

Opening the chamber of secrets to revive sterile neutrino dark matter

Manibrata Sen

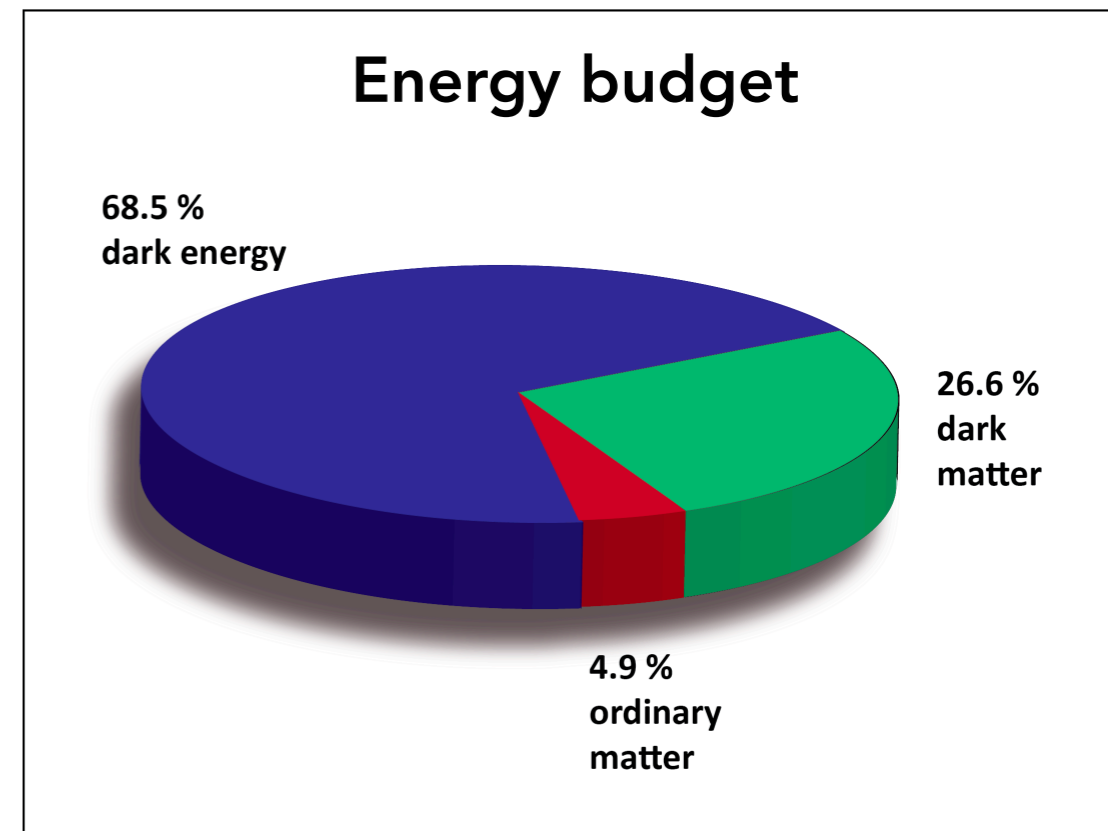
Max-Planck-Institut für Kernphysik, Heidelberg

13.06.23

HIDDeN & ASYMMETRY Webinar



The Standard Model of Particle Physics

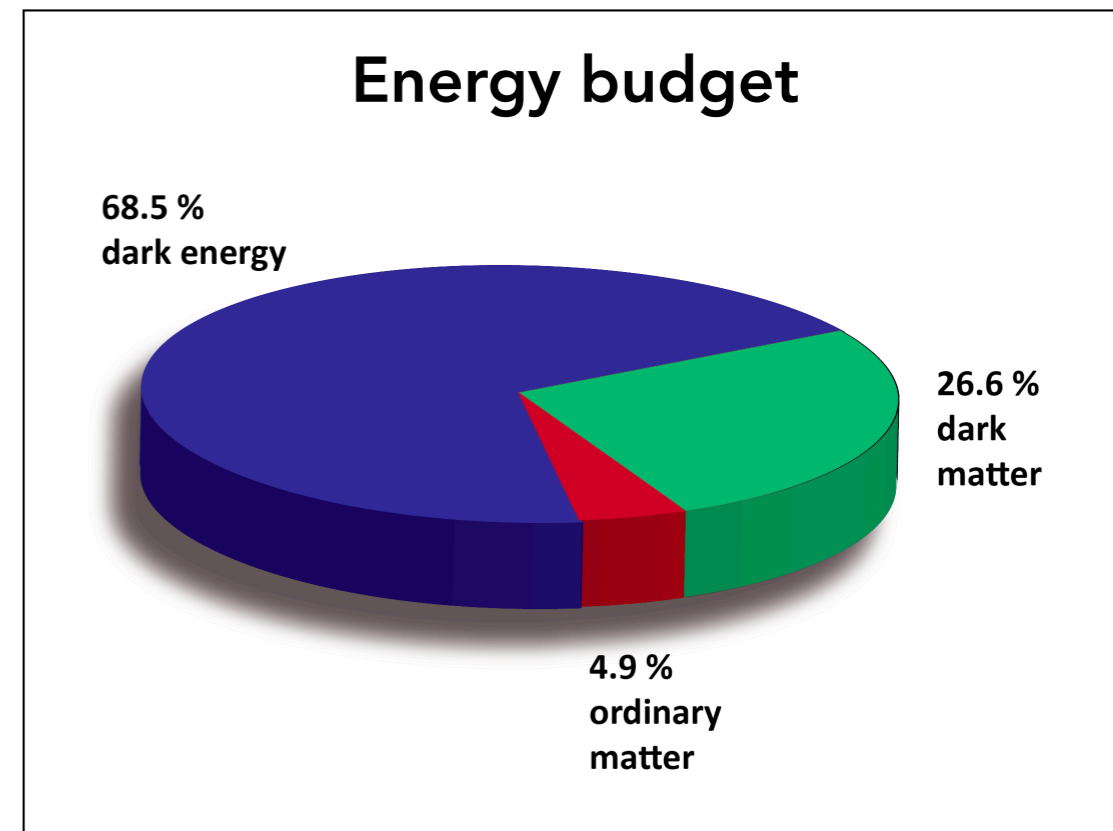
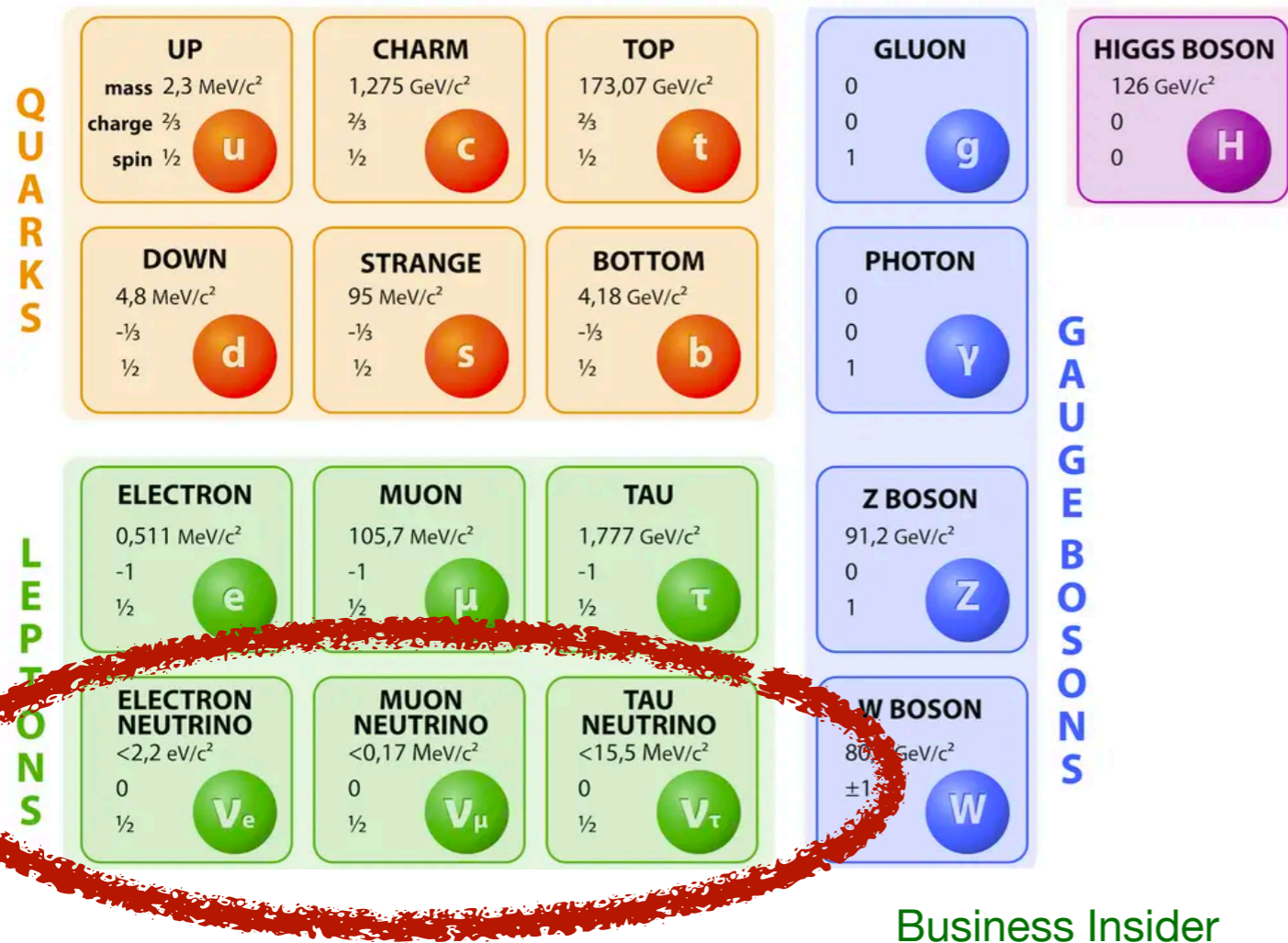


Business Insider

Major unanswered questions:

- Why are neutrinos massive?
- What composes the 95% of the energy budget of the Universe?
- Why is our Universe matter-antimatter asymmetric?

The Standard Model of Particle Physics



Major unanswered questions:

- Why are neutrinos massive?
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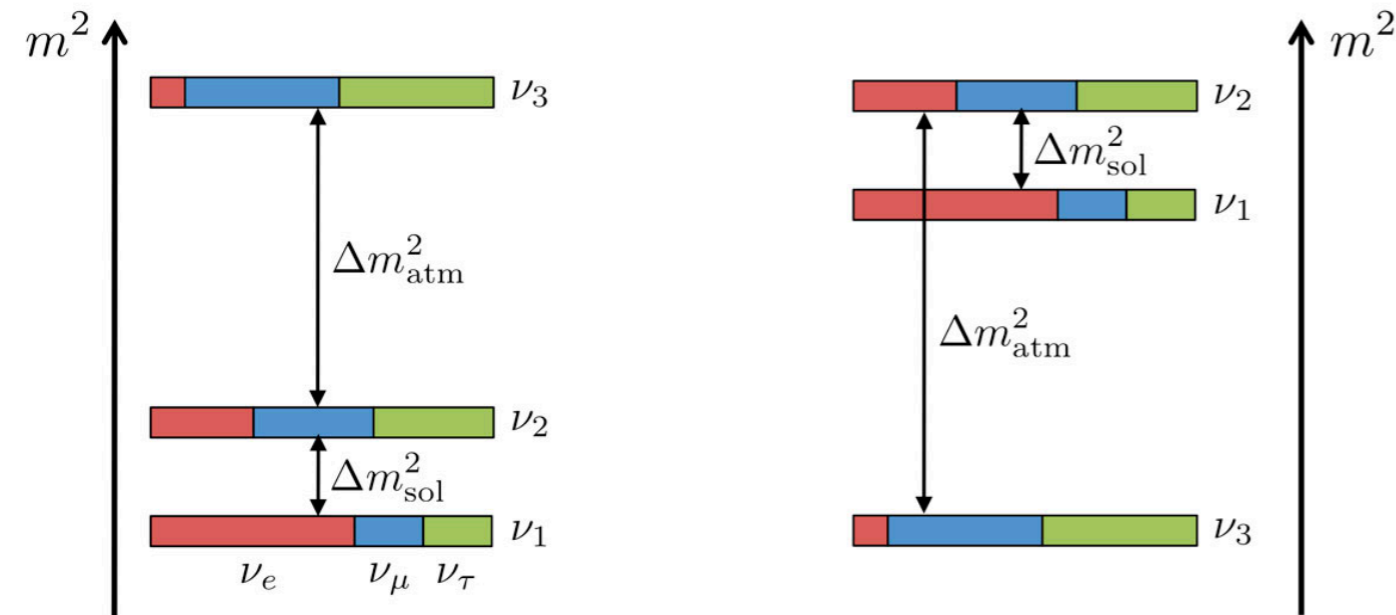
What we know so far...

Credit: The Particle Zoo

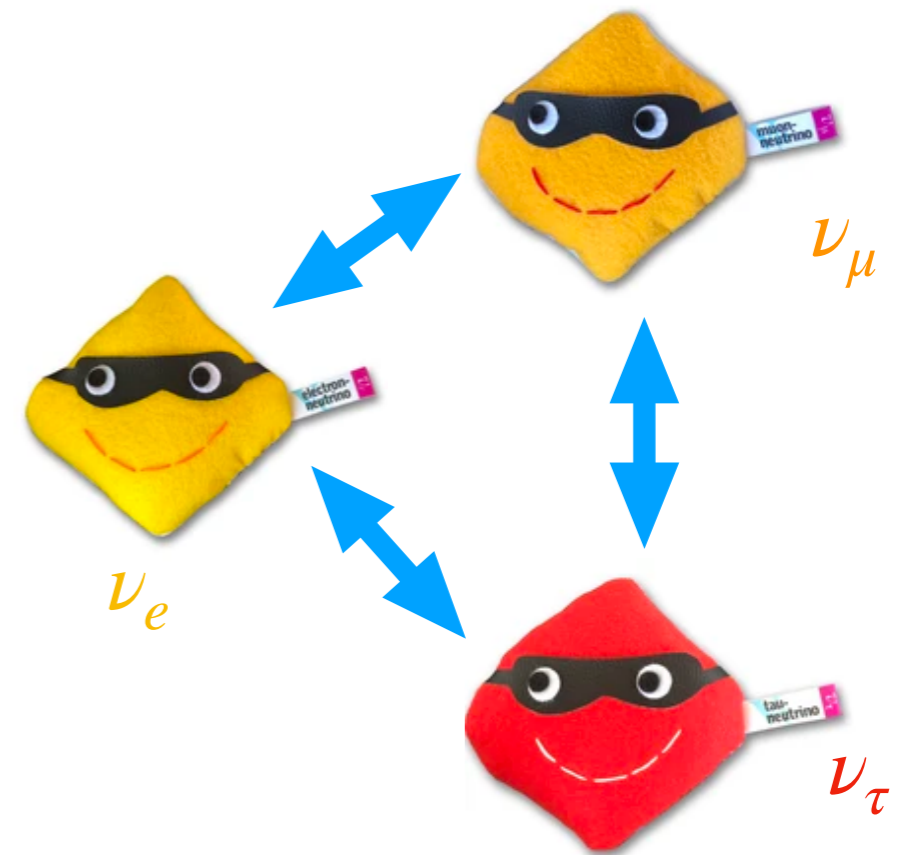
- Neutrinos are massless within the SM.
- Nature wants neutrinos to be massive.

normal hierarchy (NH)

inverted hierarchy (IH)



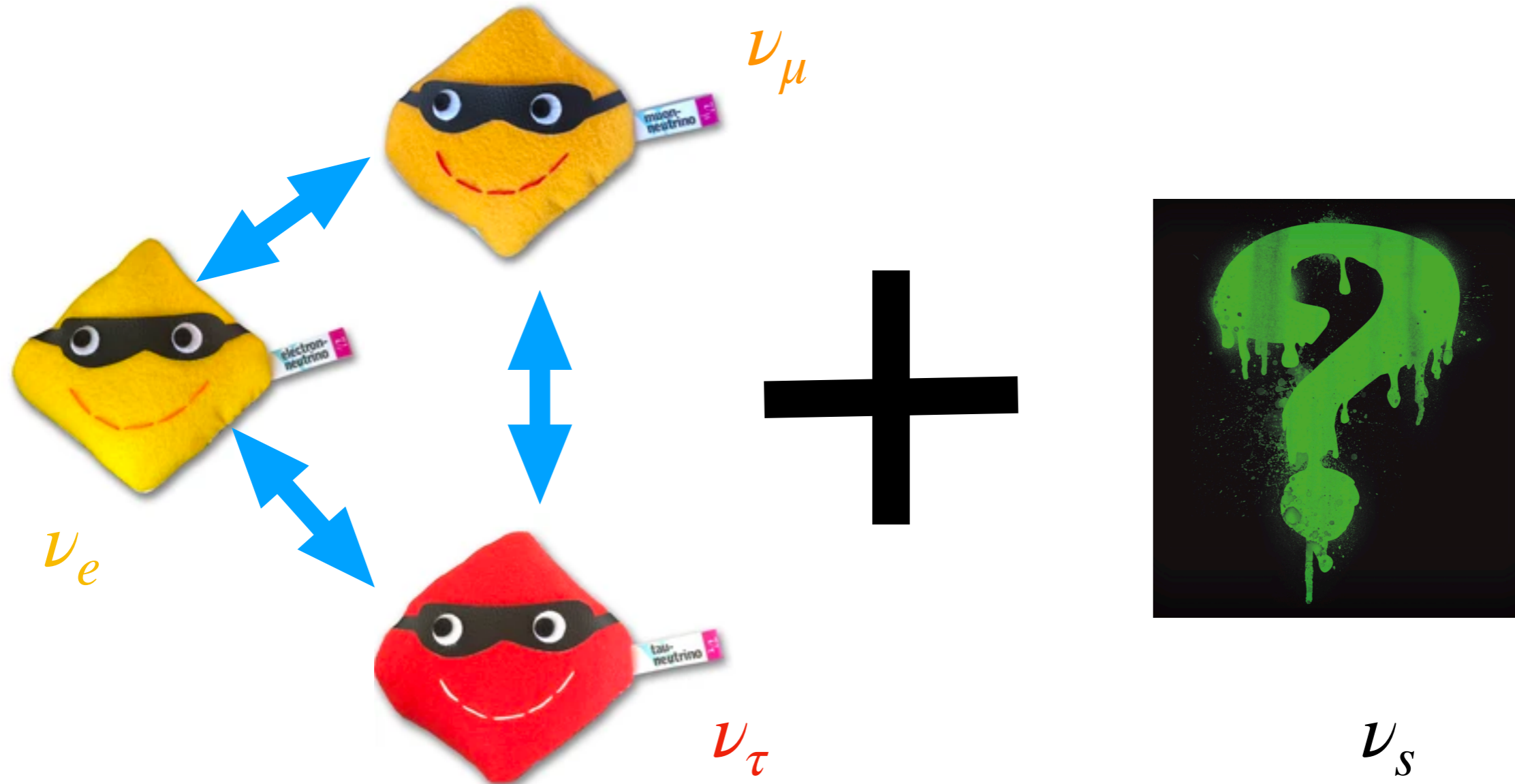
Mass ordering yet unknown



- Neutrinos interact “weakly” with the rest, as well as with themselves.
- There are 3 active light neutrinos, and can change flavors.

The sterile neutrino - the Riddler

Can there be more neutrinos?



Are there more of these ?

Three directions:

1. Neutrino mass.
2. Short baseline anomalies. (eV masses)
3. Cosmology. (mostly keV onwards)

Why do we like sterile neutrinos?

- Sterile neutrinos by definition have no gauge interactions within the SM.
- Provides the SM neutrinos with the 'right' partner.
- Can give masses to neutrinos.
- Can be used to answer the baryon-asymmetry of the universe through leptogenesis.
- **Possible dark matter candidate.** Can also be used to solve small-scale structure problems.
- Hints in terrestrial experiments?



See Abazajian (2017), Dasgupta and Kopp (2021) for a detailed review

Sterile neutrinos as Dark Matter

- Extra keV mass eigenstate $\nu_4 = \cos \theta \nu_s + \sin \theta \nu_a$
- Can be detected through 1-loop decay into photons: $\nu_s \rightarrow \nu_a \gamma$.

- Decay rate $\Gamma \propto m_4^5 \sin^2 2\theta = 10^{-27} \left(\frac{\theta^2}{10^{-5}} \right) \left(\frac{m_4}{1 \text{ keV}} \right)^5 \text{ s}^{-1}$.

