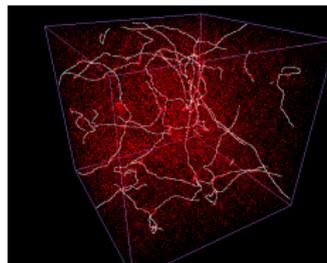


Dark matter decay

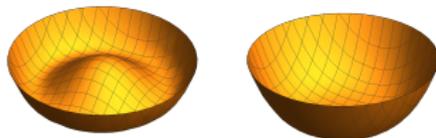




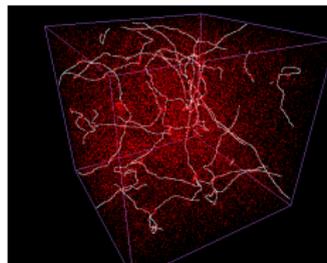
strings form upon
symmetry breaking



[- Ringeval, Bouchet]

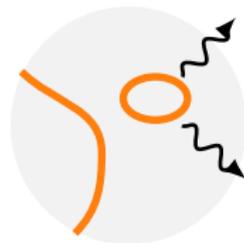
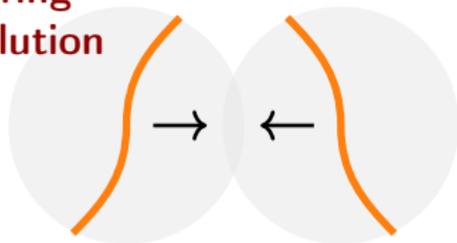


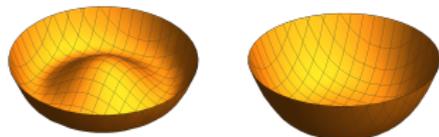
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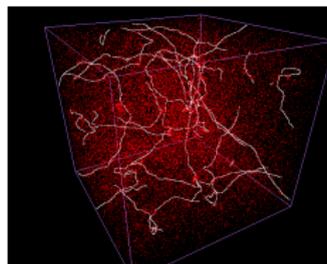
[- Ringeval, Bouchet]

string
evolution



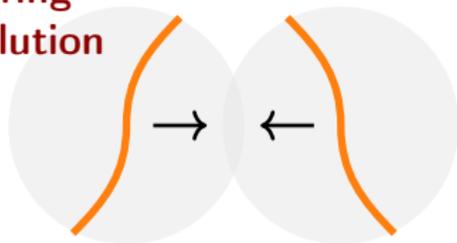


strings form upon
symmetry breaking



[- Ringeval, Bouchet]

**string
evolution**



most of energy
radiated in axions

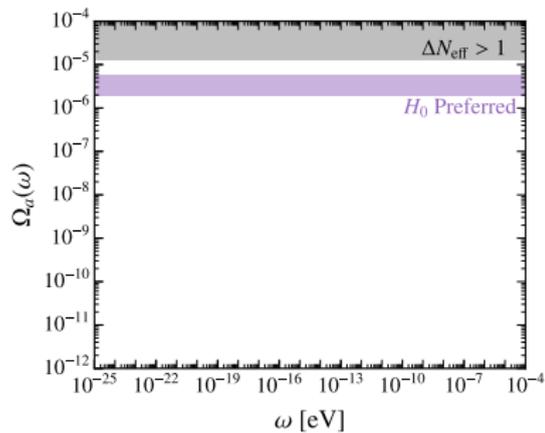
large loop
emission dominates?



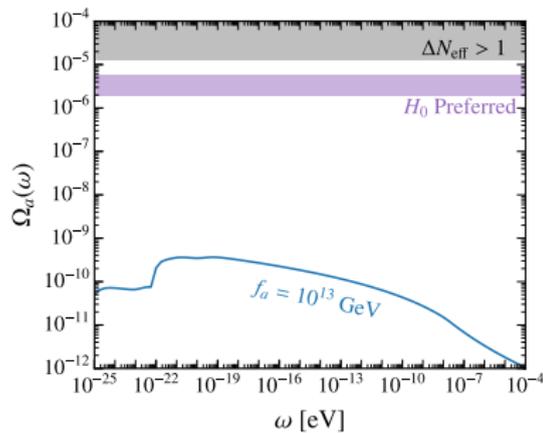
calculate axions
semi-analytically

[Gorghetto, Hardy, Villadoro - 1806.04677, 2007.04990]

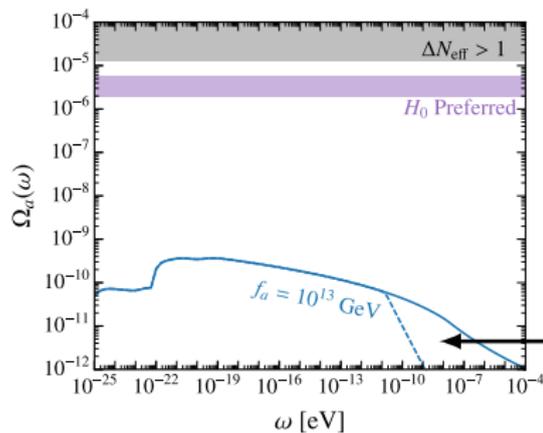
The string spectrum



The string spectrum



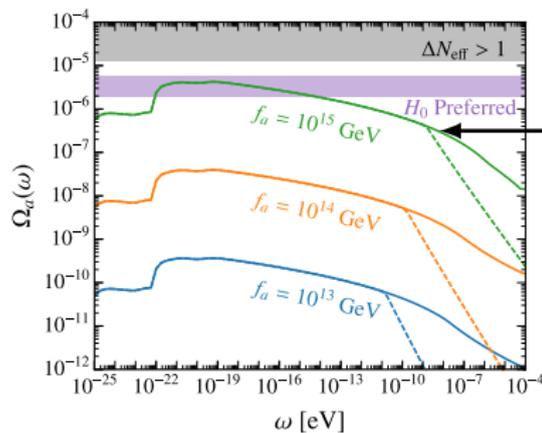
The string spectrum



uncertainty
in start of
scaling

[Hindmarsh, Lizarraga,
see, e.g., Lopez-Eiguren, Urrestilla
2102.07723]