Radiative decay detectable.

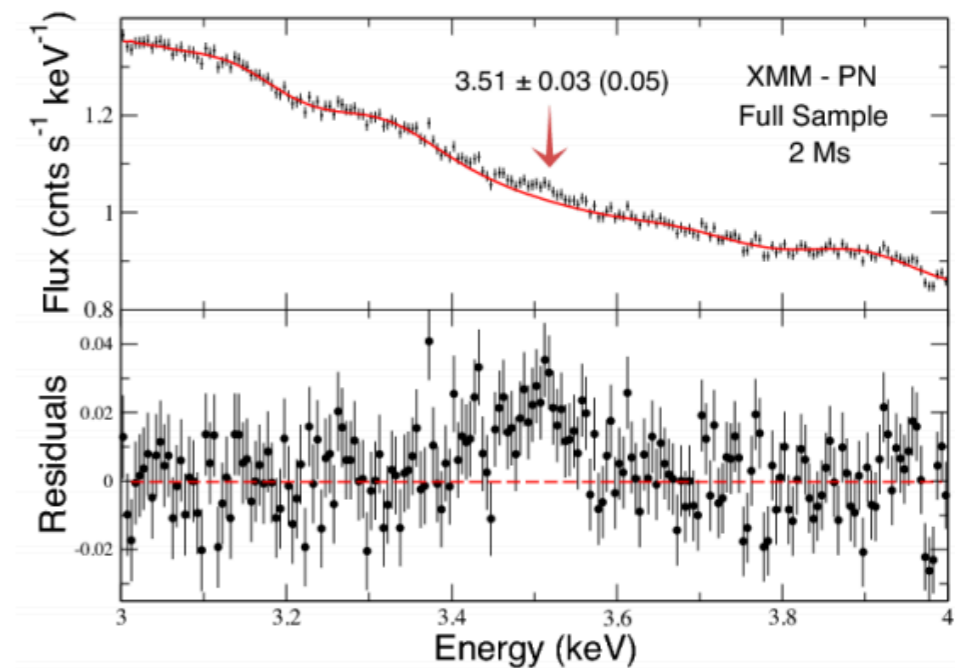
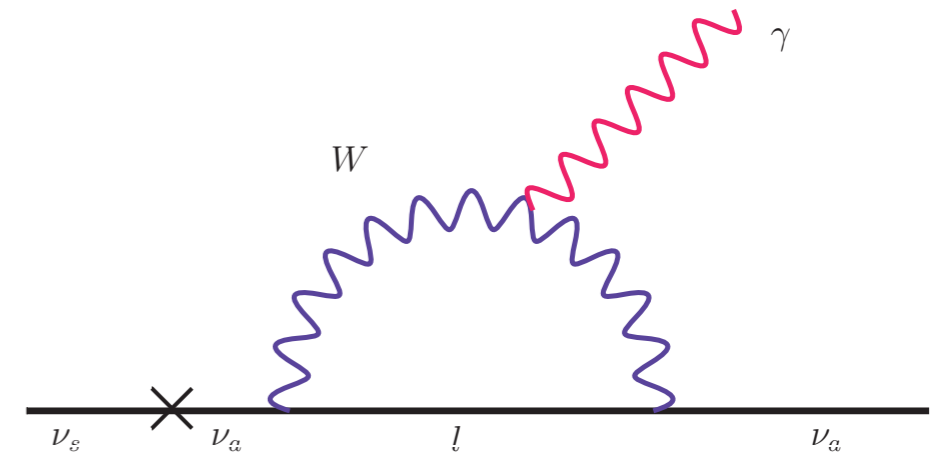
Zatsepin and Smirnov, *Yad. Fiz.* 1978, Pal and Wolfenstein, *PRD*1982
 Abazajian, Fuller and Patel, *PRD*2001 + many more...

- Non-observation puts bound on $m_4 - \sin 2\theta$ plane.
- Radiative decay leads to line at $E_\gamma = m_4/2$.

Hints of a line at $E = 3.55 \text{ keV}$? Sterile neutrino at 7.1 keV ?

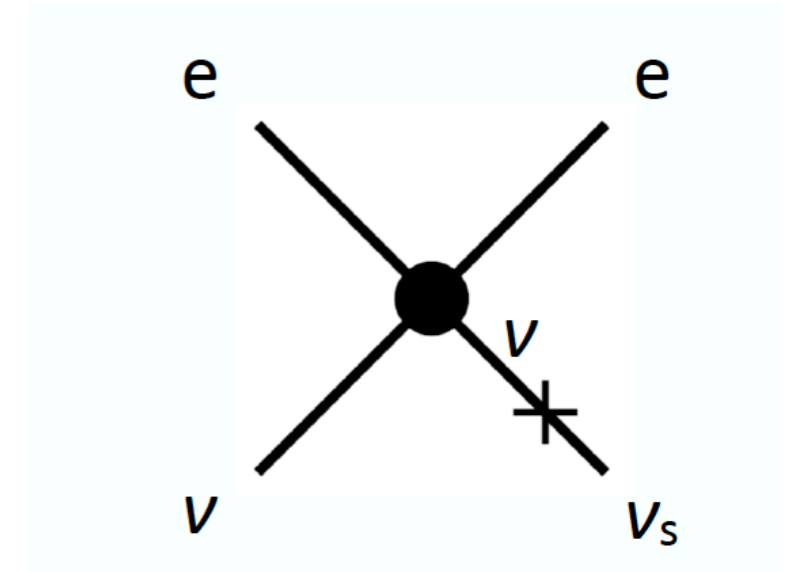
Bulbul et al. *Astro.* 2014, Boyarski et al., *PRL* 2014.
 See a contrary report by Dessert et. al. (*Science*, 2020).
 Comments on that followed at Boyarski et. al.2004.06601, and Abazajian, 2004.06170.

- But how do we produce these neutrinos?

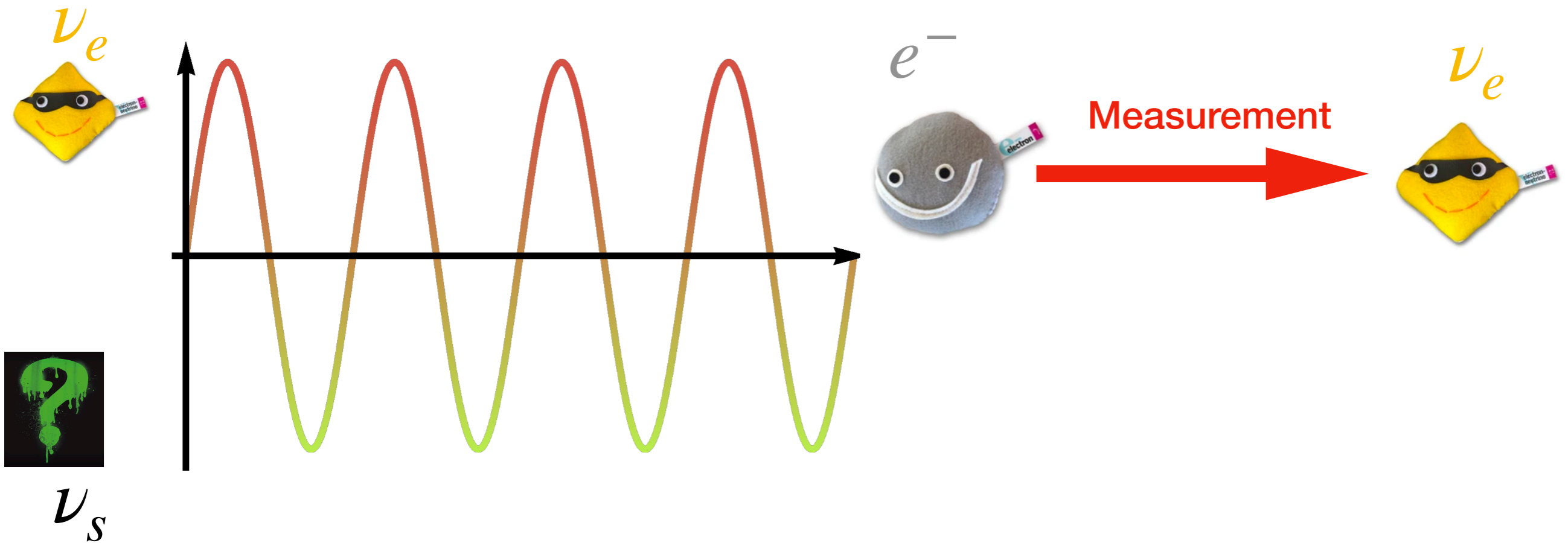


Production: the Dodelson-Widrow mechanism

- The ν_s cannot be in thermal equilibrium with SM particles before BBN.
- Must be produced non-thermally with $\theta \ll 1$.
- ν_a oscillates into ν_s before decoupling. Creates a non-thermal population of ν_s .



Dodelson and Widrow, PRL1994.



Production: the Dodelson-Widrow mechanism

ν_a oscillates into ν_s before decoupling.

Creates a non-thermal population of ν_s . Dodelson and Widrow, PRL1994

$$T \frac{\partial}{\partial T} f_{\nu_s} \Big|_{p/T} = \frac{\Gamma_a}{2H} \langle P(\nu_a \rightarrow \nu_s) \rangle f_{\nu_a} ,$$

$$\langle P(\nu_a \rightarrow \nu_s) \rangle = \frac{1}{2} \frac{\Delta^2 \sin^2 2\theta}{\Delta^2 \sin^2 2\theta + \frac{\Gamma_a^2}{4} + (\Delta \cos 2\theta - V)^2}$$

Averaged over
one mean free path

↑

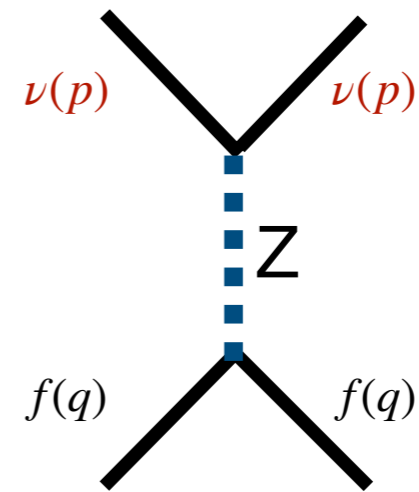
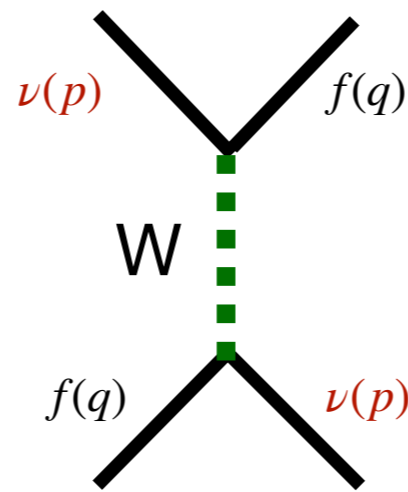
$$\Delta = m_s^2 / 2E$$

↑
Damping

↑
Matter potential
 $V = V_T + V_D$

Finite temperature: $V_T \propto T$

Finite density: $V_D \propto n_f$



Analyzing the Dodelson-Widrow mechanism

$$T \frac{\partial}{\partial T} f_{\nu_s} \Big|_{p/T} = \frac{\Gamma_a}{2H} \langle P(\nu_a \rightarrow \nu_s) \rangle f_{\nu_a},$$

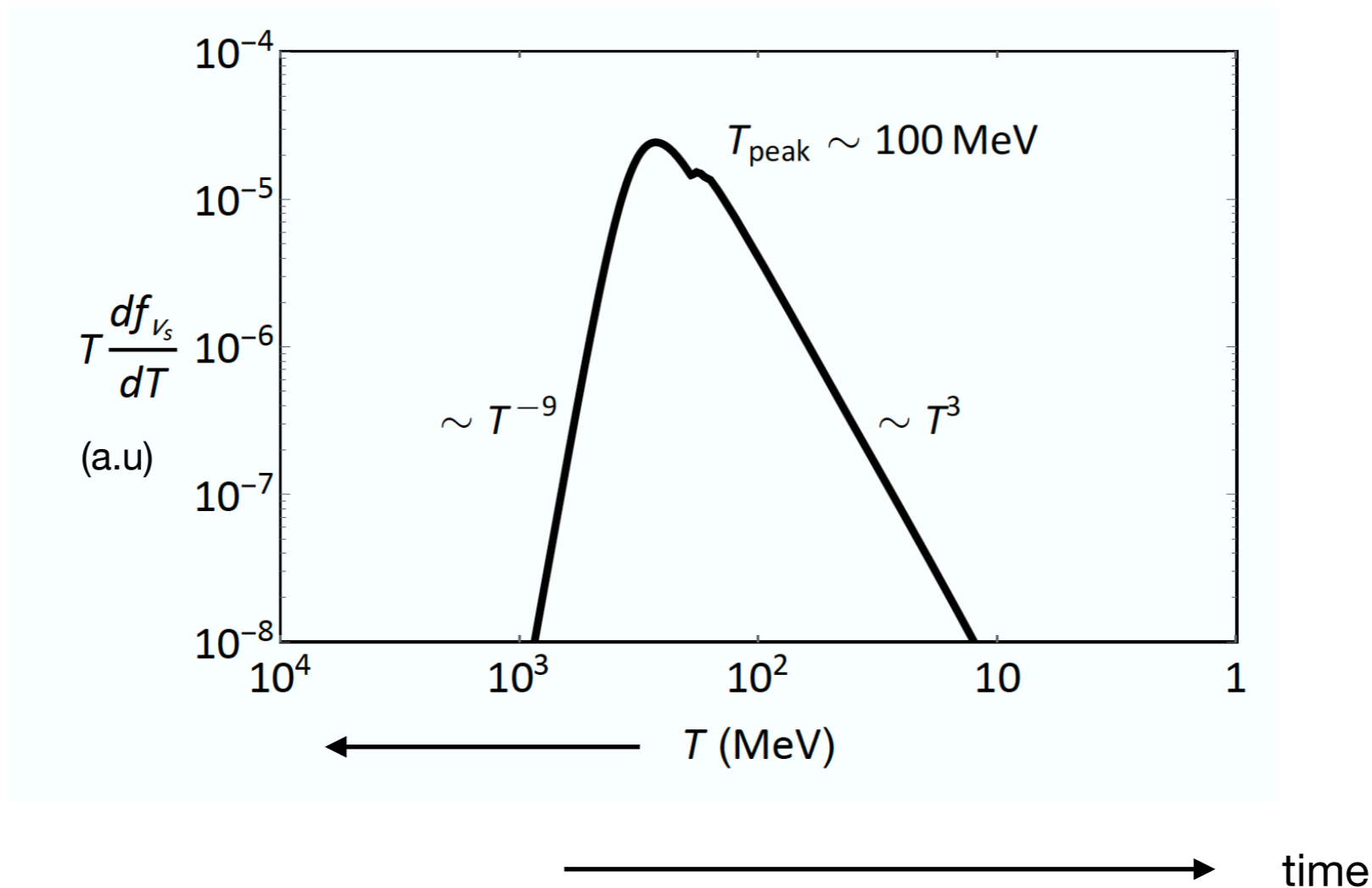
$$\langle P(\nu_a \rightarrow \nu_s) \rangle = \frac{1}{2} \frac{\Delta^2 \sin^2 2\theta}{\Delta^2 \sin^2 2\theta + \frac{\Gamma_a^2}{4} + (\Delta \cos 2\theta - V)^2}$$

SM

$$\begin{aligned} V^{W,Z} &\sim T^5 \\ \Gamma_a &\sim T^5 \\ \Delta &\sim T^{-1} \end{aligned}$$

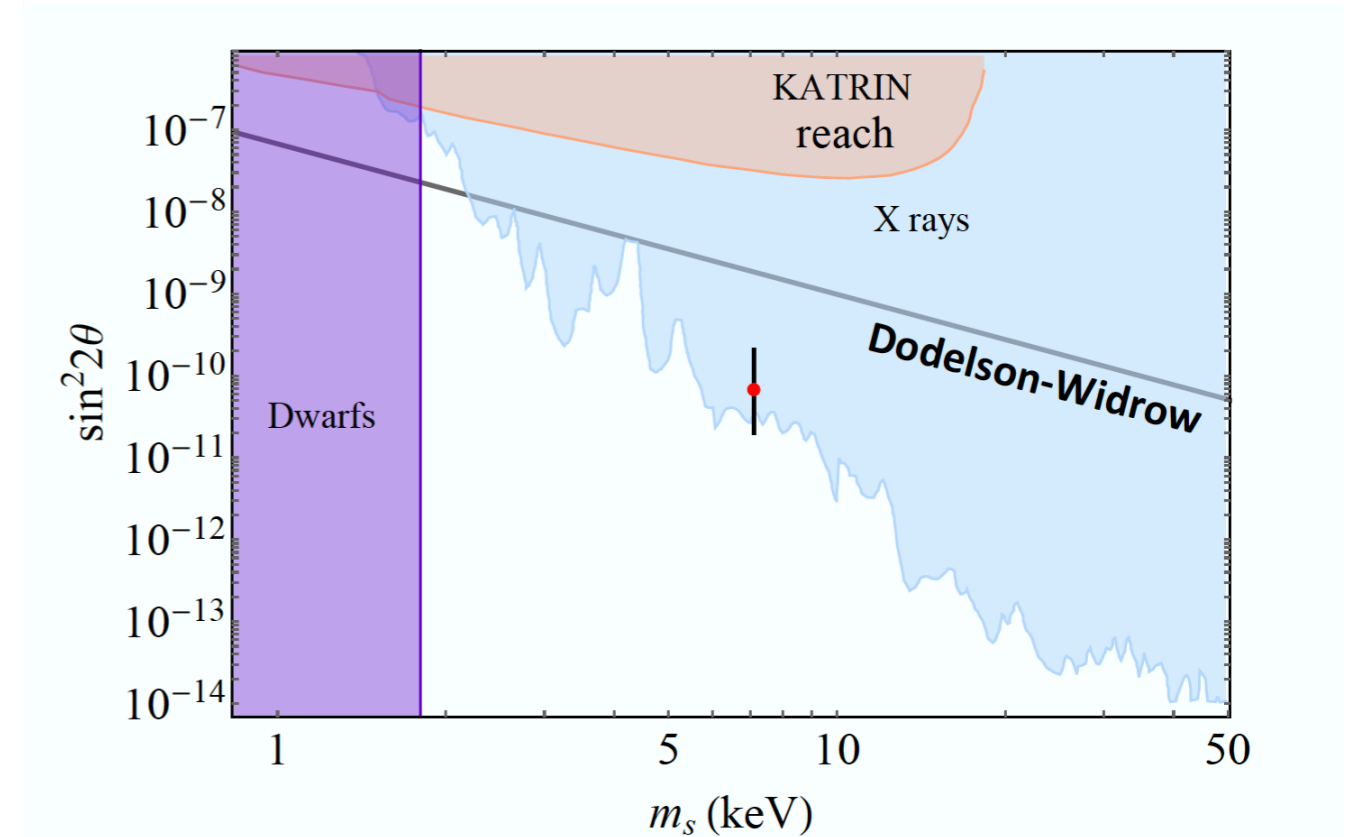
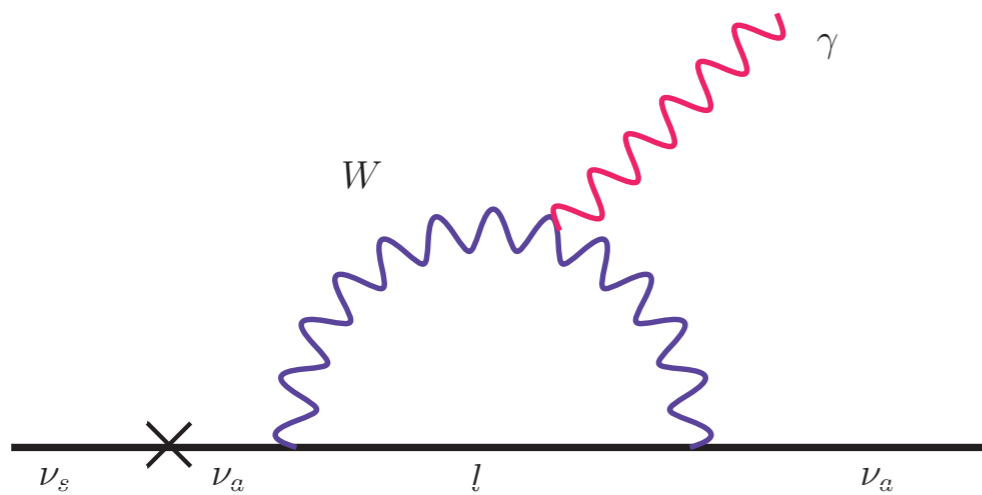
- Case 1: When $\Gamma \gg \Delta$, $T \frac{df}{dT} \sim \frac{\Gamma}{H} \frac{\Delta^2}{\Gamma^2} \propto T^{-9}$
- Case 2: When $\Gamma \ll \Delta$, $T \frac{df}{dT} \sim \frac{\Gamma}{H} \propto T^3$

The Dodelson-Widrow mechanism... contd



- ν_s freeze in. Production is maximized at $T \sim 100$ MeV.
- Can satisfy relic density of DM. But as with all theories, this is too good to be allowed...