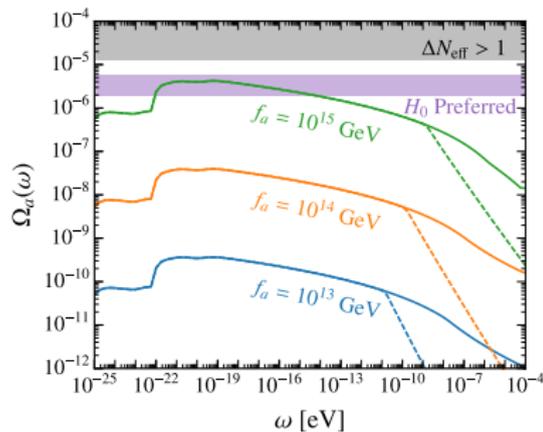
The string spectrum



large f_a
needed
for $\rho_a \sim \rho_\gamma$

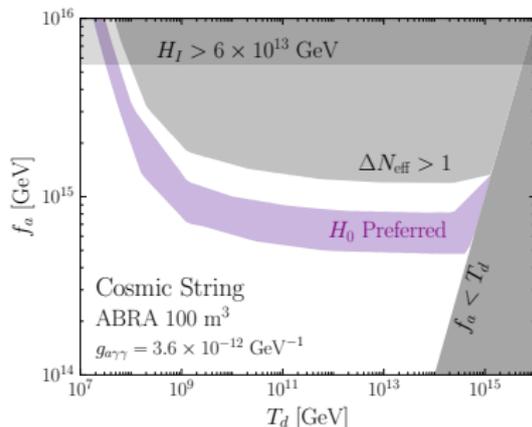
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The string spectrum



[Hindmarsh, Lizarraga,
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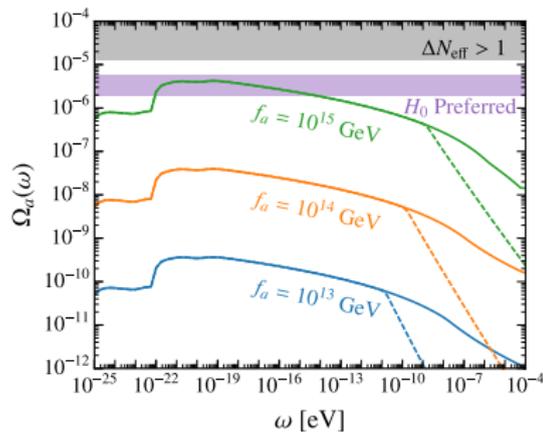
Experimental sensitivity



$$f_a \lesssim 10^{14} \text{ GeV if } m_a \lesssim 10^{-28}$$

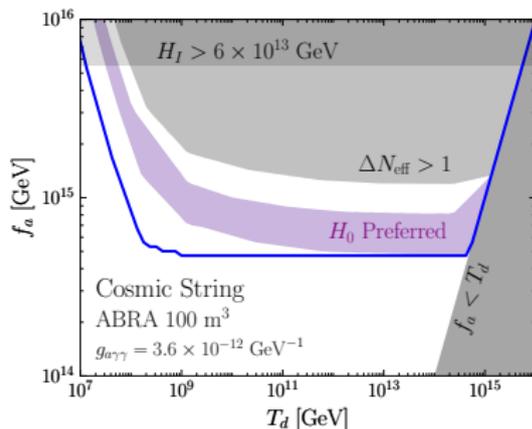
[Lopez-Eiguren, Lizarraga,
Hindmarsh, Urrestilla
1705.04154]

The string spectrum



[Hindmarsh, Lizarraga,
see, e.g., Lopez-Eiguren, Urrestilla
2102.07723]

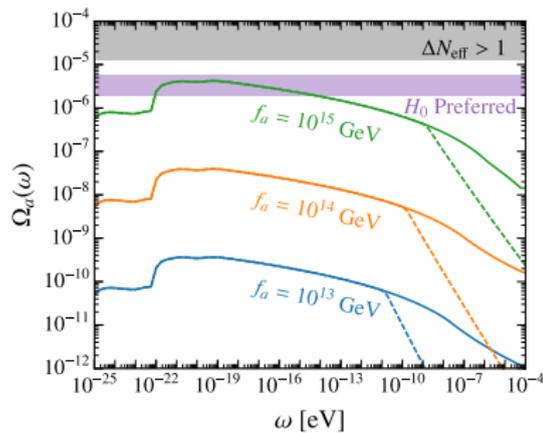
Experimental sensitivity



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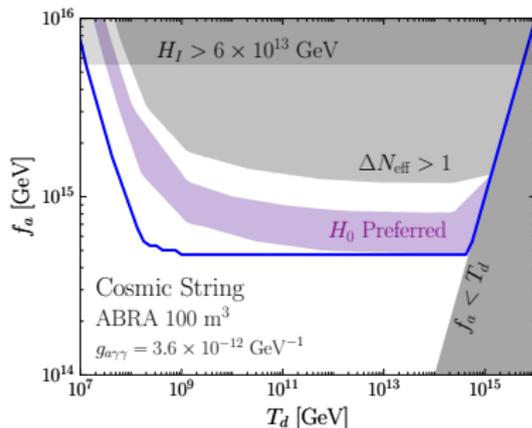
The string spectrum



[Hindmarsh, Lizarraga,
see, e.g., Lopez-Eiguren, Urrestilla
2102.07723]

Upcoming experiments probe $g_{a\gamma\gamma} \gg \frac{\alpha}{4\pi f_a}$
Requires clockwork or related mechanisms

Experimental sensitivity

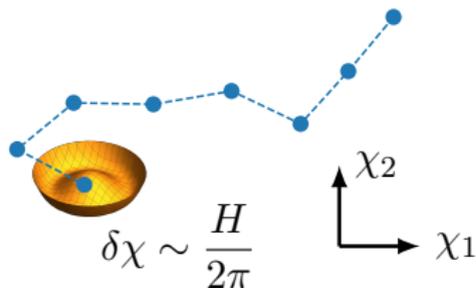


$f_a \lesssim 10^{14}$ GeV if $m_a \lesssim 10^{-28}$

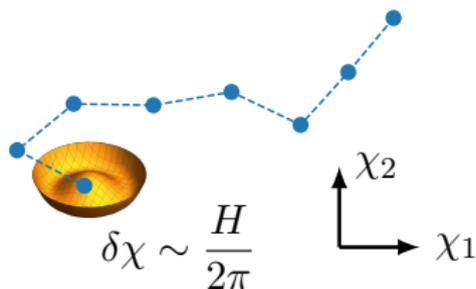
[Lopez-Eiguren, Lizarraga,
Hindmarsh, Urrestilla
1705.04154]