The Dodelson-Widrow mechanism...constrained



- Ruled out by X-ray bounds and phase-space considerations (Tremaine-Gunn, galaxy counts, Lyman alpha, strong lensing, etc.).
- A finite lepton asymmetry (Shi-Fuller Mechanism) can help. Required lepton asymmetry difficult to constrain. [Shi and Fuller, PRL 1999](#), [Fuller, Abazajian and Patel PRD 2001](#)
- Can we open up parameter space without introducing a lepton asymmetry?



**Secret neutrino
self-interactions**

Secret neutrino self-interactions

- Active neutrino secret self-interactions. Can be much stronger than ordinary weak interactions.

- Model building aspect?

Consider

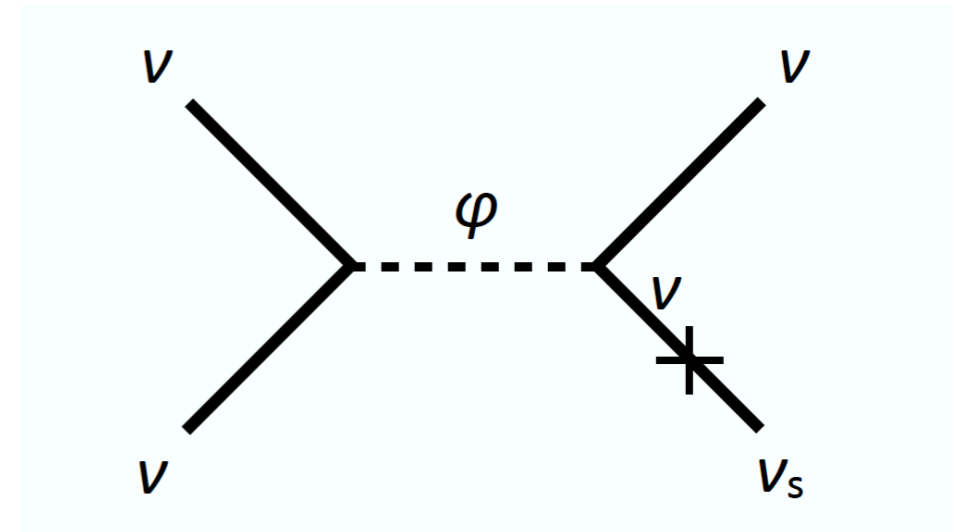
$$\mathcal{L}_\nu = \frac{y}{\Lambda^2} (LH)^2 \varphi^* \xrightarrow{\text{EWSB}} \lambda_\varphi \nu_a \nu_a \varphi^*$$

φ has lepton number.

- Relic \sim (rate) \times (mixing angle).

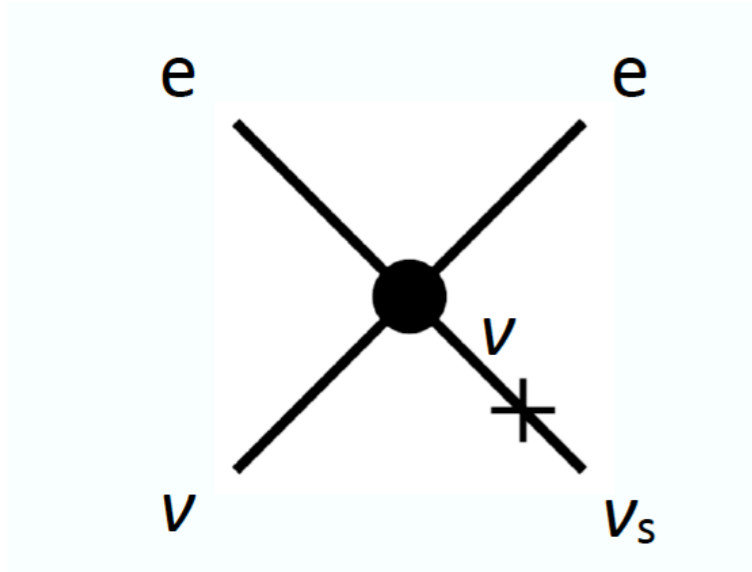
$$T \frac{\partial}{\partial T} f_{\nu_s} \Big|_{p/T} = \frac{\Gamma_a}{2H} \langle P(\nu_a \rightarrow \nu_s) \rangle f_{\nu_a}$$

Increasing rate can satisfy same results for smaller θ . This allows us to shift the DW line below X-ray bounds.



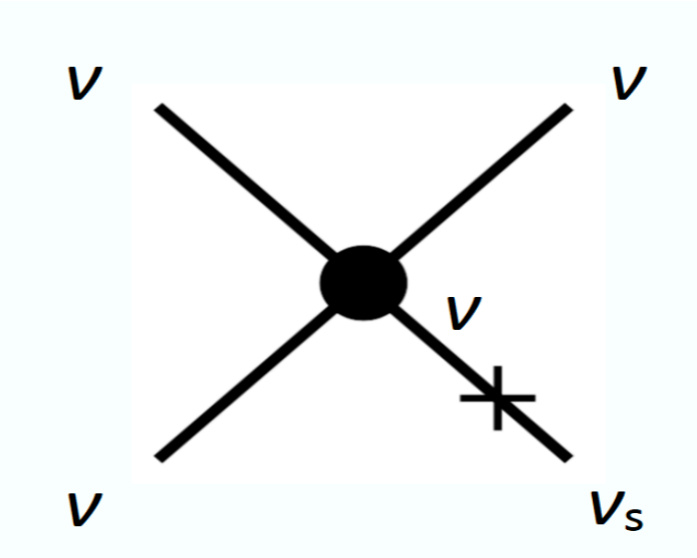
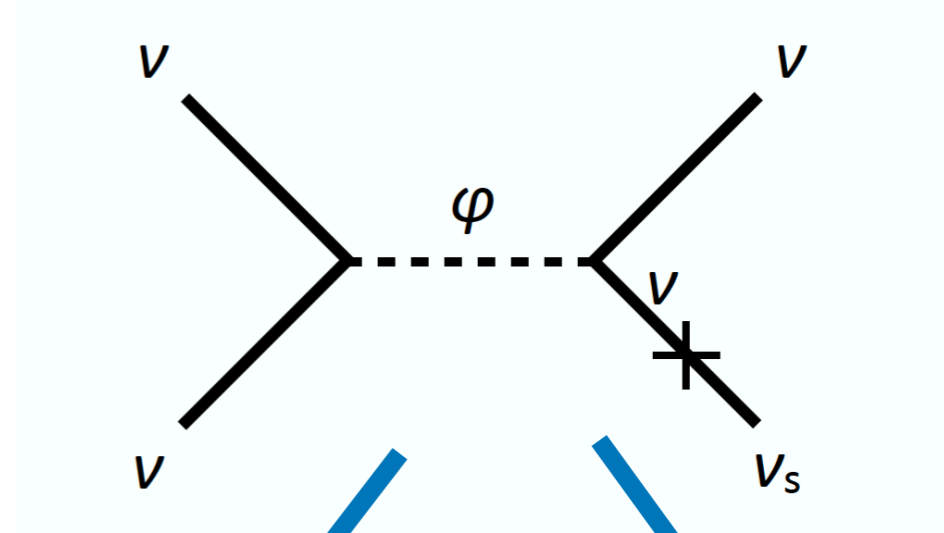
What changes in the DW mechanism?

S.M

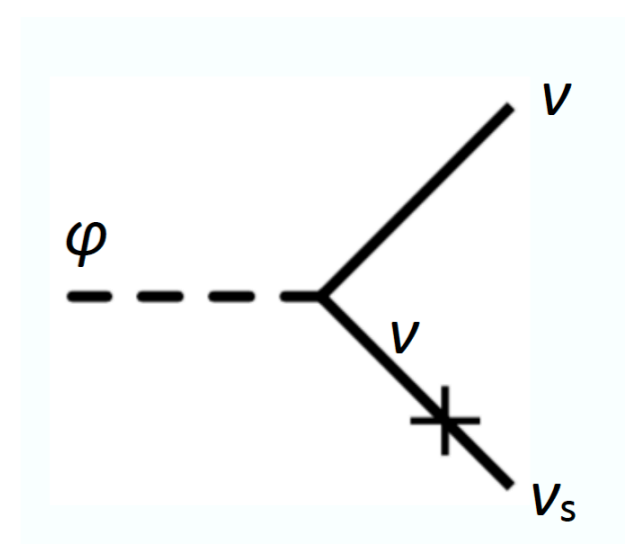


$$M_{W,Z} \geq T_{peak}$$

S.M + Self-Interactions



$$M_{\phi} > T_{peak}$$



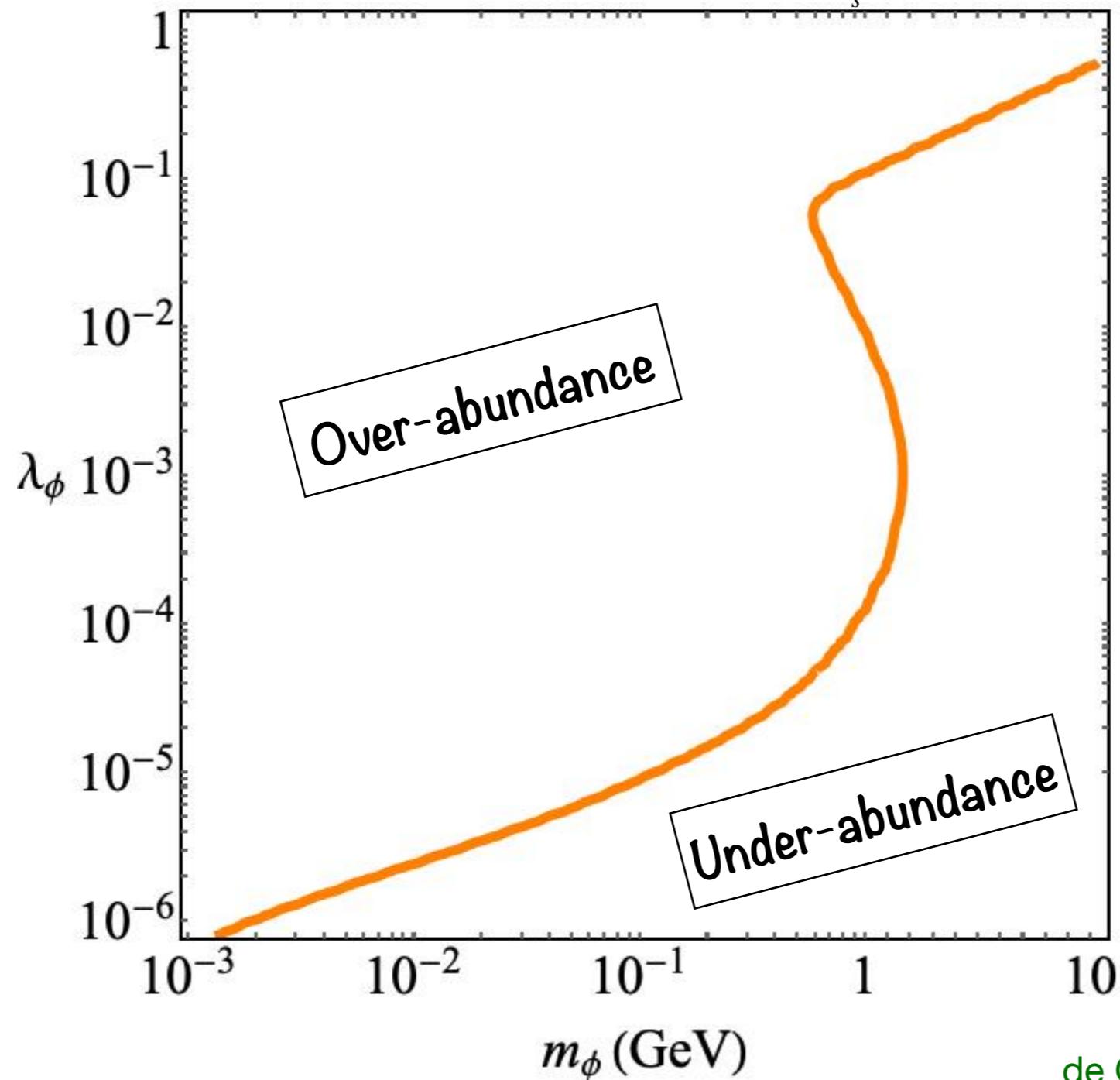
$$M_{\phi} \lesssim T_{peak}$$

$$m_\phi > \text{MeV}$$

Numerical estimates

$$T \frac{\partial}{\partial T} f_{\nu_s} \Big|_{p/T} = \frac{\Gamma_a}{4H} \frac{\Delta^2 \sin^2 2\theta}{\Delta^2 \sin^2 2\theta + \frac{\Gamma_a^2}{4} + (\Delta \cos 2\theta - V)^2} f_{\nu_a}$$

$$\Omega h^2 = 0.12, m_{\nu_s} = 7.1 \text{ keV}, \sin^2 2\theta = 7 \times 10^{-11}$$



Not a monotonic dependence!
Why?

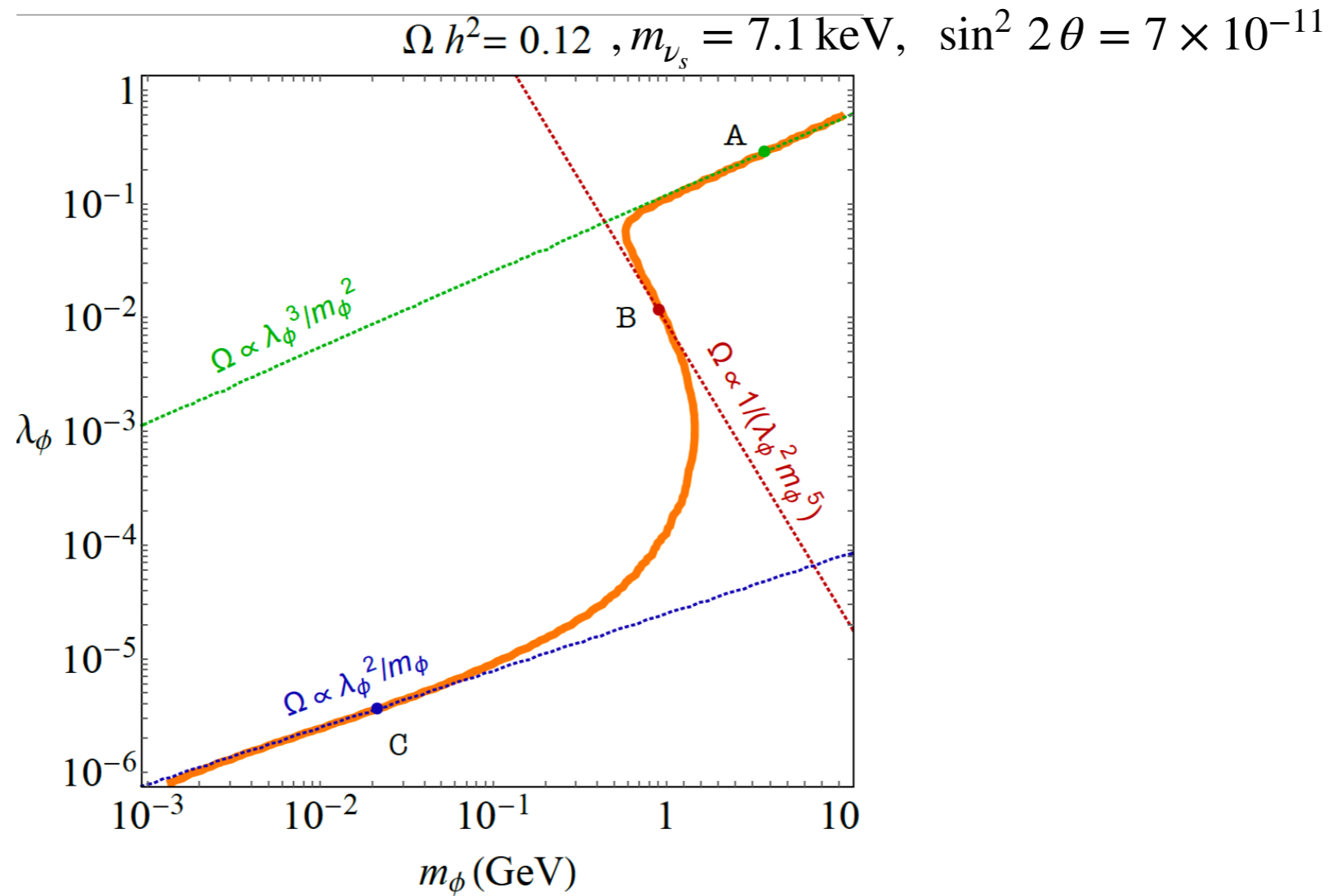
Numerical and analytical estimates

$$T \frac{\partial}{\partial T} f_{\nu_s} \Big|_{p/T} = \frac{\Gamma_a}{2H} \frac{1}{2} \frac{\Delta^2 \sin^2 2\theta}{\Delta^2 \sin^2 2\theta + \frac{\Gamma_a^2}{4} + (\Delta \cos 2\theta - V)^2} f_{\nu_a}$$

● Two scales in problem:

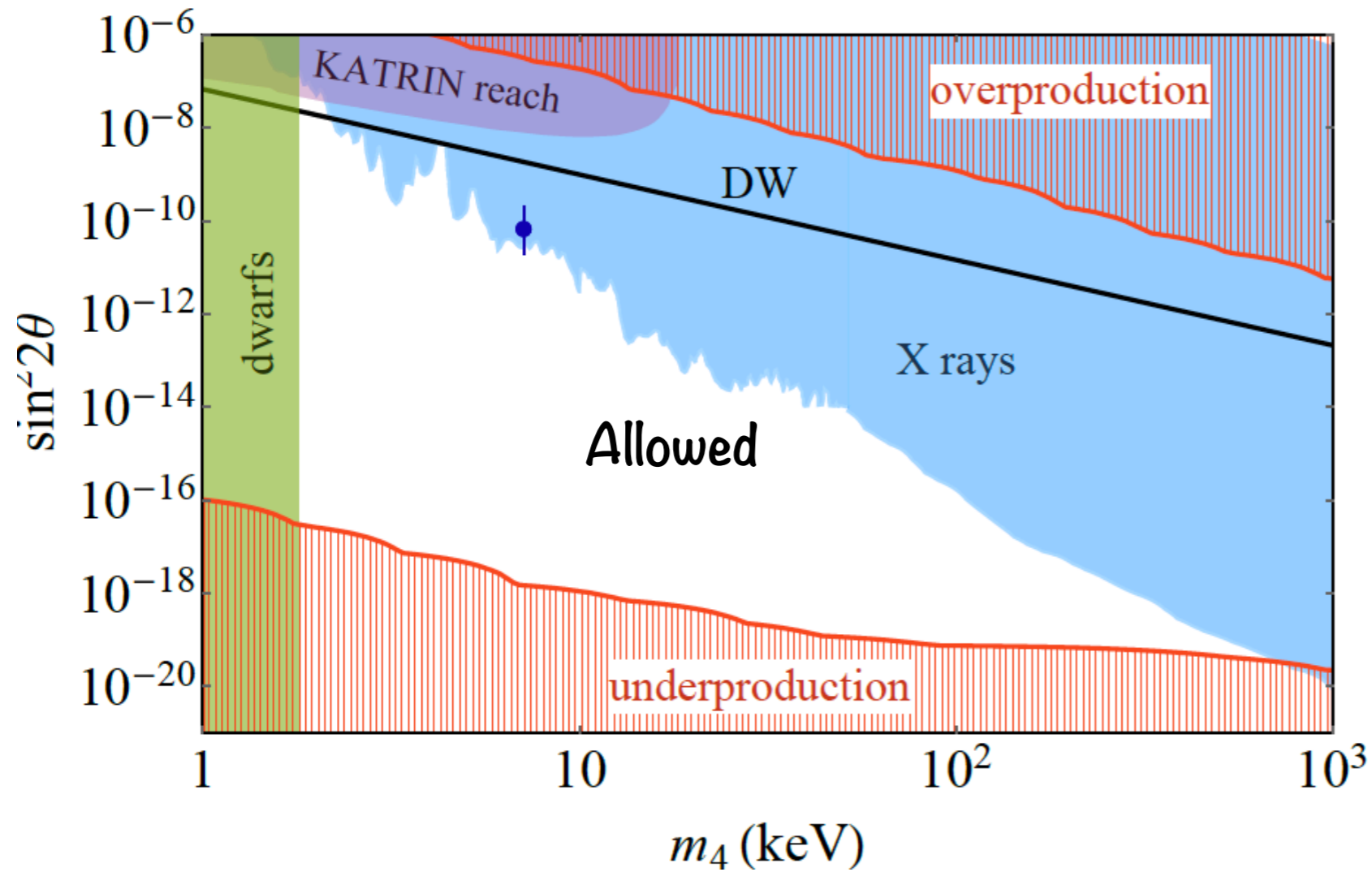
1. $t_{\Gamma=H}$: When $\Gamma/H = 1$, to determine when interactions are in equilibrium.
2. $t_{\Delta=V}$: When $|\Delta| \sim |V|$, mixing angle is not suppressed.
3. t_φ : When $T = m_\varphi$, mediator cannot be produced on-shell for lower temperature

Explanation of Results

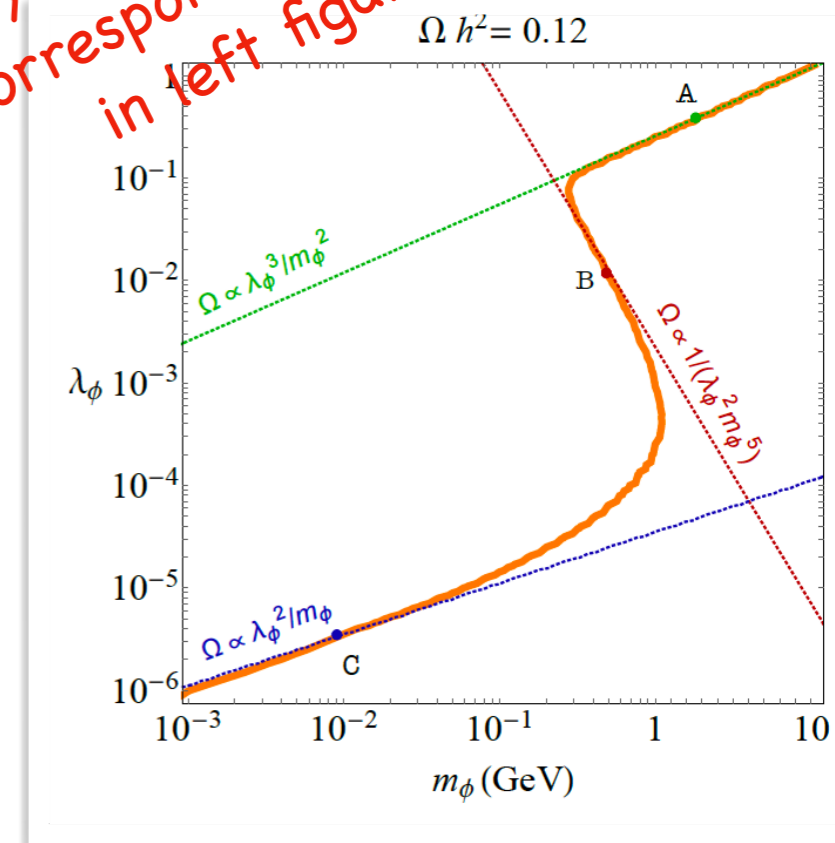


1. **A:** $t_\phi < t_{\Delta=V} < t_{\Gamma=H}$. Production around $t_{\Delta=V}$ from scattering via an off-shell ϕ . Similar to the usual DW mech.
2. **B:** Intermediate mass, coupling: $t_\phi < t_{\Gamma=H} < t_{\Delta=V}$. Peak production happens in $(t_\phi < t < t_{\Gamma=H})$ when θ_{eff} is suppressed.
3. **C:** $t_{\Delta=V} < t_\phi < t_{\Gamma=H}$. DM produced most efficiently through on-shell ϕ exchange $(t_{\Delta=V} < t < t_\phi)$

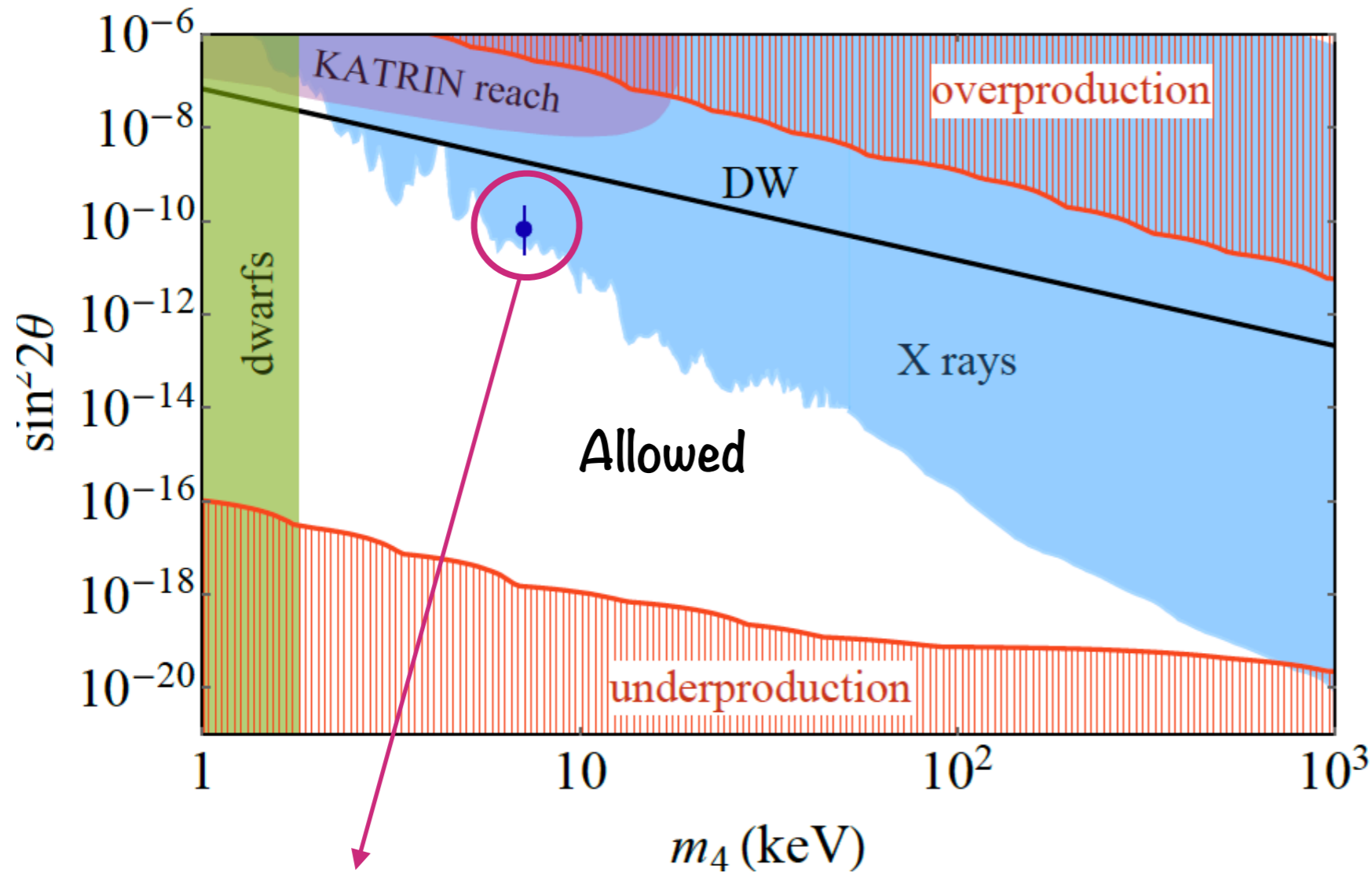
Allowed Relic Density window



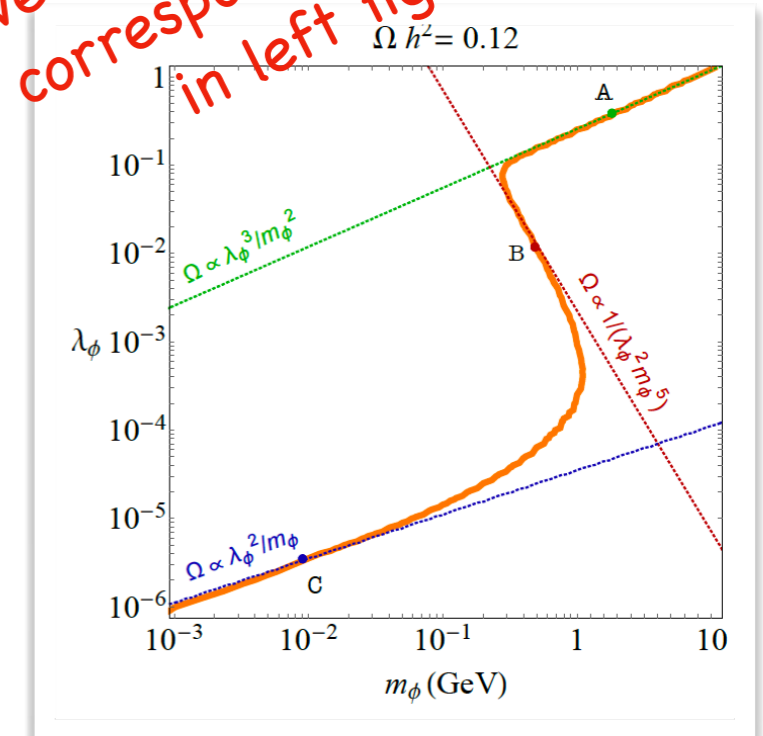
Every point in this plane corresponds to a line in left figure



Allowed Relic Density window



Every point in this plane corresponds to a point in left figure

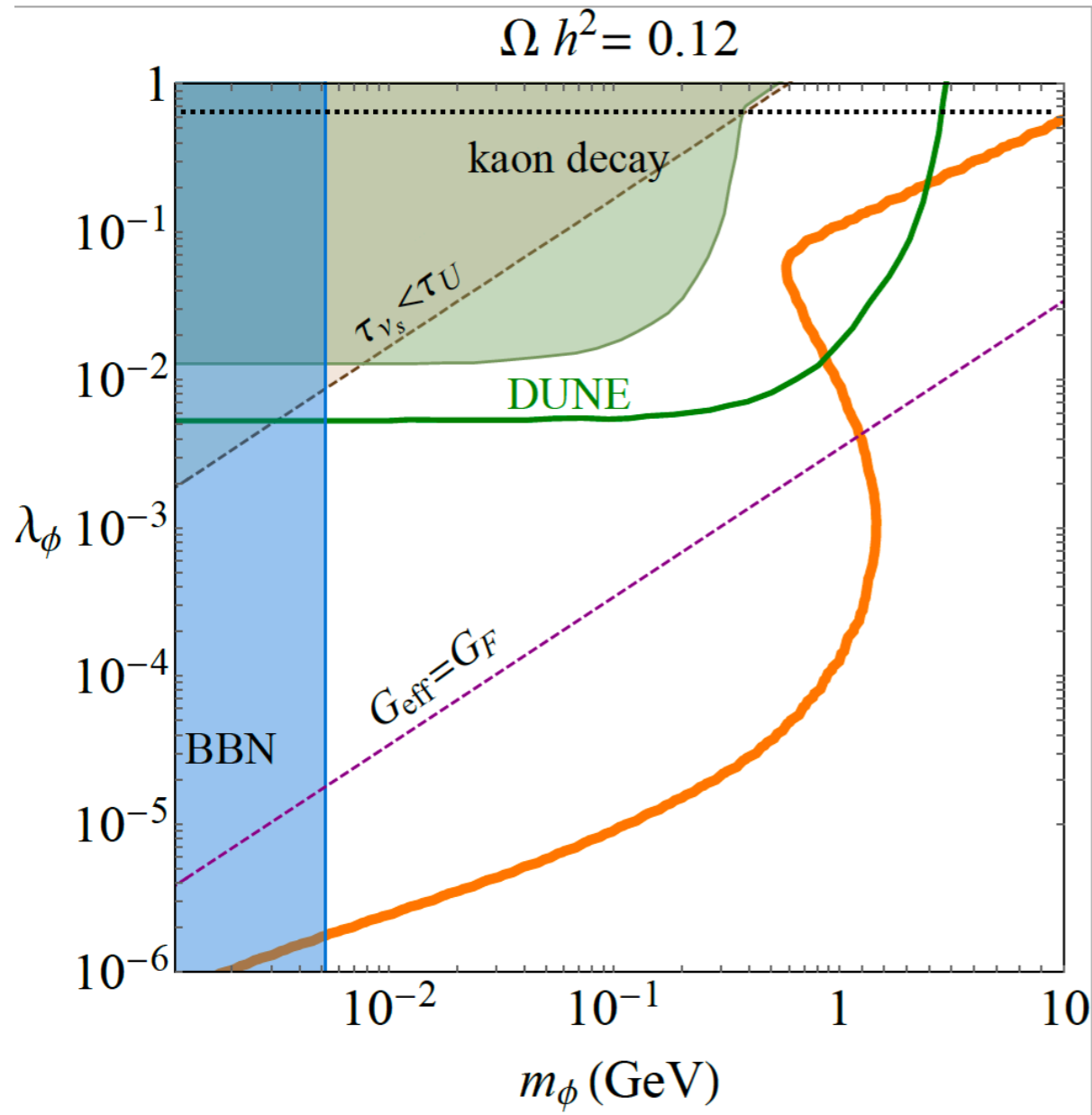


Can be used to satisfy the 3.5 keV X-ray line also ~
 $m_{\nu_s} = 7.1 \text{ keV}, \sin^2 2\theta = 7 \times 10^{-11}$ Bulbul et al. Astro. 2014+many more

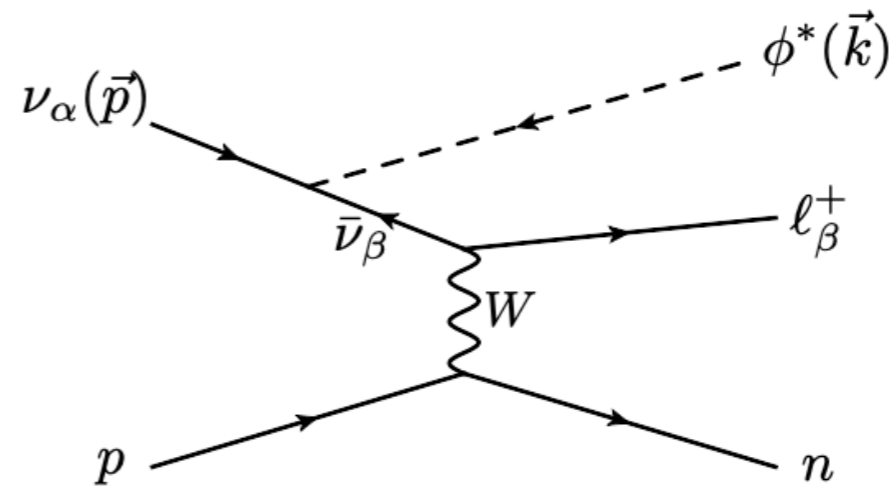
Experimental tests

Lab based tests

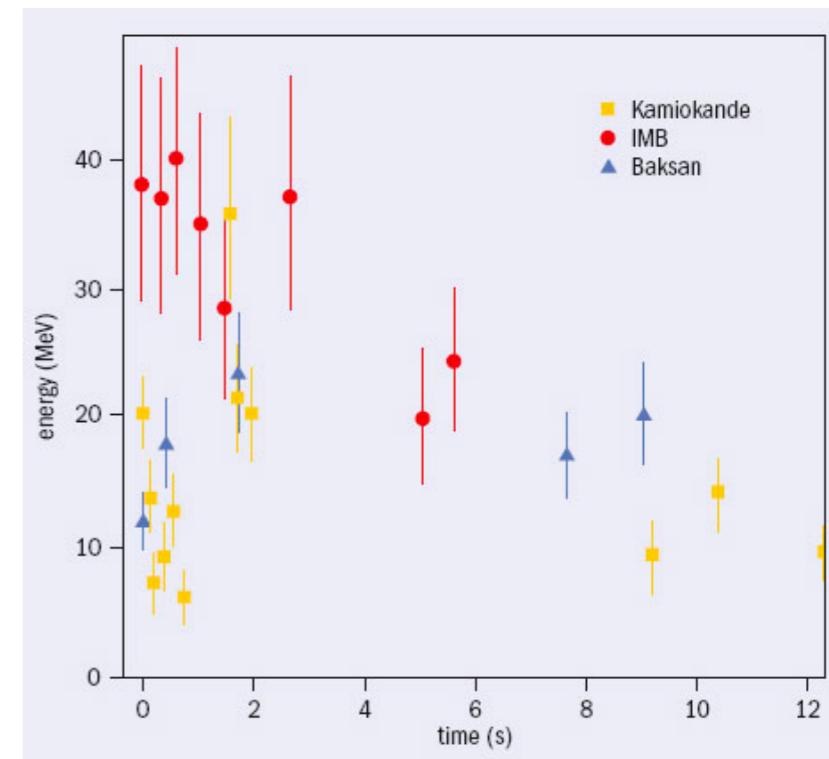
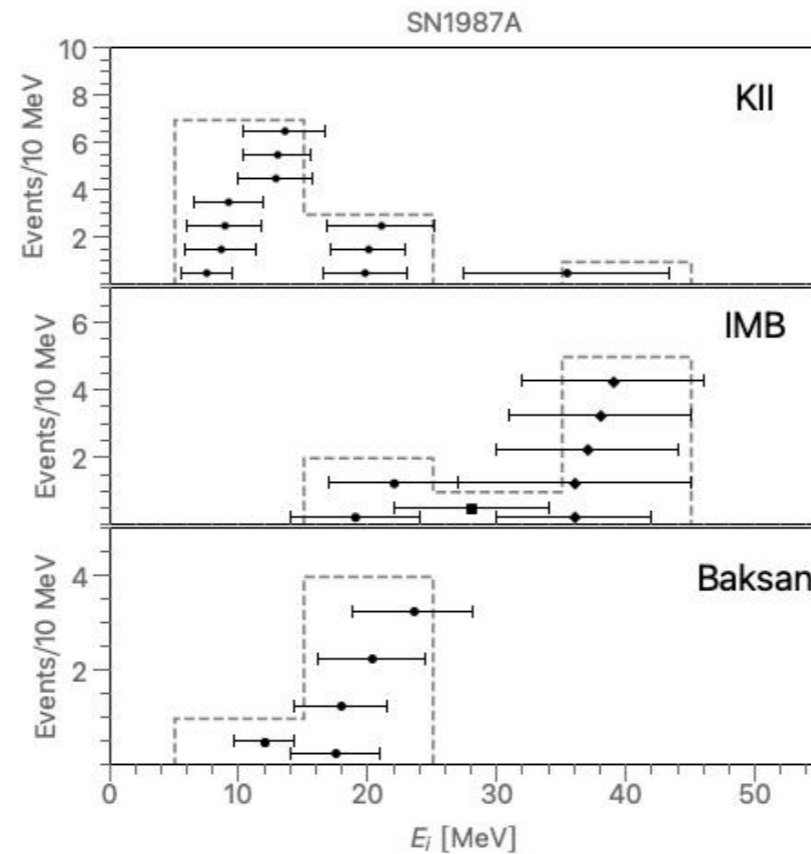
The vertex: $\mathcal{L} = \nu_a \nu_a \varphi$



- Invisible Higgs decays, Z decays
- $K^- \rightarrow \mu^- \nu_\mu \varphi$, $\varphi \rightarrow \nu\nu$.
Bounds from $\text{Br}(K^- \rightarrow \mu^- 3\nu) < 10^{-6}$.
- Look for "wrong sign muon" in $\nu_\mu N \rightarrow \mu^+ N' \varphi$.
Parameter space can also be probed through missing energy.