Scalar pushed
from minimum
during inflation

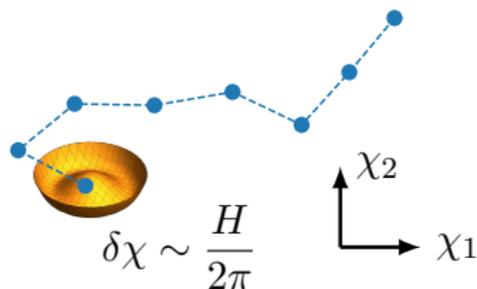


Scalar pushed
from minimum
during inflation



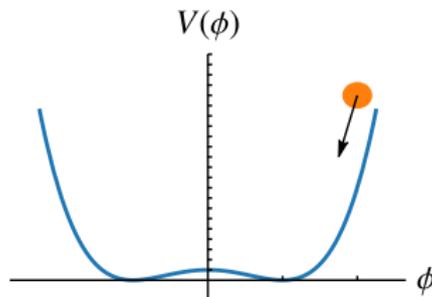
$\chi_i \gg f_a$ at end of inflation

Scalar pushed
from minimum
during inflation

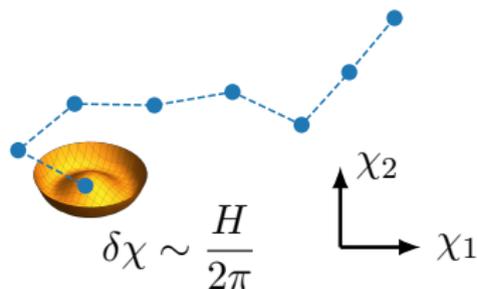


$\chi_i \gg f_a$ at end of inflation

Scalar oscillations
produce axions
when $H \sim m_{\text{eff}}(\chi)$

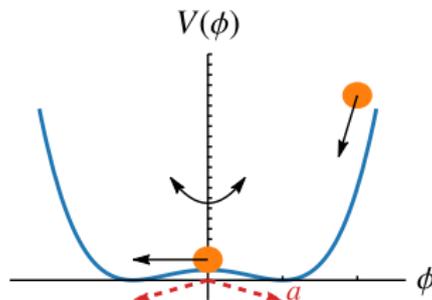


Scalar pushed
from minimum
during inflation

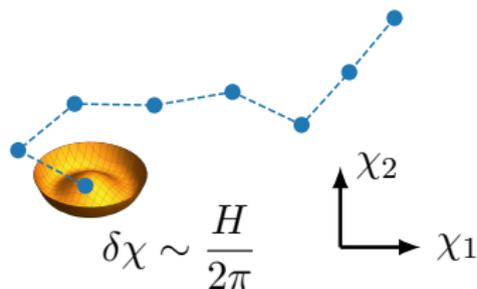


$\chi_i \gg f_a$ at end of inflation

Scalar oscillations
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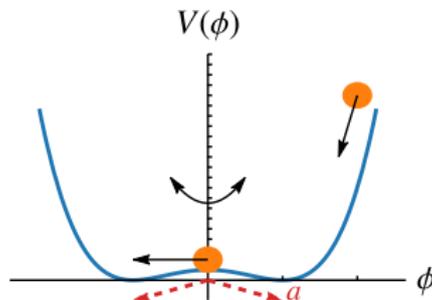


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$\Omega_a \sim \text{Gaussian}$



$$V(\Phi) = \lambda^2 \left(|\Phi|^2 - f_a^2 \right)^2$$

Oscillations when
 $m_\chi^{\text{eff}}(\chi_i) \simeq \lambda \chi_i \sim H$

Typical energy:

Energy density:

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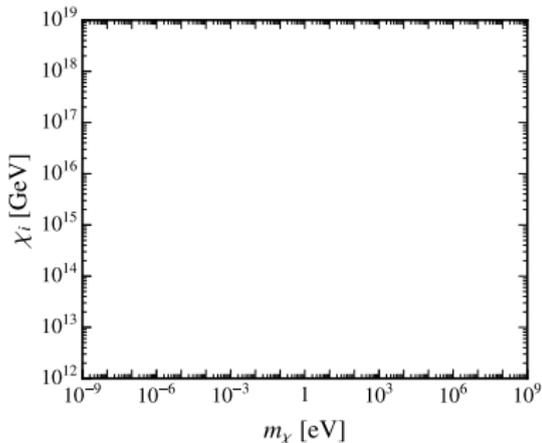
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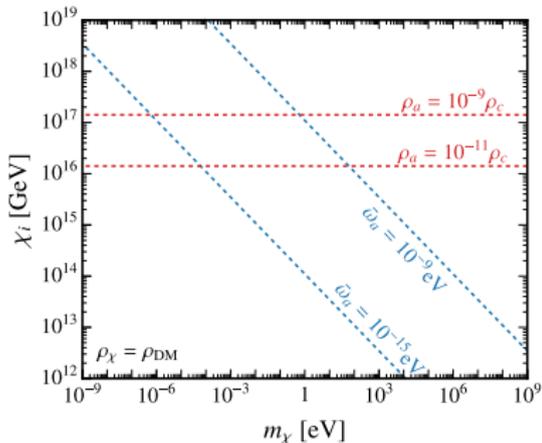
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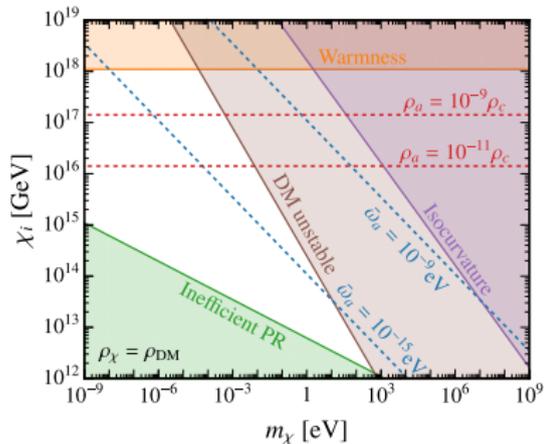
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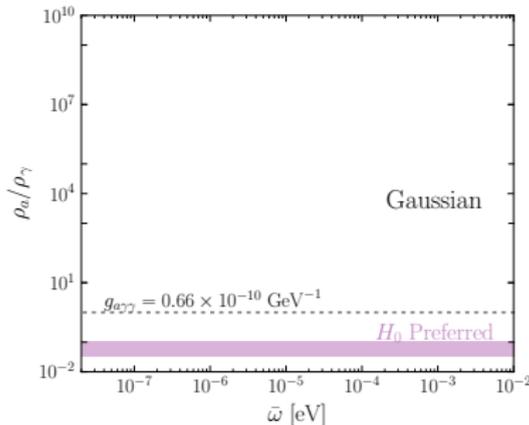
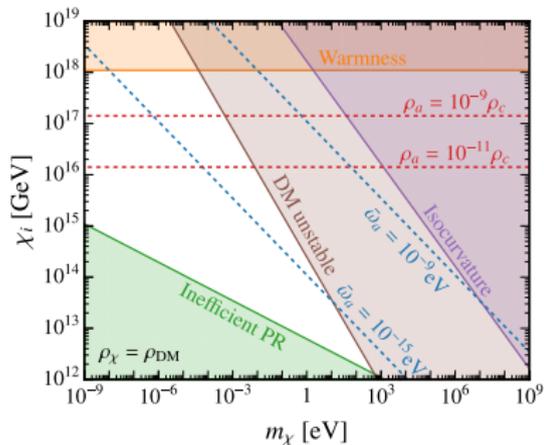