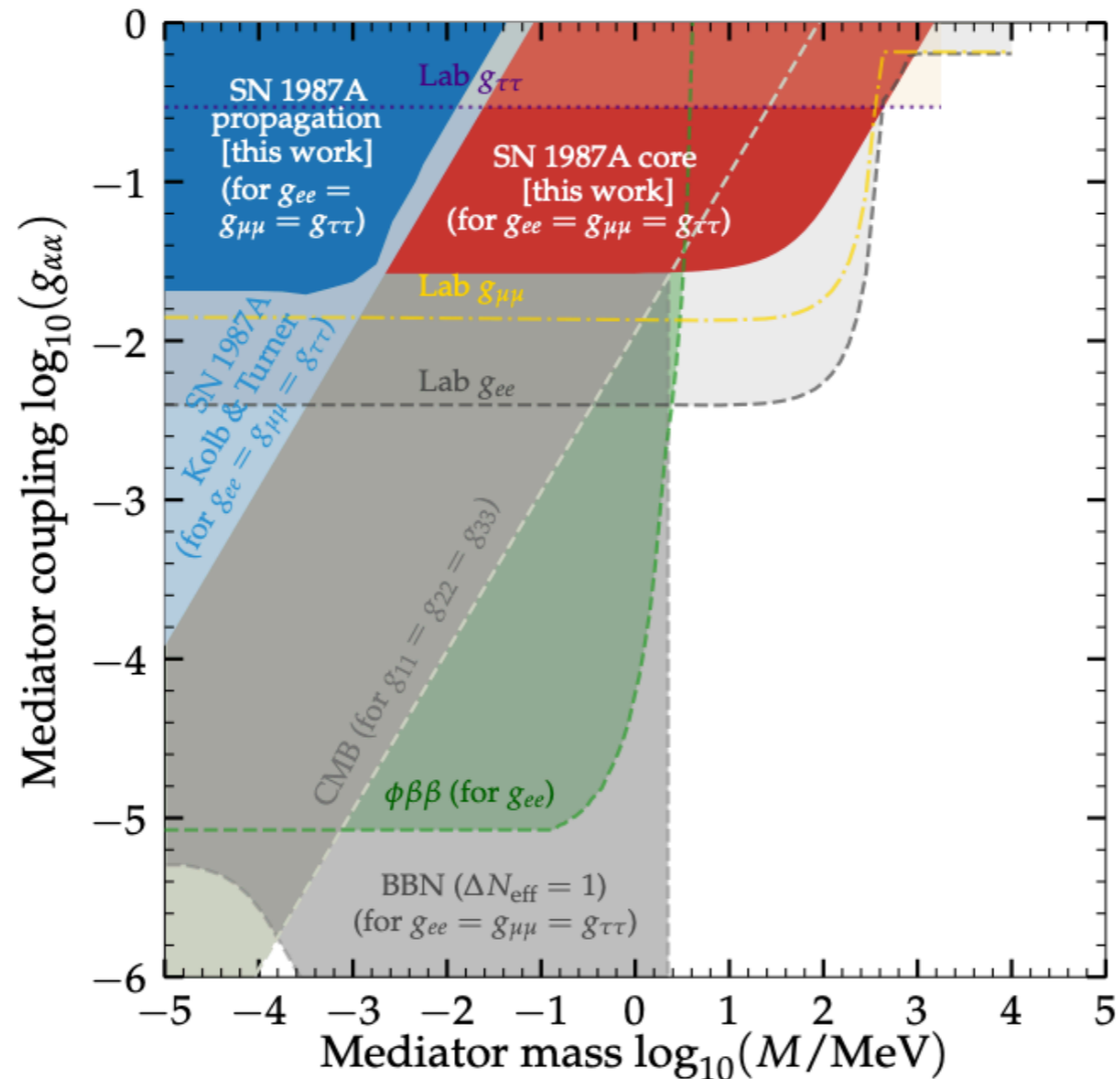


Astro tests: supernova cooling bounds



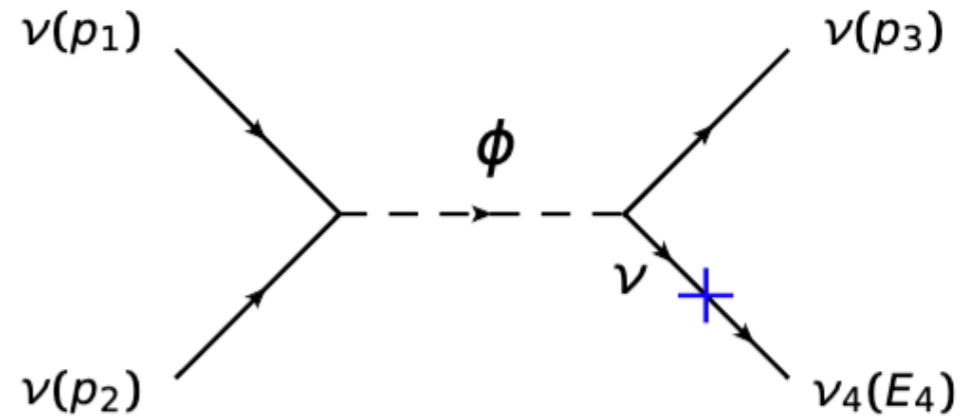
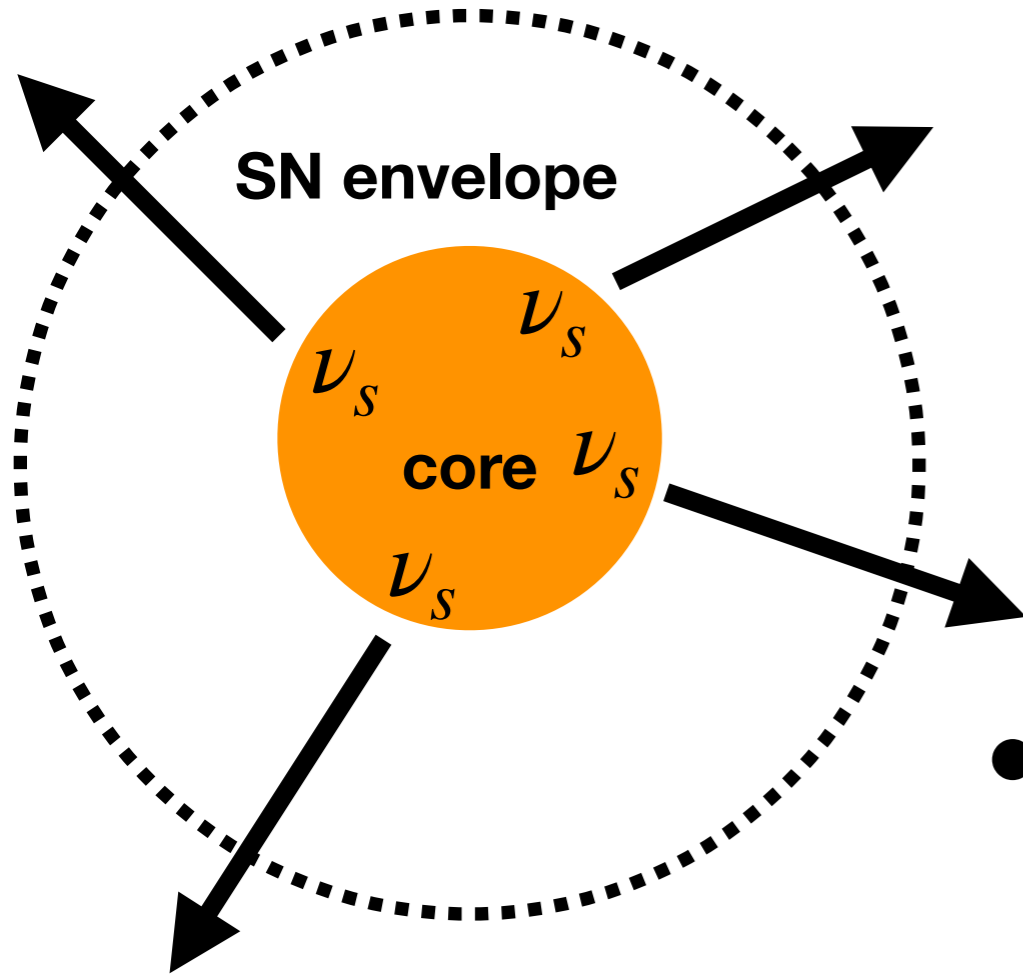
- Around 30 neutrinos of energy $\mathcal{O}(10)$ MeV observed from SN1987A for a period of 10s or so.
- New modes of energy loss due to weakly coupled particles.
- If $\mathcal{L}_x > \mathcal{L}_\nu \sim 10^{52}$ erg/s, then duration of neutrino burst is reduced from 10s.
Raffelt criterion.
- Alternation of the neutrino events.

Astro tests: Core-Collapse supernova constraints



- Scatterings with the cosmic neutrino background could have down-scattered the neutrinos from SN1987A (blue shaded)
- Successful explosion could have been hindered (red shaded).
- Production of mediators, leading to cooling— less stringent bounds.

Astro tests: supernova cooling bounds

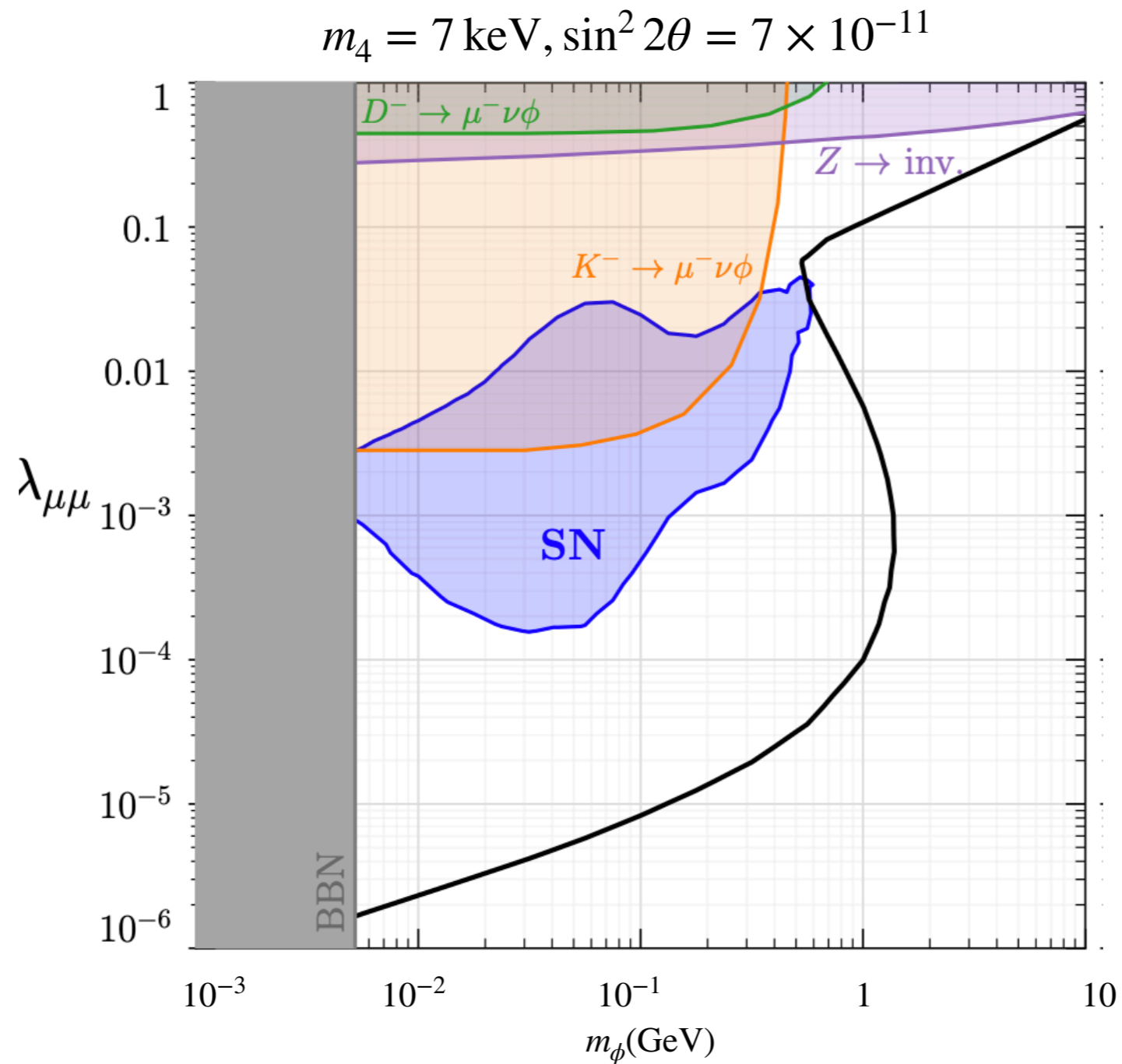


- ν_s can also be produced inside the SN core due to these new interactions, and lead to additional cooling channels.

$$L = \int d^3\vec{r} \int \frac{d^3\vec{p}_1}{(2\pi)^3} f_\nu(E_1, r) \int \frac{d^3\vec{p}_2}{(2\pi)^3} f_\nu(E_2, r) \frac{1}{4E_1 E_2} \int \frac{d^3\vec{p}_3}{(2\pi)^3 2E_3} \int \frac{d^3\vec{p}_4}{(2\pi)^3 2E_4} \times (2\pi)^4 \delta^4(\vec{p}_1 + \vec{p}_2 - \vec{p}_3 - \vec{p}_4) |\mathcal{M}|^2 E_4 e^{-\tau(E_4, r)},$$

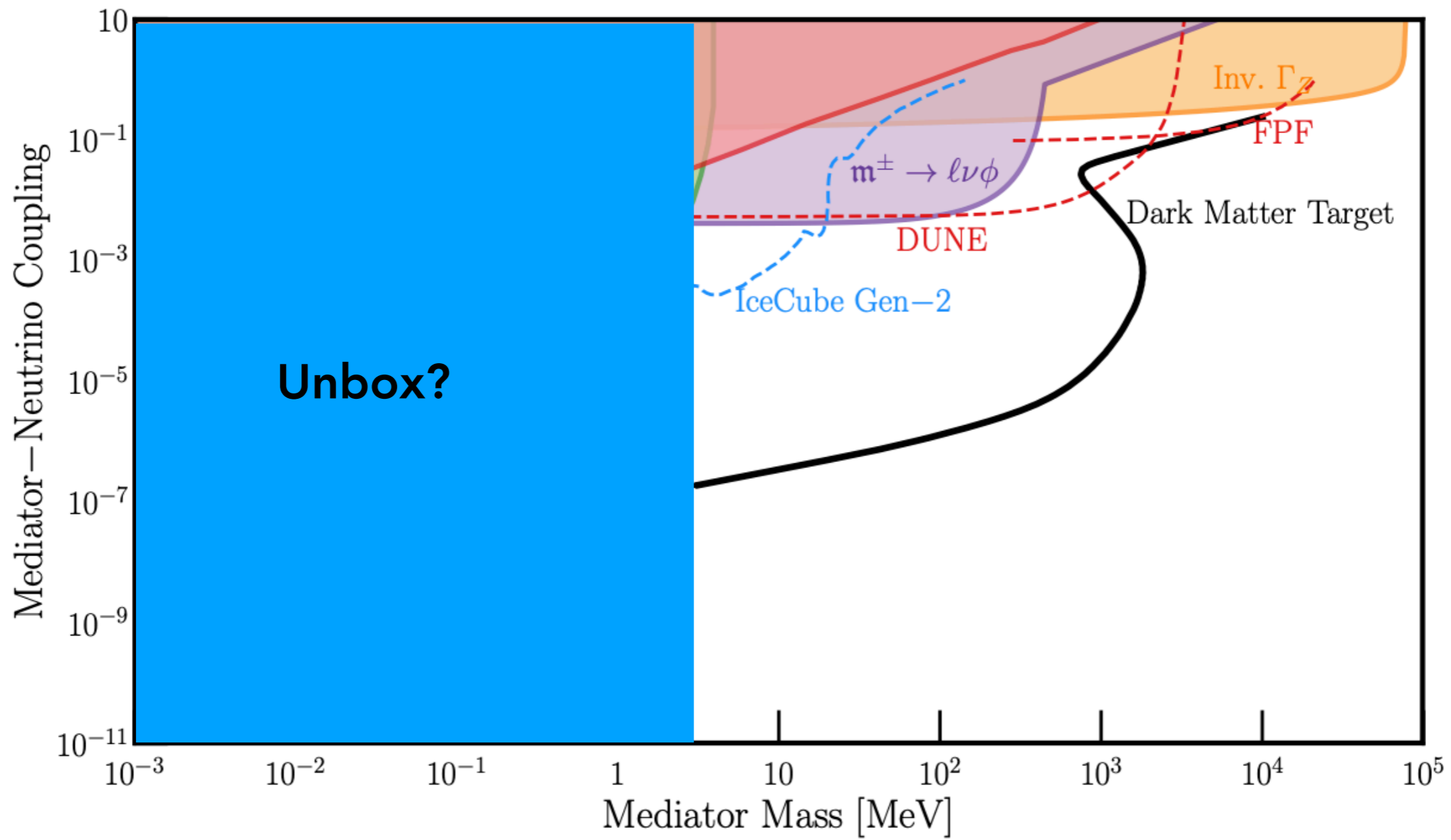
$$L_{\nu_s} > L_\nu = 10^{52} \text{ erg/s}$$

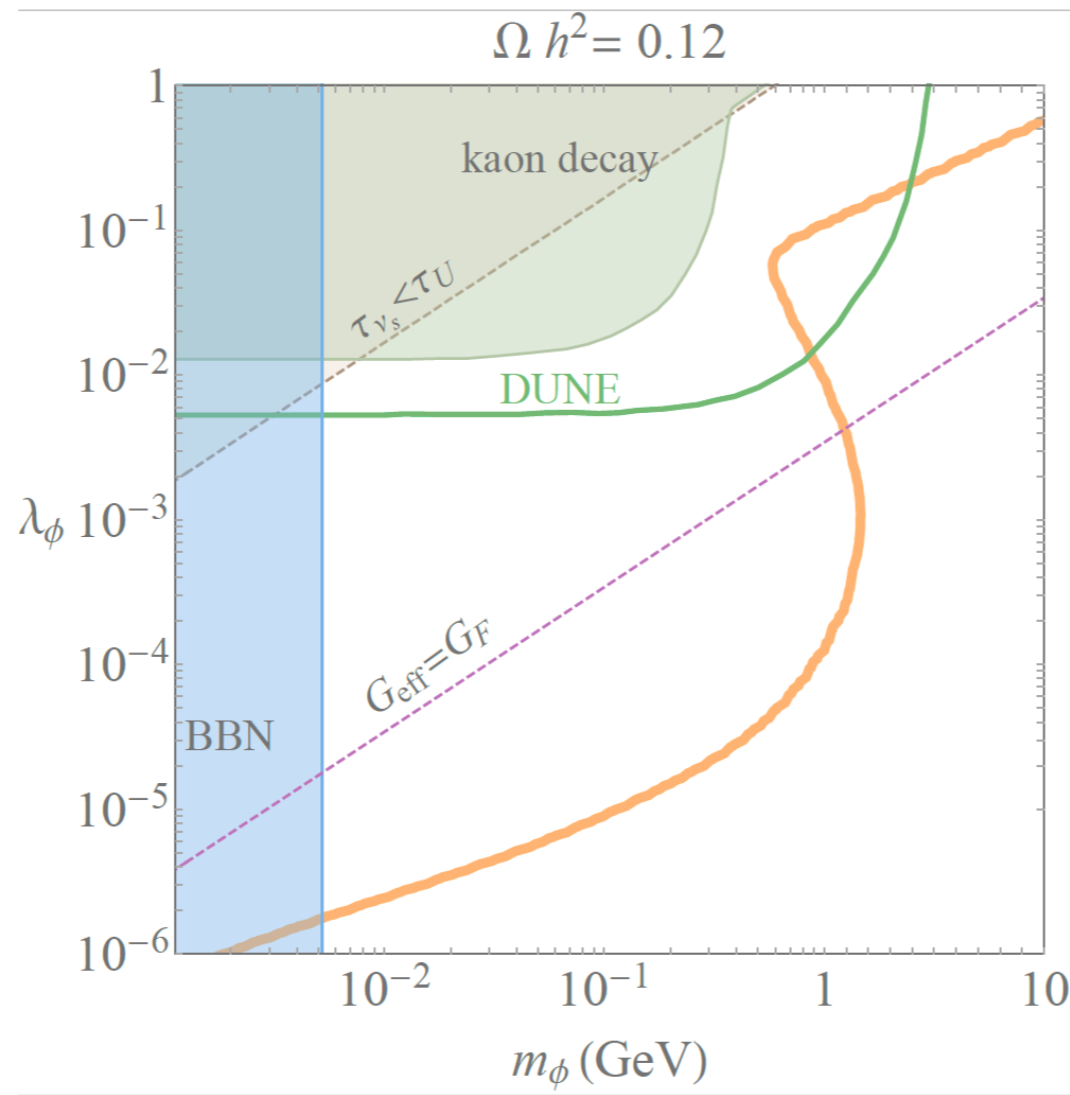
Supernova cooling bounds



Can probe the parameter space for judicious choice of sterile mass and mixing.

Big picture





$$m_\phi < \text{MeV}$$

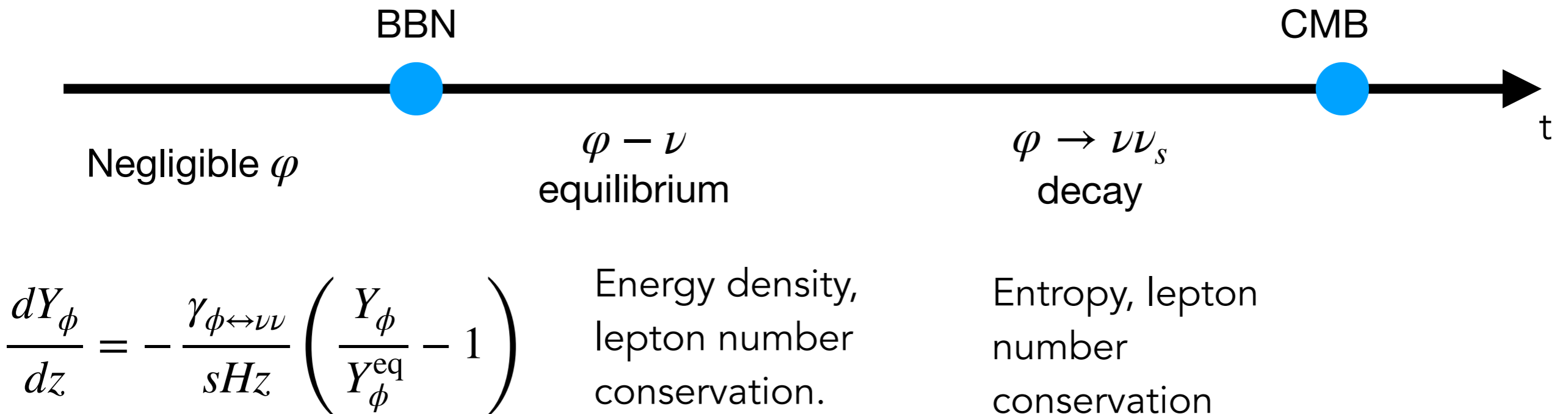
Cosmological Surveys

Low mass, low coupling limit

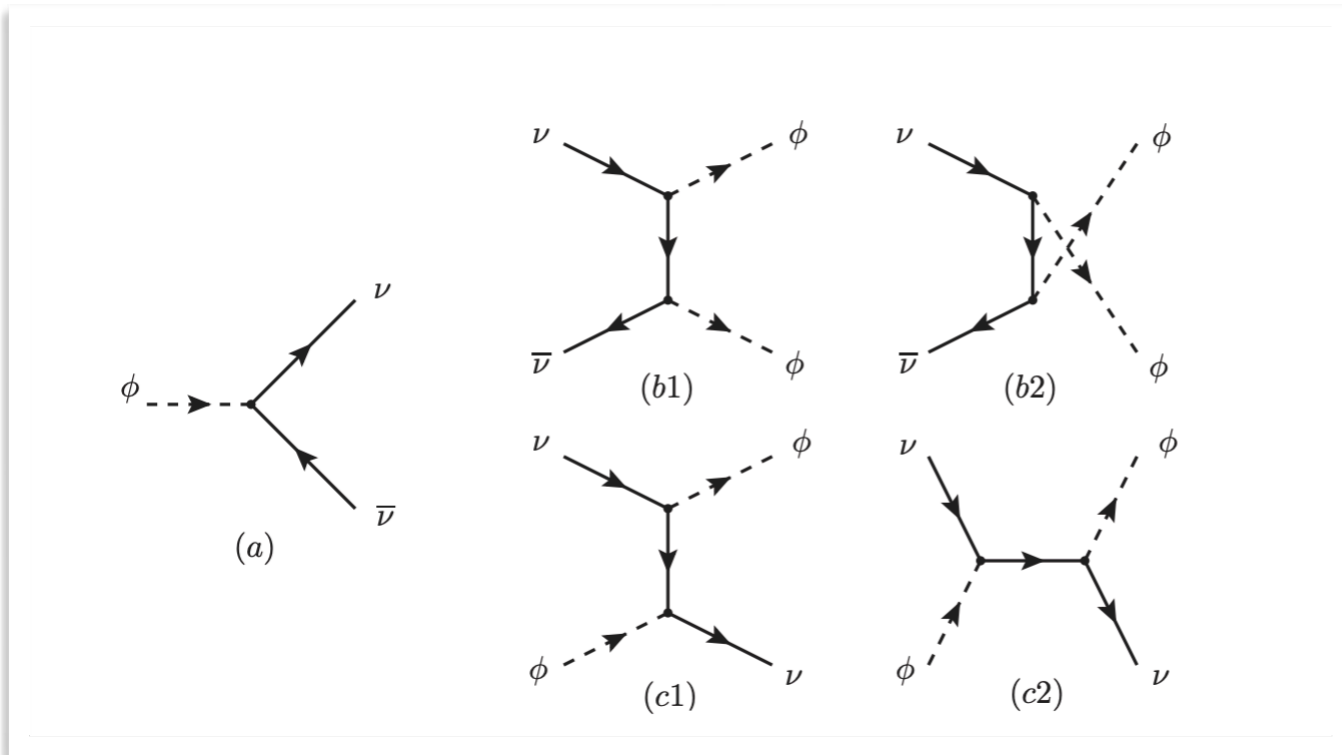
How do we evade BBN bounds? Relevant process $\phi \leftrightarrow \nu\nu$. Dominates over $2 \leftrightarrow 2$ processes.

Partial thermalization of ϕ before BBN, require feeble coupling to neutrinos.

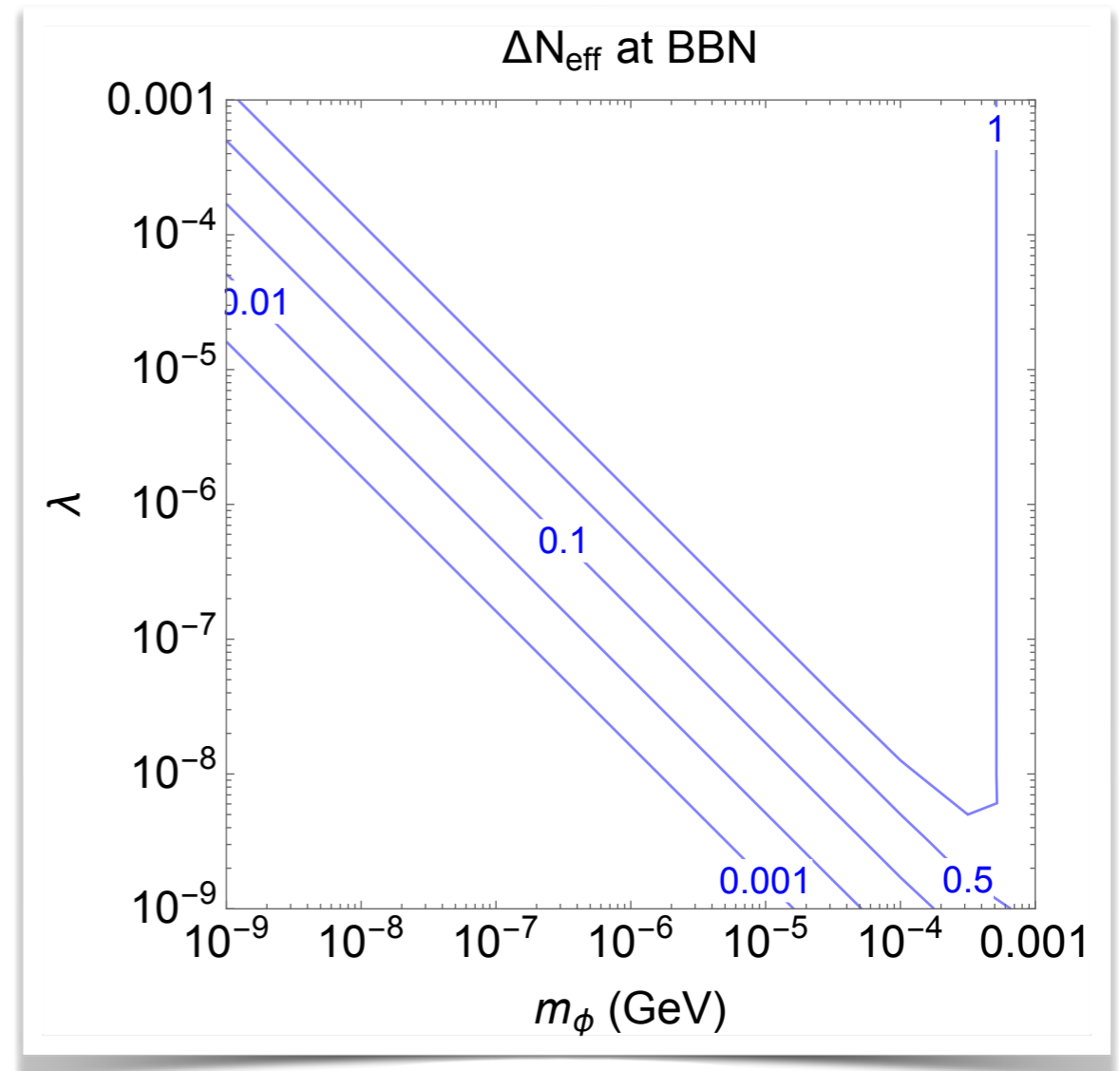
Decay of ϕ to keV ν_s before CMB



Contribution to extra radiation at BBN



Huang, Ohlsson, Zhou, PRD 2018

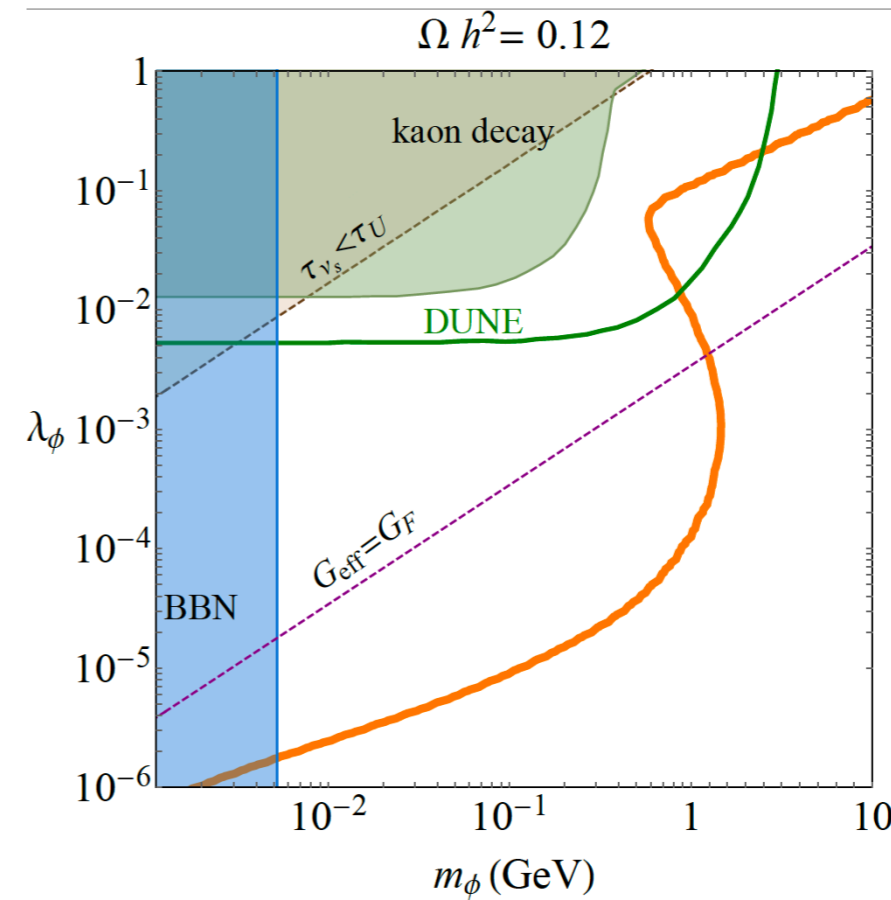
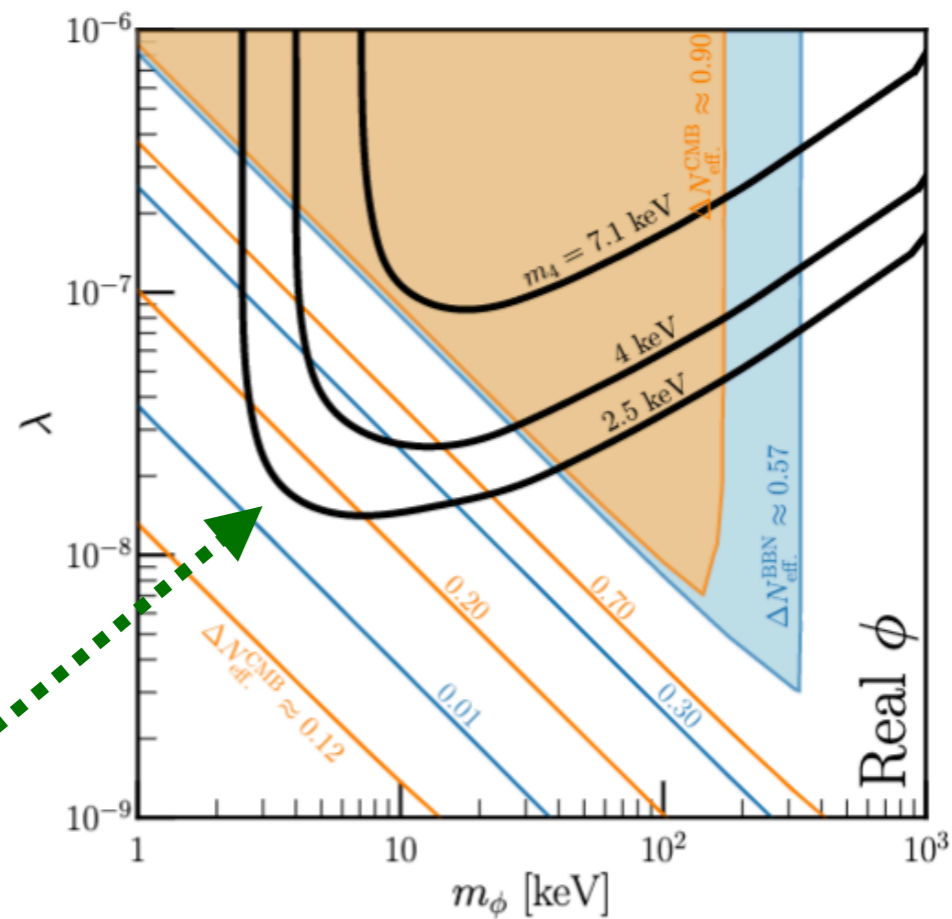


Kelly, MS and Zhang, PRL 2021

For low mass ϕ , processes like $\phi \leftrightarrow \nu\nu$ become relevant. This explains the wedge like feature.

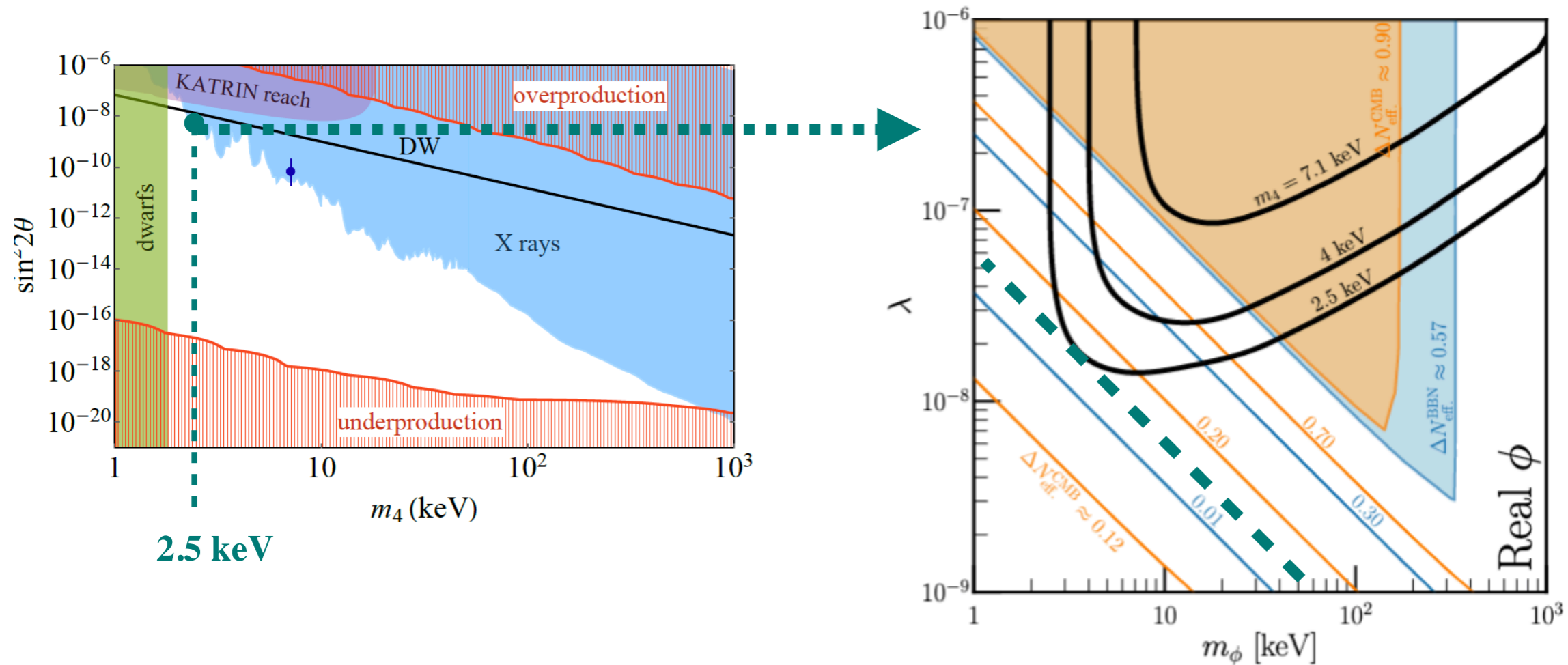
Correlation with extra radiation

- Partial thermalization of ϕ contributes to N_{eff} at BBN, and ϕ decay to N_{eff} at CMB.
- As $m_\phi \rightarrow m_4$, larger values of λ are required to compensate phase-space suppression of $\phi \rightarrow \nu\nu_s$
- Relic curves show a minima, can correlate DM relic with ΔN_{eff} .