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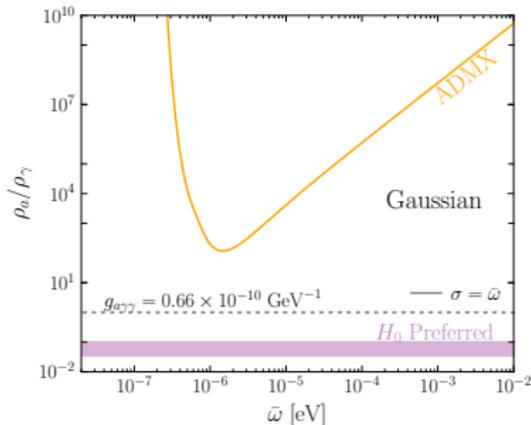
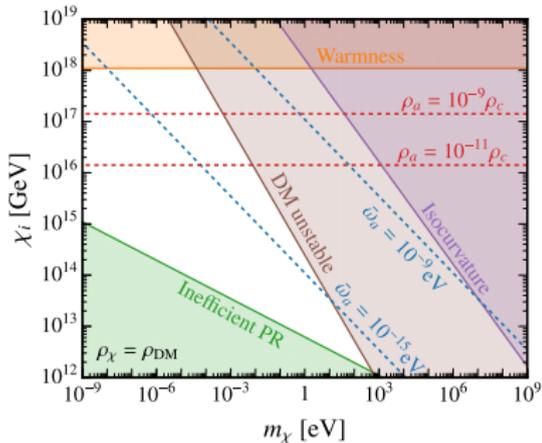
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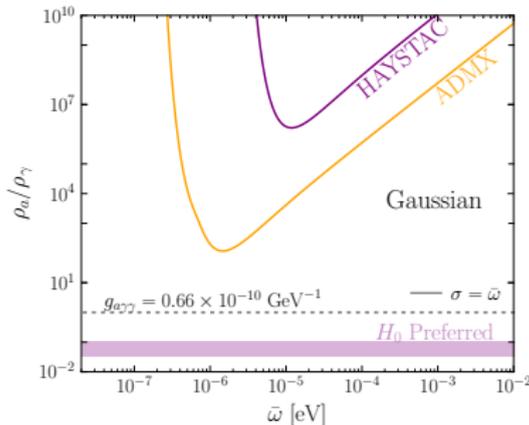
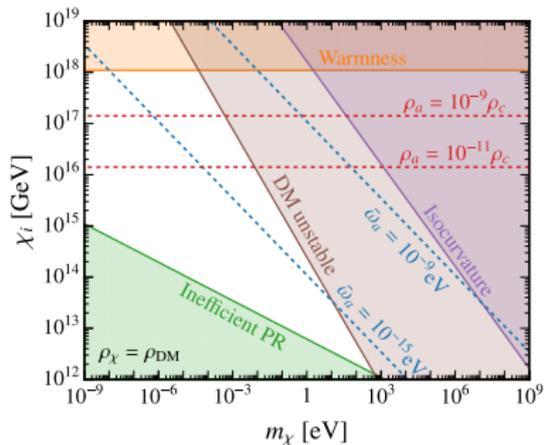
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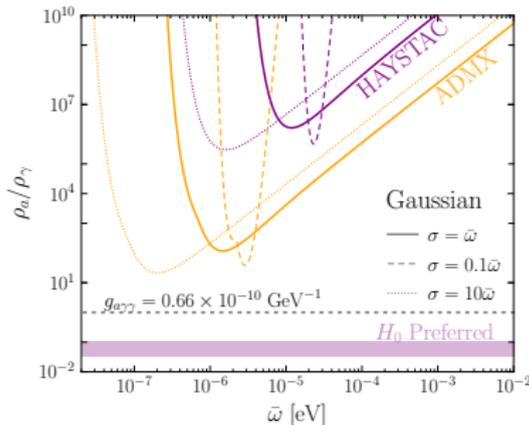
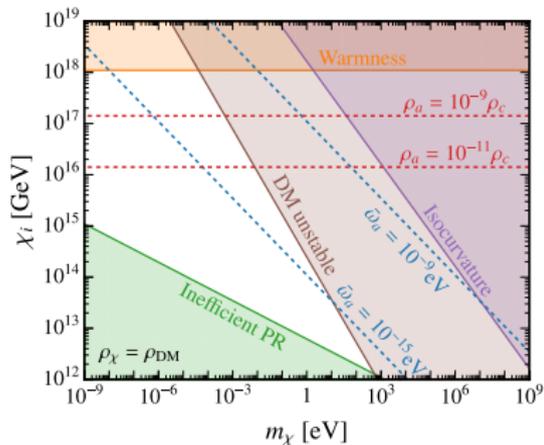
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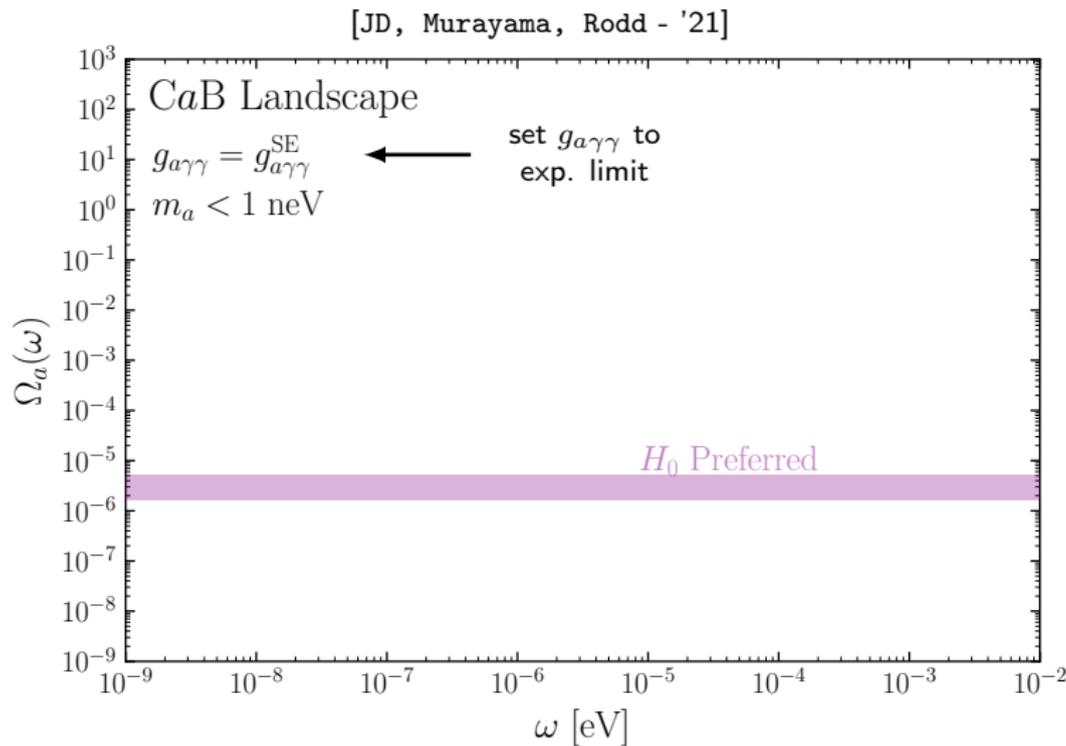
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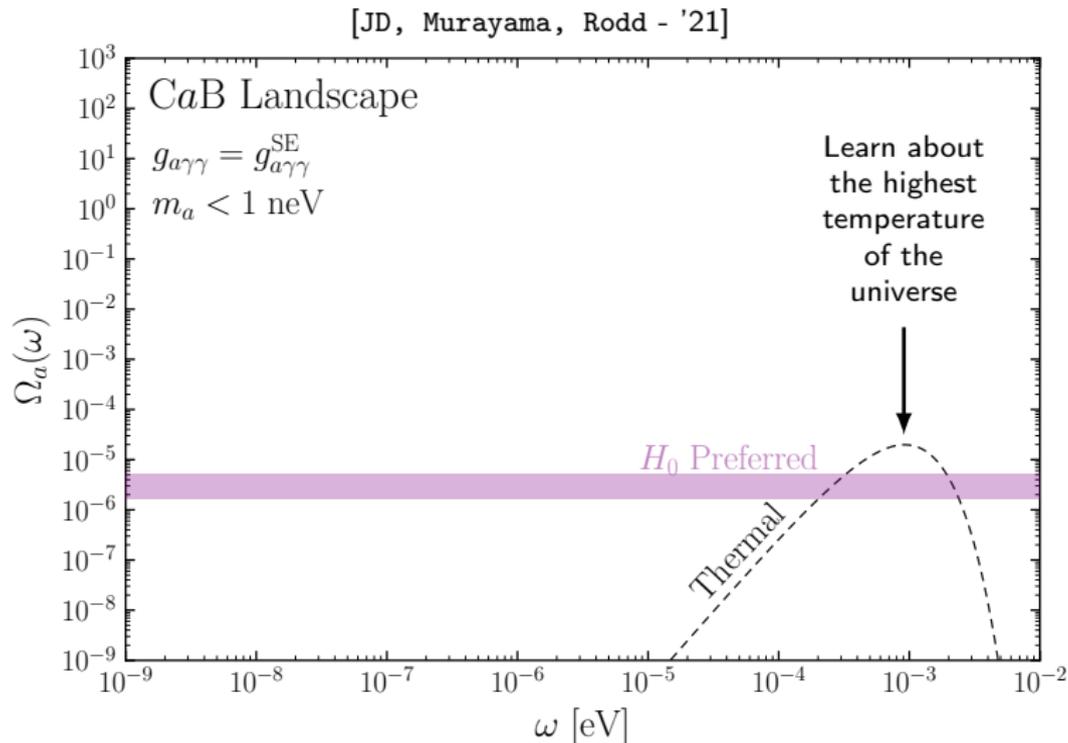
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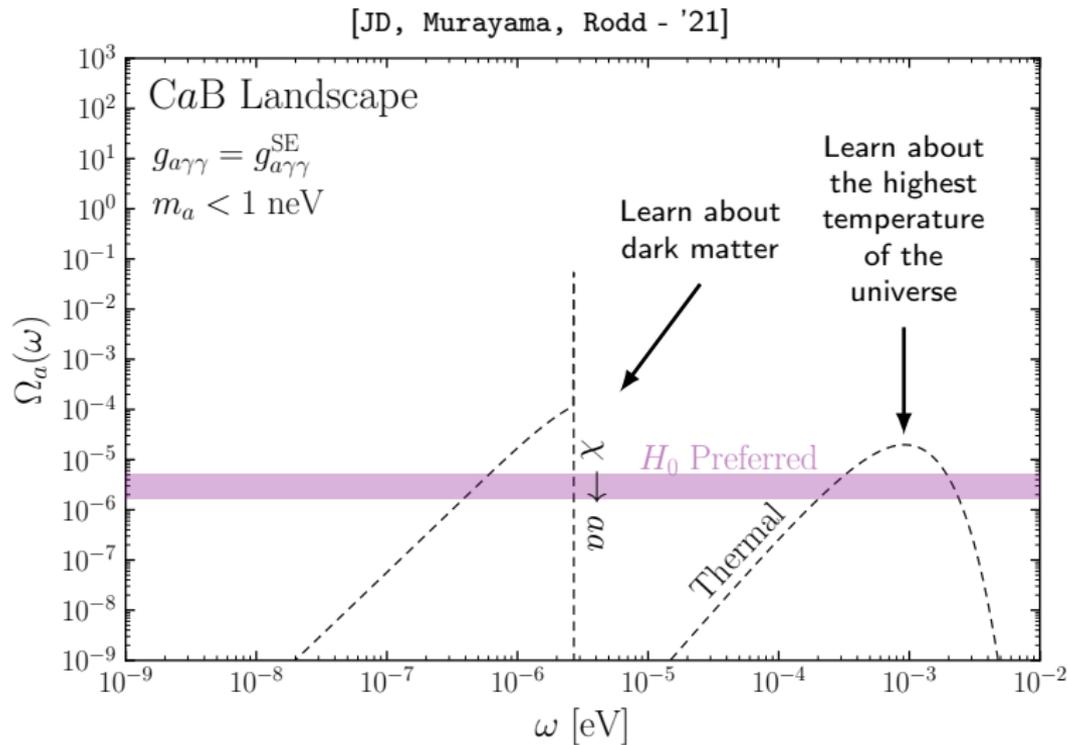
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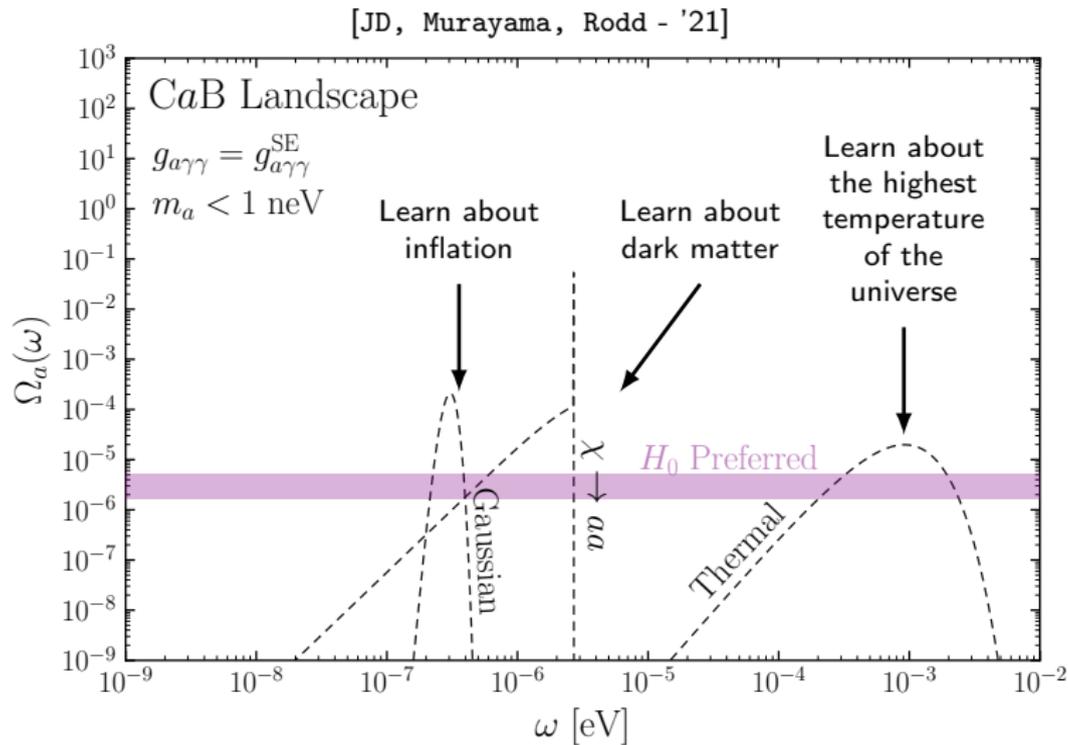
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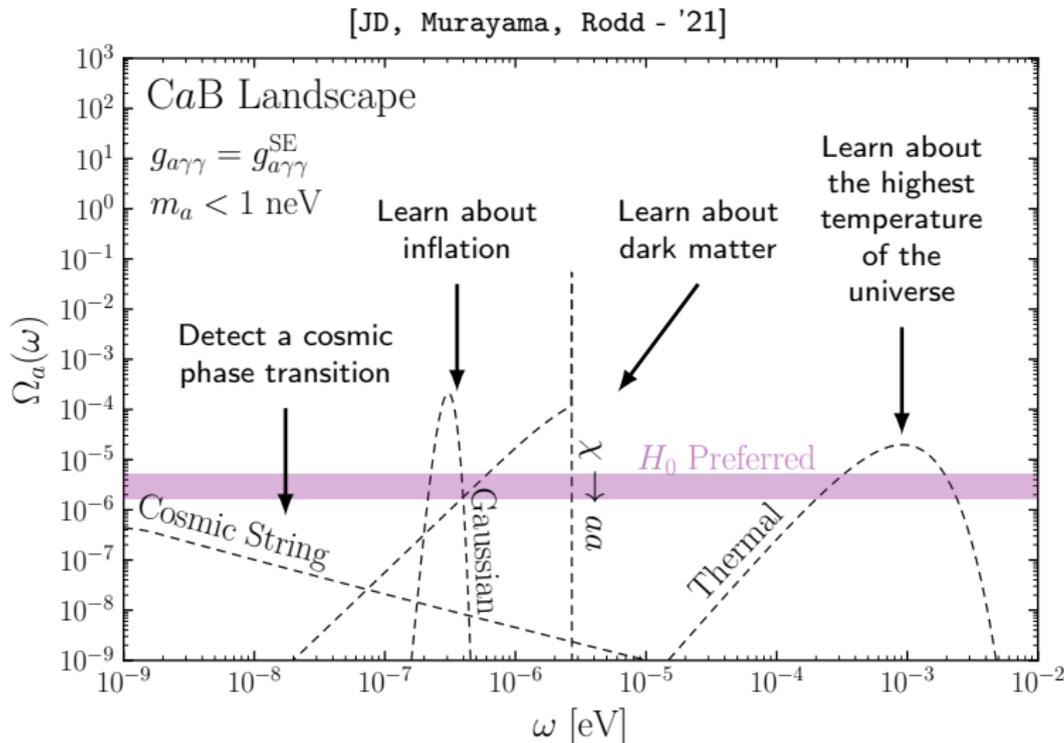