Minima

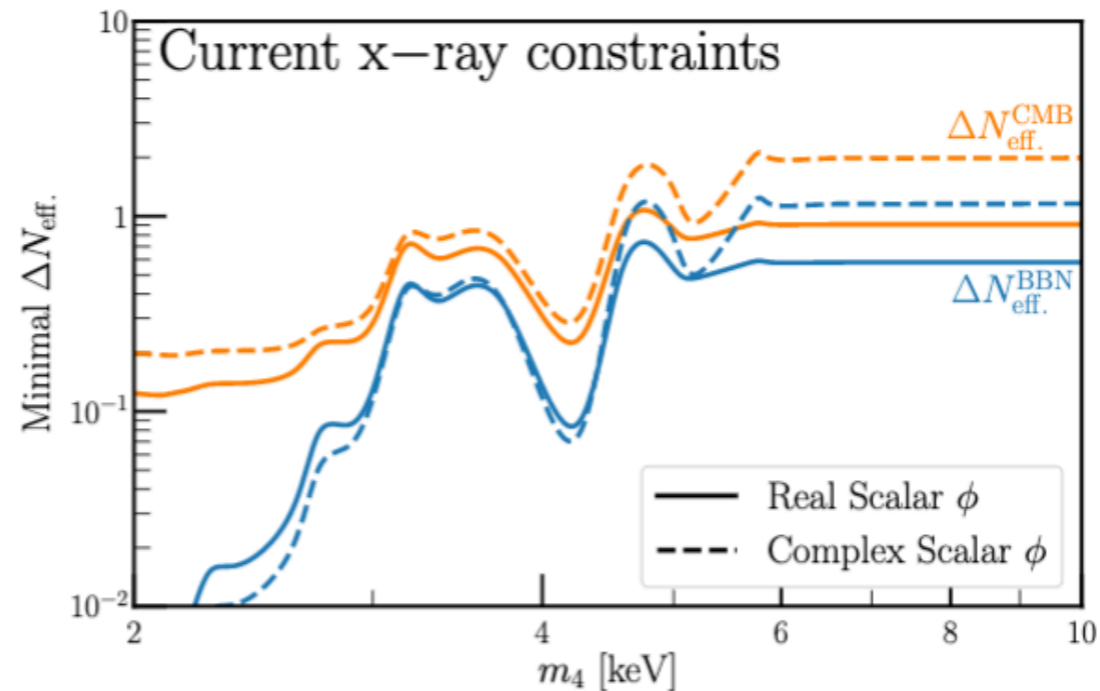
The algorithm for deriving constraints



- Consider the maximum allowed mixing angle for each sterile neutrino mass.
- For a given sterile neutrino mass, and the **maximum** allowed mixing angle, choose the curve corresponding to a **minimum** value of $\Delta N_{\text{eff}}^{\text{BBN}}$ and $\Delta N_{\text{eff}}^{\text{CMB}}$.
- This gives a target ΔN^{eff} to probe these models.

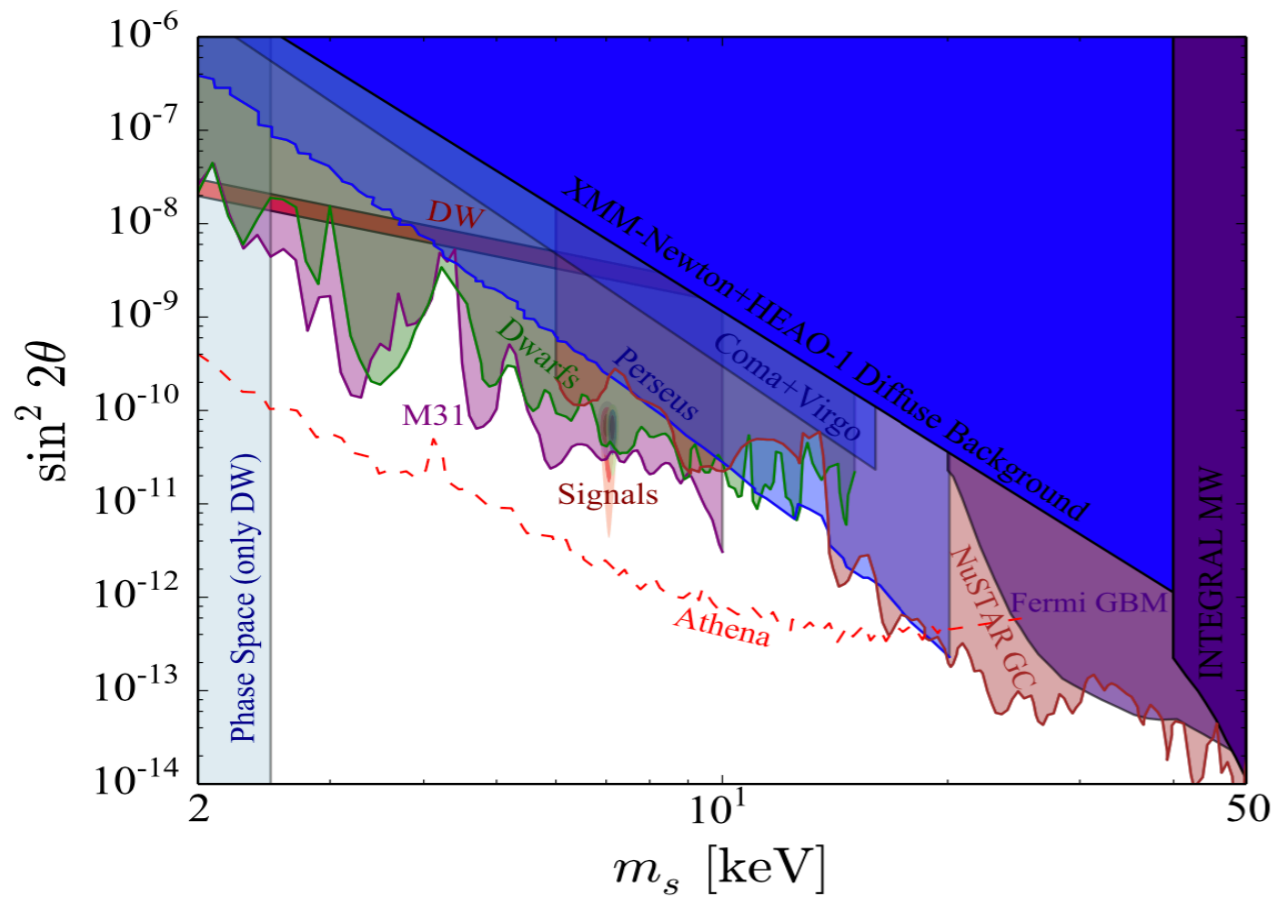
Constraints from N_{eff}

Minimal ΔN_{eff} probe

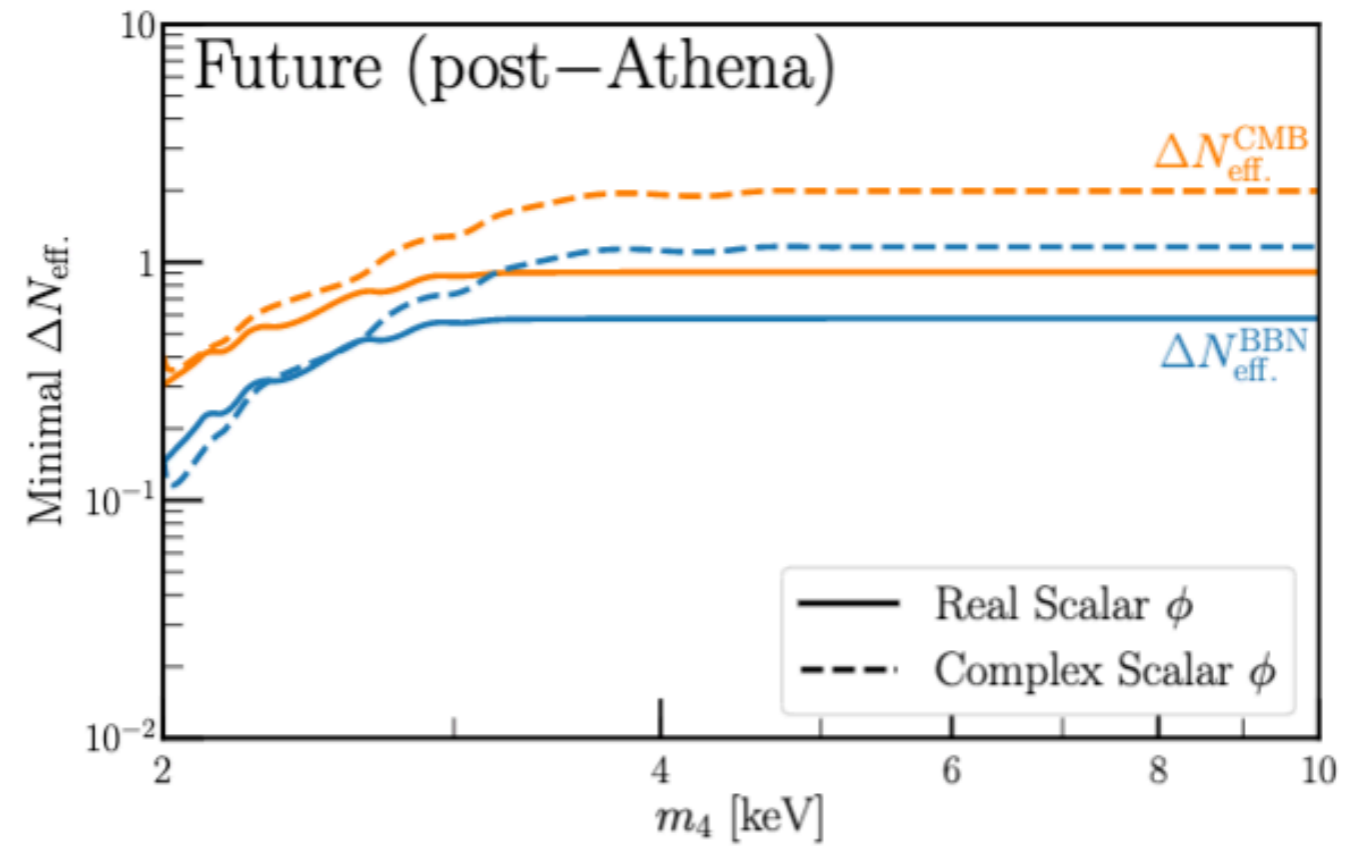


- Each point is for a **maximum** allowed mixing angle for a sterile neutrino mass.
- Corresponding minimum value of ΔN_{eff} during BBN and CMB. For real scalar,
 $0 < \Delta N_{\text{BBN}}^{\text{eff}} < 0.57$
 $0.12 < \Delta N_{\text{CMB}}^{\text{eff}} < 0.9$
- This can put additional constraints from future cosmology surveys, like CMB-S4.

Constraints from N_{eff}

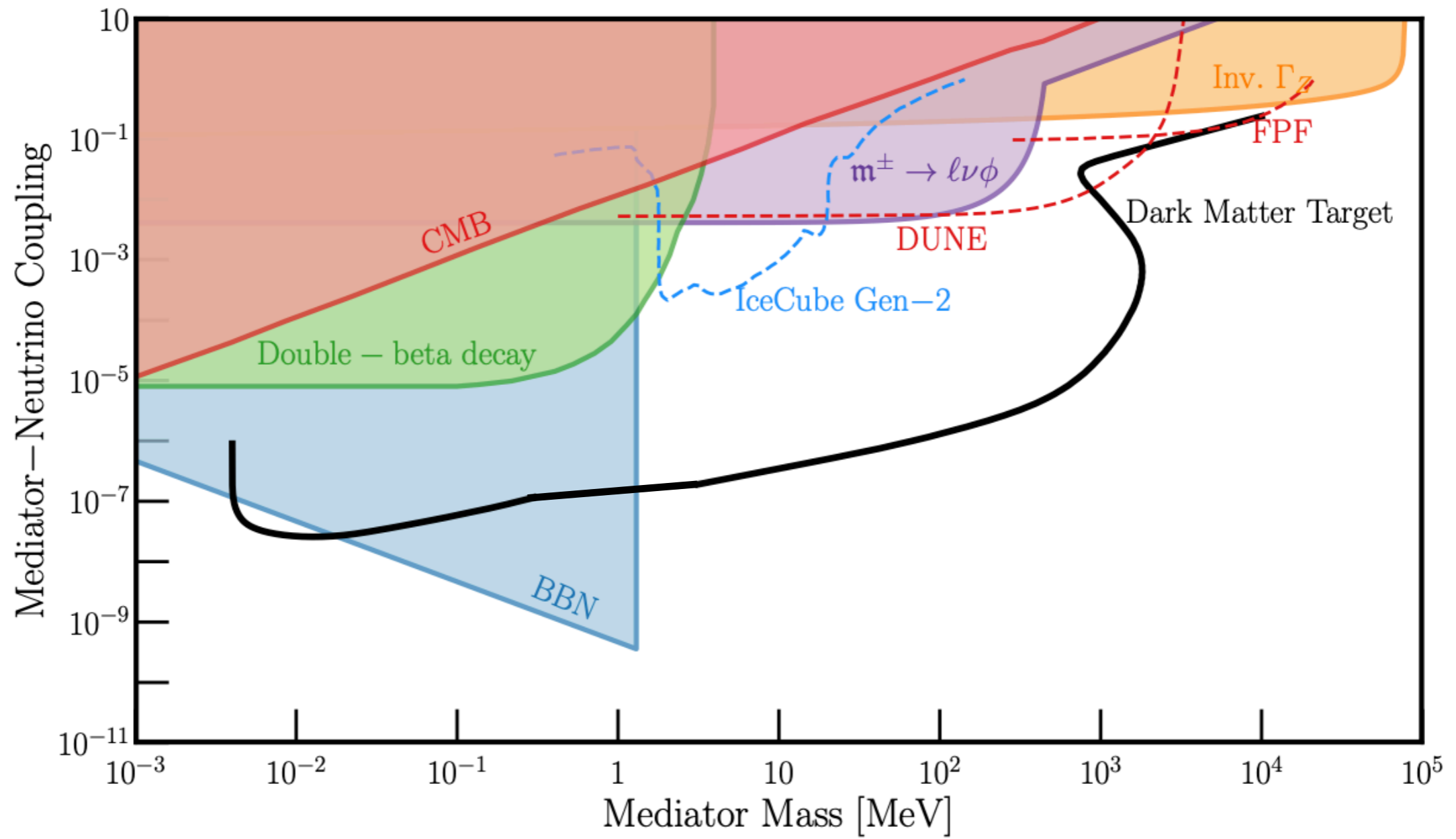


Abazajian (2017)



Stronger constraints from future surveys like Athena.

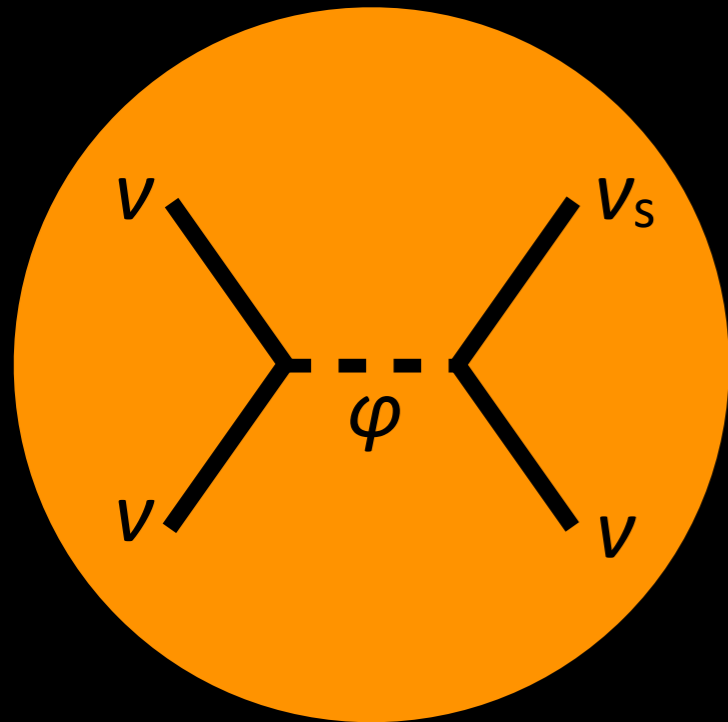
Big Picture - unboxed



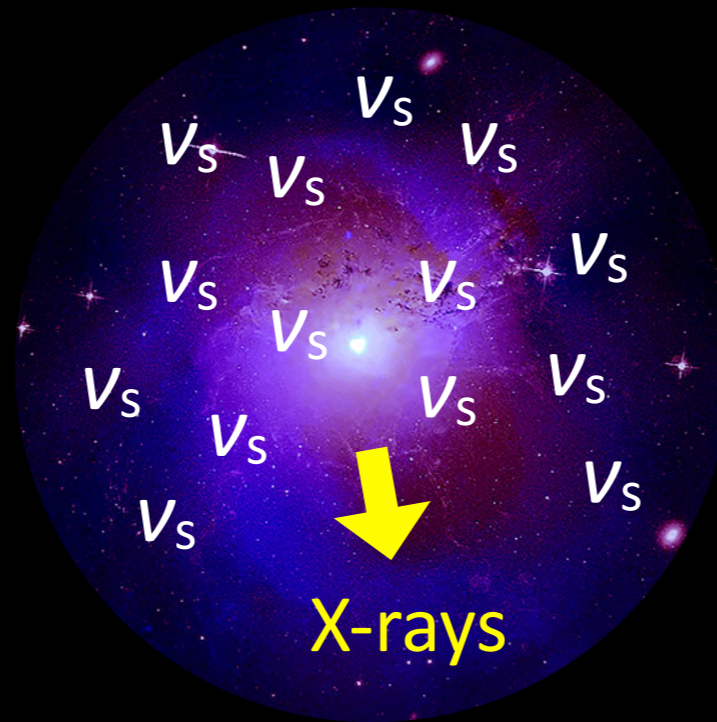
Summary

- keV sterile neutrinos are excellent warm dark matter candidates. Can be produced non-thermally through a mixture of oscillations and collisions.
- Vanilla scenario is in tension with X-ray bounds+ phase space bounds.
- Introduce secret interactions among active neutrinos. Can be used to efficiently produce sterile neutrino DM in the early Universe.
- Leaves imprints in the lab, in astrophysical objects as well as in the early Universe.
- Can be cornered from all possible directions with upcoming experiments.
- This will be an exciting decade for sterile neutrino dark matter theories.

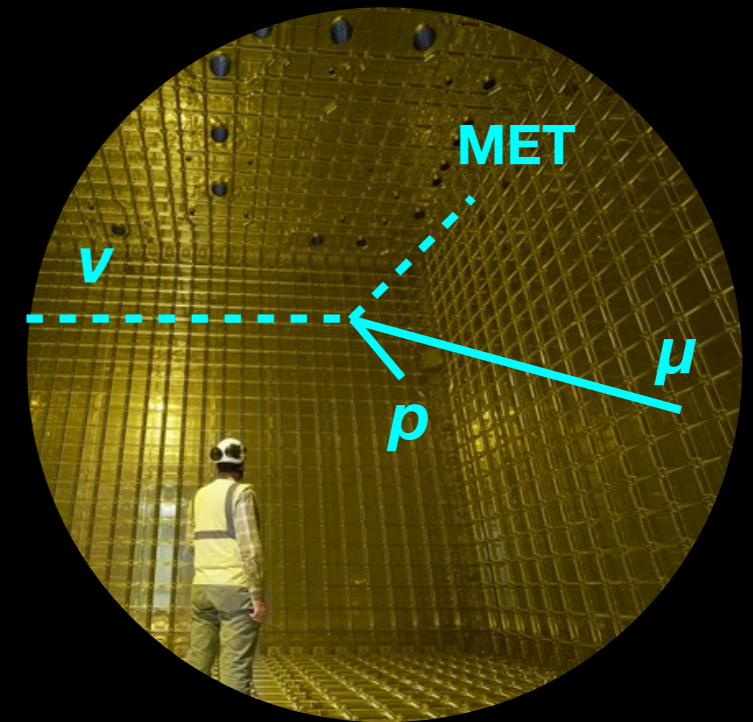
Summary



early universe



today



near future

Thank you!