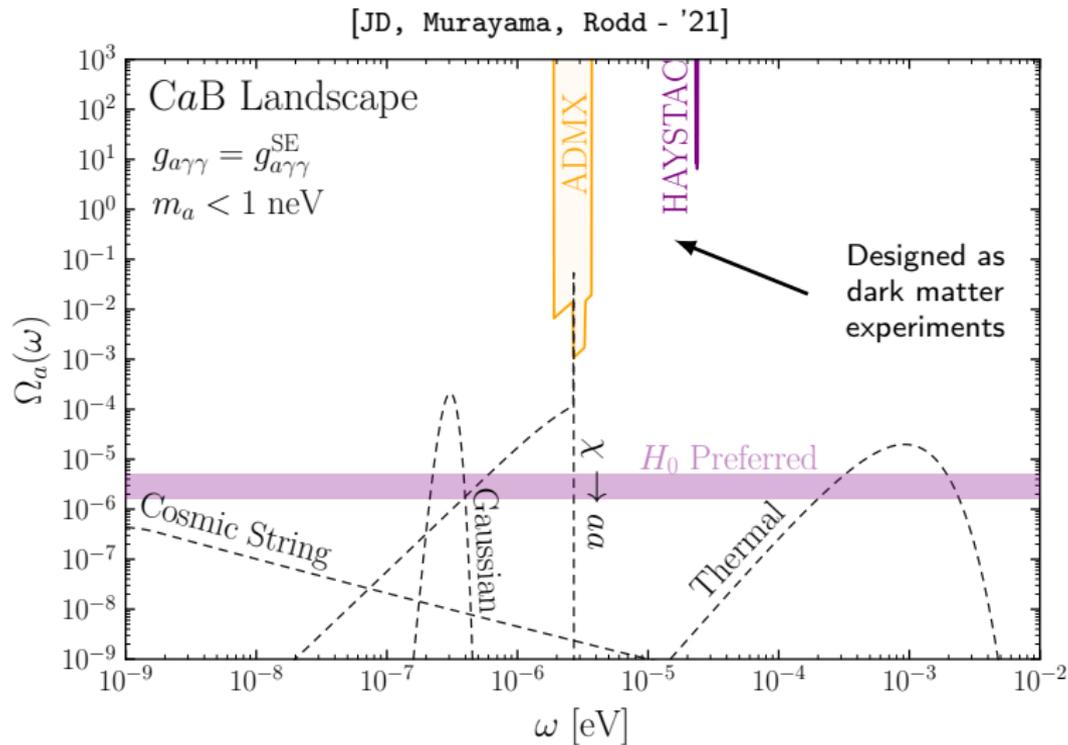


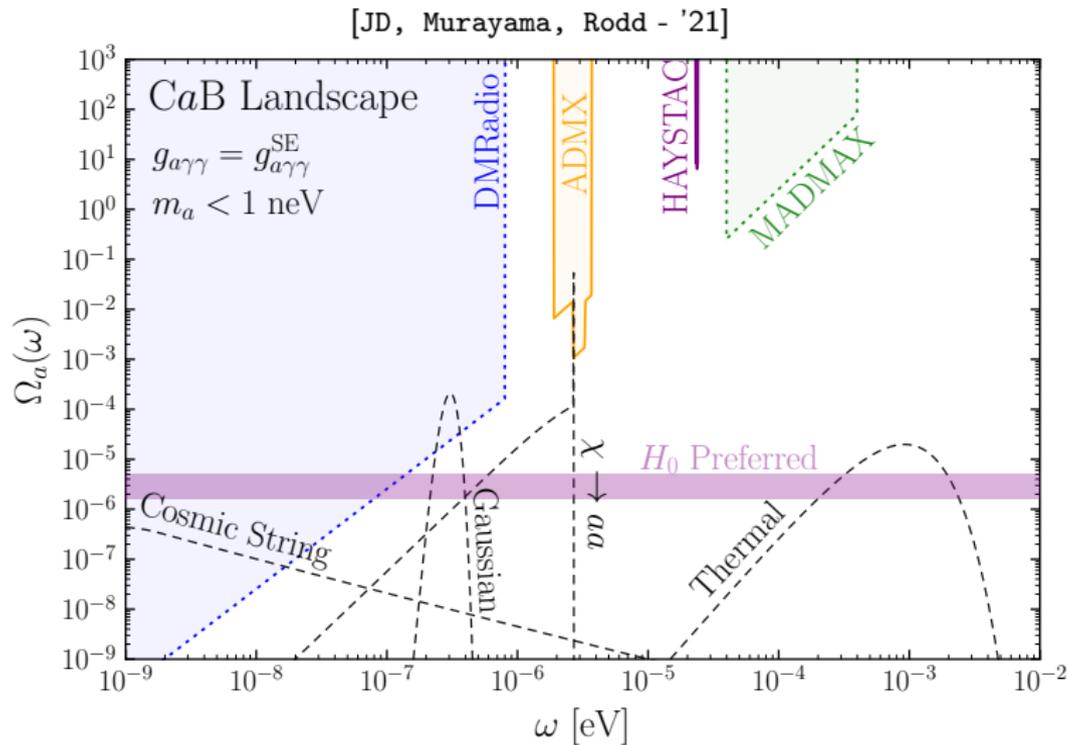


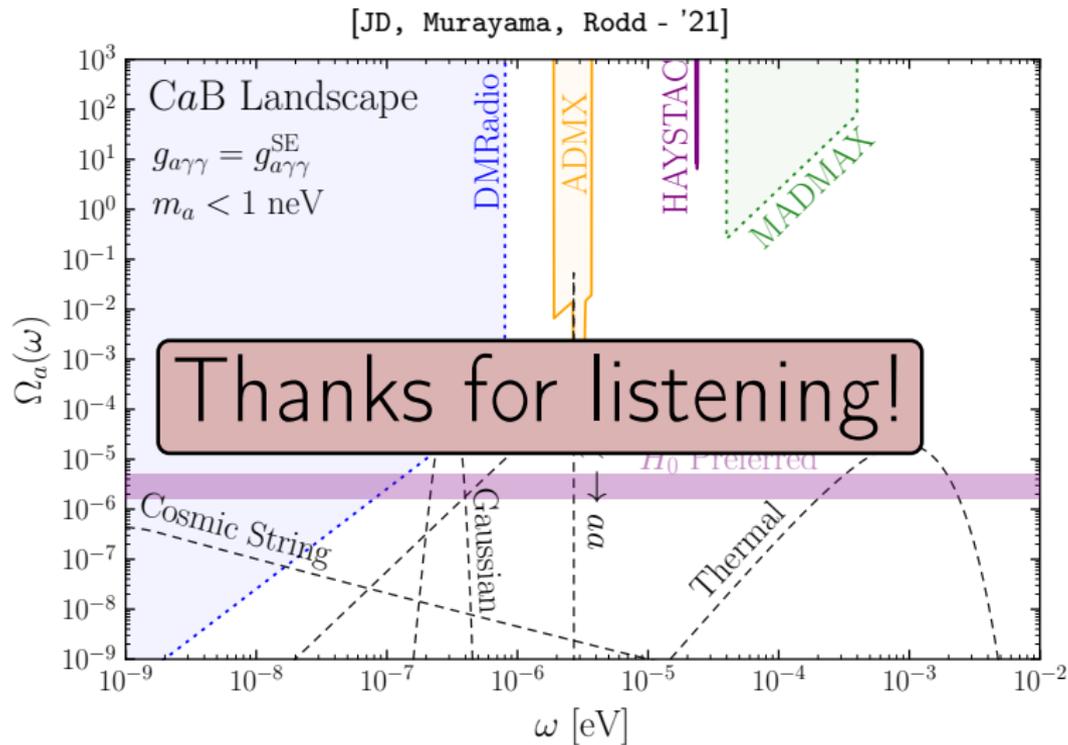














How to probe $\omega \ll \text{meter}^{-1}$?

$$\vec{\mathbf{J}}_{\text{eff}} = g_{a\gamma\gamma} \vec{\mathbf{B}}_0 \partial_t a - g_{a\gamma\gamma} \vec{\mathbf{E}}_0 \times \nabla a$$

LC circuit for readout

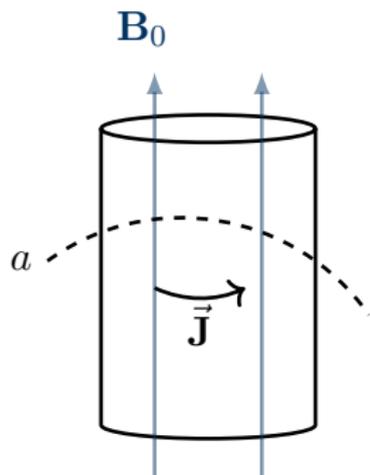
[1310.8545 - Sikivie, Sullivan, Tanner]

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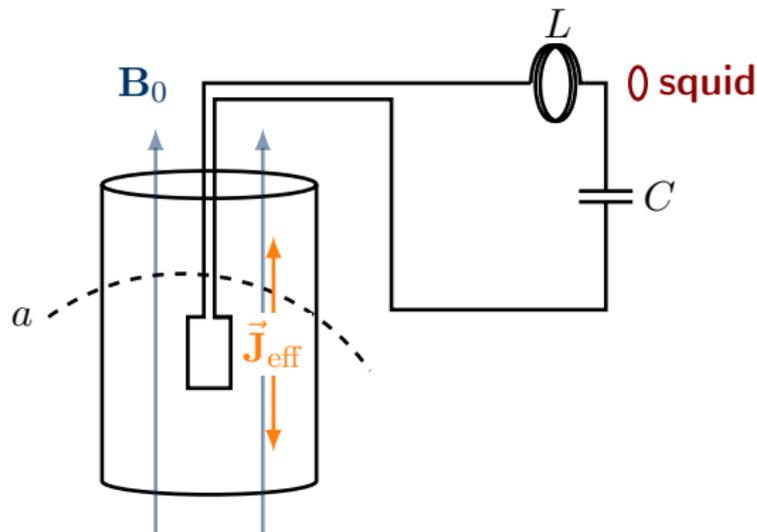
“ABRACADABRA”
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[1310.8545 - Sikivie, Sullivan, Tanner]



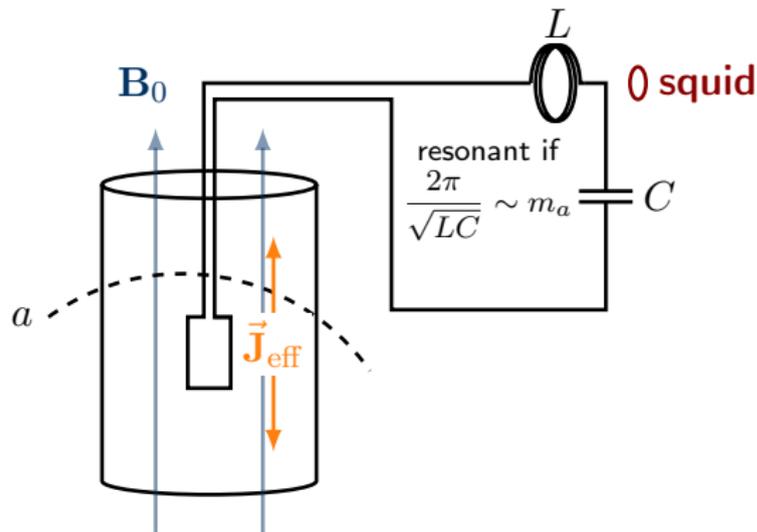
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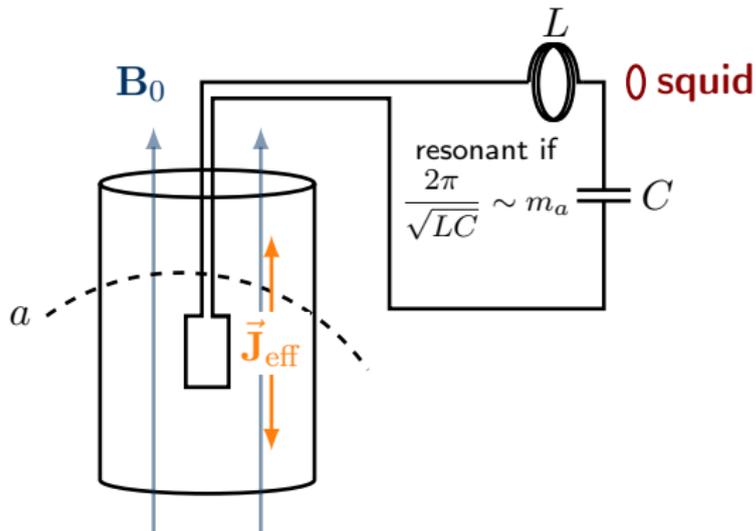
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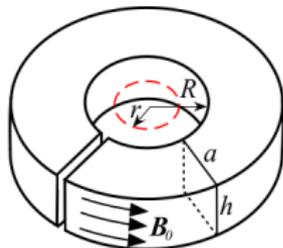


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[1310.8545 - Sikivie, Sullivan, Tanner]

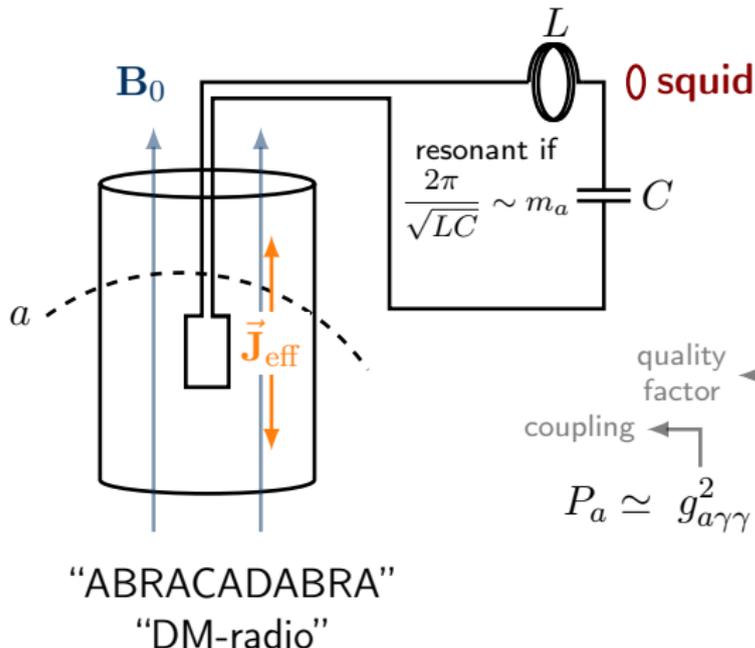
Toroid is better?



[Kahn, Safdi, Thaler
1602.01086]

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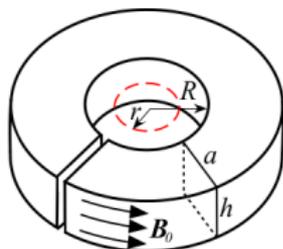
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LC circuit for readout

[1310.8545 - Sikivie, Sullivan, Tanner]

Toroid is better?



[Kahn, Safdi, Thaler
1602.01086]

quality factor
coupling

volume

$$P_a \simeq g_{a\gamma\gamma}^2 Q_a n_a B_0^2 V_B C \rightarrow \mathcal{O}(10^{-2})$$

\downarrow number density \downarrow magnetic field