BACKUP

Backup: UV Completion

Another option, which we call the type I model, is to introduce pairs of vector-like fermions N_i and N_i^c ($i = 1, 2, \dots, n$, the number of vector-like fermions) that are SM singlets carrying $B-L$ charges ∓ 1 , respectively. The most general renormalizable Lagrangian includes

$$\mathcal{L}_{\text{UV}} \supset \tilde{y}_{\alpha i} L_{\alpha i} H N_i^c + M_{N,i} N_i N_i^c + \lambda_{N,ij} \phi N_i N_j + \lambda_{N,ij}^c \phi^* N_i^c N_j^c + \tilde{\lambda}_{N\nu,ij}^c \phi^* N_i^c \nu_j^c + \text{h.c.} , \quad (4.3)$$

where \tilde{y} are the strengths of the new Yukawa interactions and λ_N characterizes the strength of the interaction between N^c and the $LeNCS$ field ϕ .⁵ The constraint that the right-handed neutrino couplings λ_c^{ij} to ϕ are very small – see Sec. III H – implies that $\lambda_{N,ij}^c$ and $\tilde{\lambda}_{N\nu,ij}^c$ are also small and henceforth neglected. When all heavy fermion fields are integrated out, we obtain the effective operator in Eq. (1.3), $(L_\alpha H)(L_\beta H)\phi/\Lambda_{\alpha\beta}^2$, with

$$\frac{1}{\Lambda_{\alpha\beta}^2} = \sum_{i,j} \tilde{y}_{\alpha i} \frac{1}{M_{N_i}} \lambda_{N,ij} \frac{1}{M_{N_j}} \tilde{y}_{\beta j} . \quad (4.4)$$

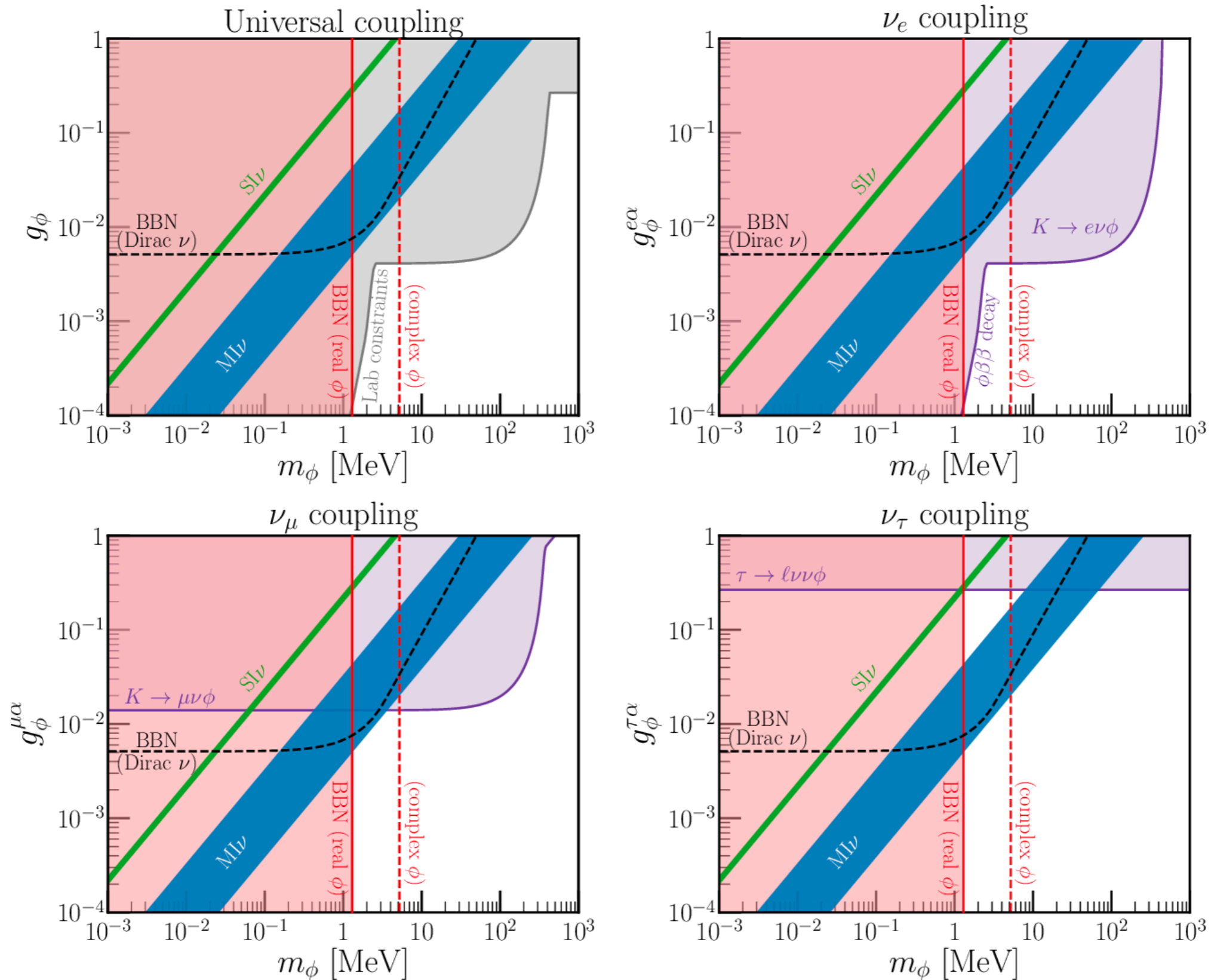
One option is to introduce a scalar T , a triplet under $SU(2)_L$ with hypercharge $+1$ and $B-L$ charge $+2$. We will call it the type II model, because it has a structure similar to the type-II seesaw. As already highlighted, however, unlike the seesaw mechanism, there are no $B-L$ -violating effects here. The most general renormalizable Lagrangian in this case contains

$$\mathcal{L}_{\text{UV}} \supset \tilde{y}_{\alpha\beta} L_\alpha T L_\beta + \lambda_T H T^\dagger H \phi - M_T^2 \text{Tr}(T^\dagger T) + \text{h.c.} , \quad (4.1)$$

where $\tilde{y}_{\alpha\beta}$ are Yukawa couplings between the triplet T and leptons of flavor α and β , λ_T are scalar couplings between the triplet, the Higgs field and the $LeNCS$ ϕ , and M_T is the triplet scalar mass. When the T field is integrated out, the low-energy effective theory matches that in Eq. (1.3) with

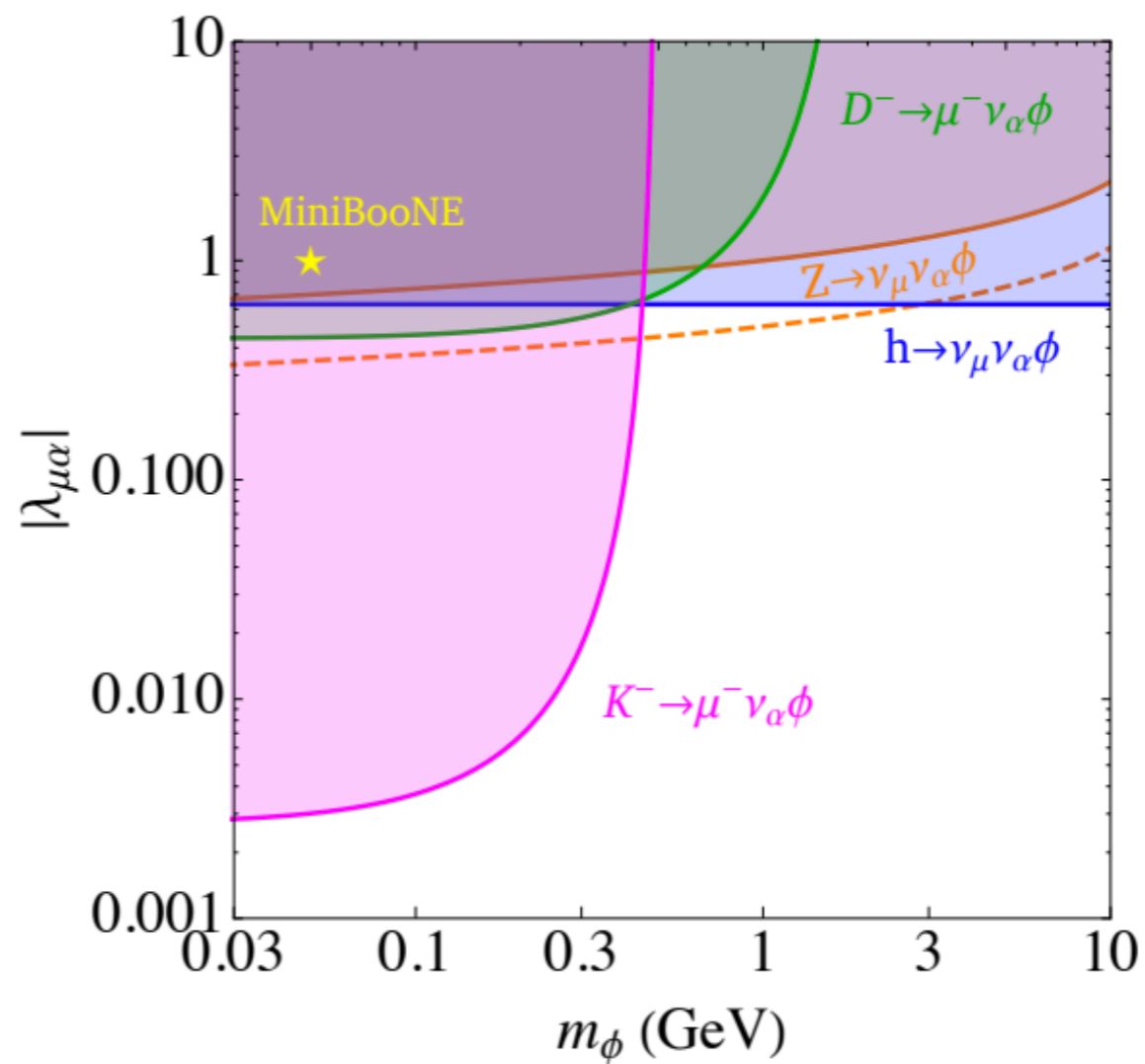
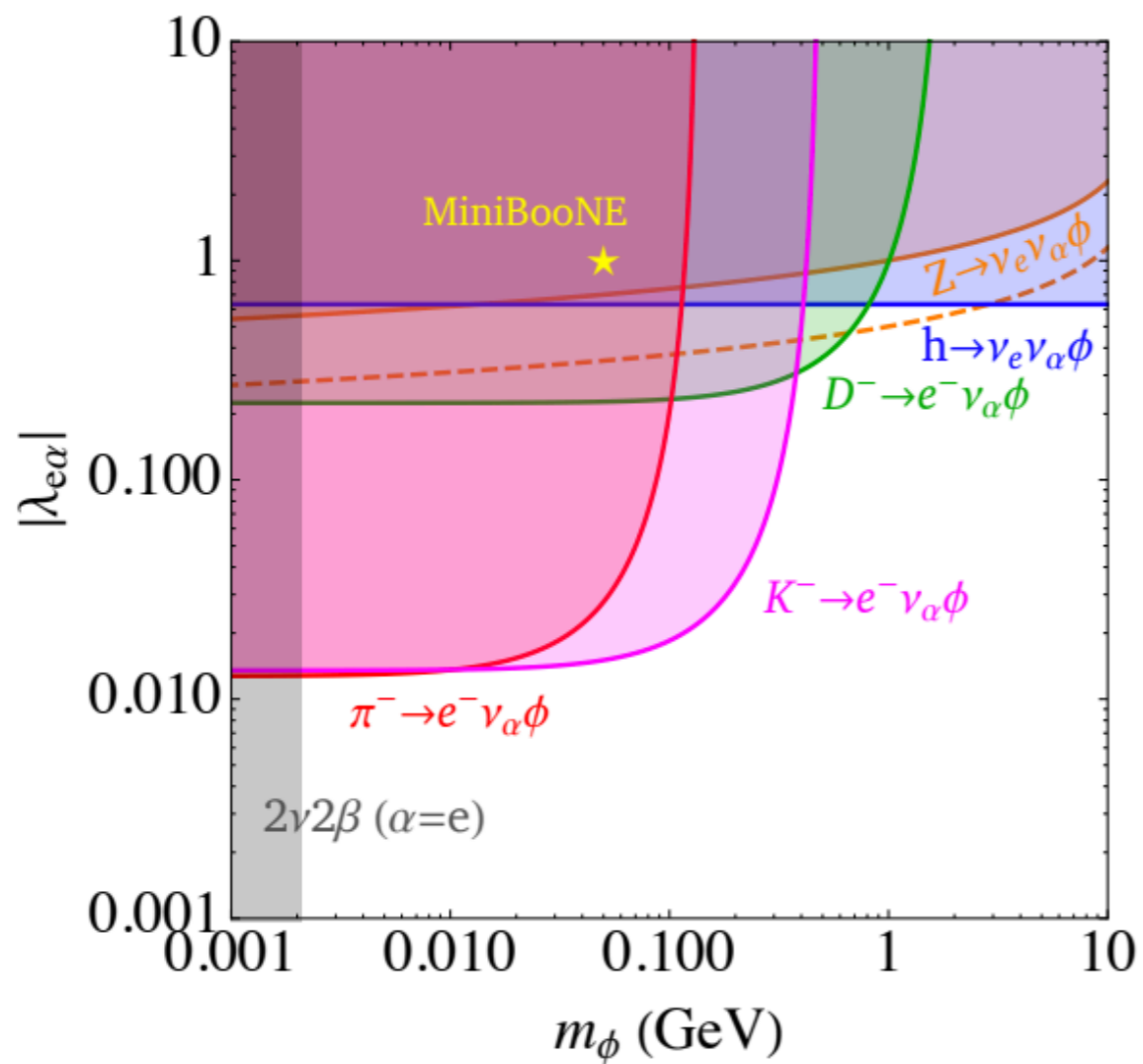
$$\frac{1}{\Lambda_{\alpha\beta}^2} = \frac{\tilde{y}_{\alpha\beta} \lambda_T}{M_T^2} . \quad (4.2)$$

Self-interaction bounds

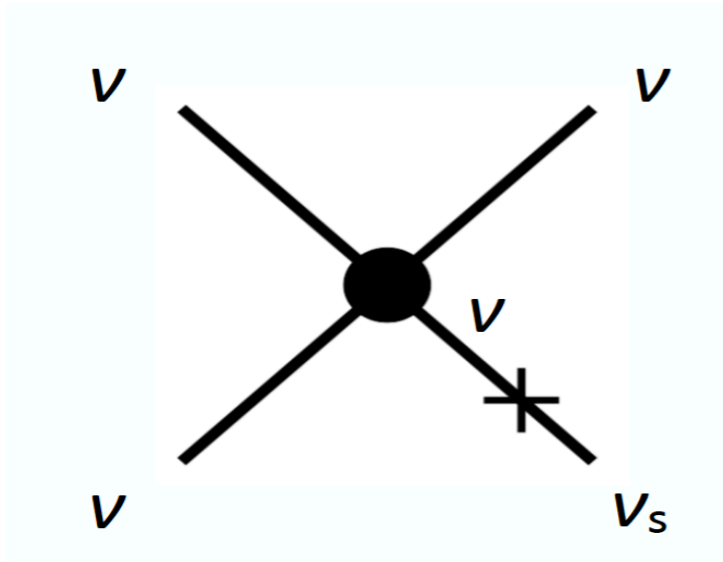


Berryman, de Gouvêa, Kelly and Zhang PRD2018
 Blinov, Kelly, Krnjaic and McDermott, PRL2018

Self-interaction bounds

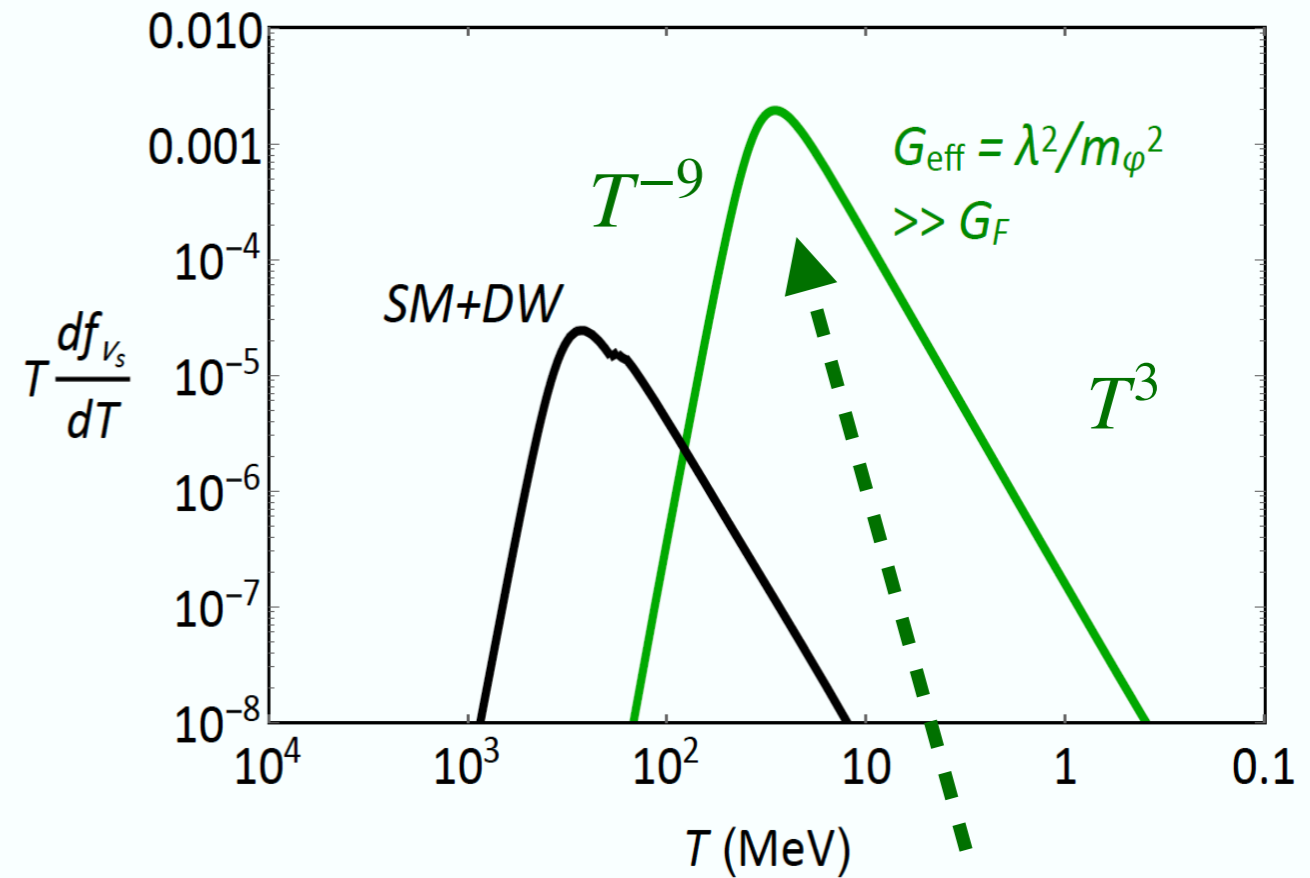


$$m_\phi \gg T$$



- Similar to DW, except with a stronger interaction.

$$\Gamma_a \sim \frac{\lambda_\phi^4}{m_\phi^4} ET^4, \quad V \sim -\frac{\lambda_\phi^2}{m_\phi^4} ET^4$$

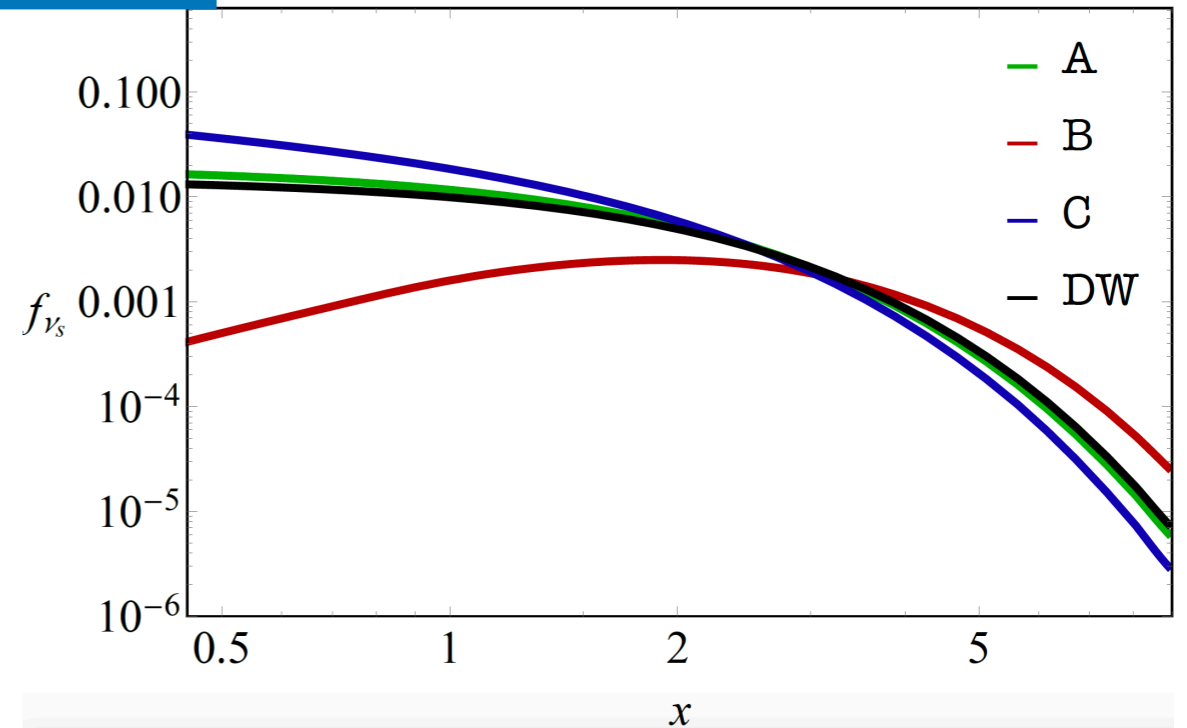
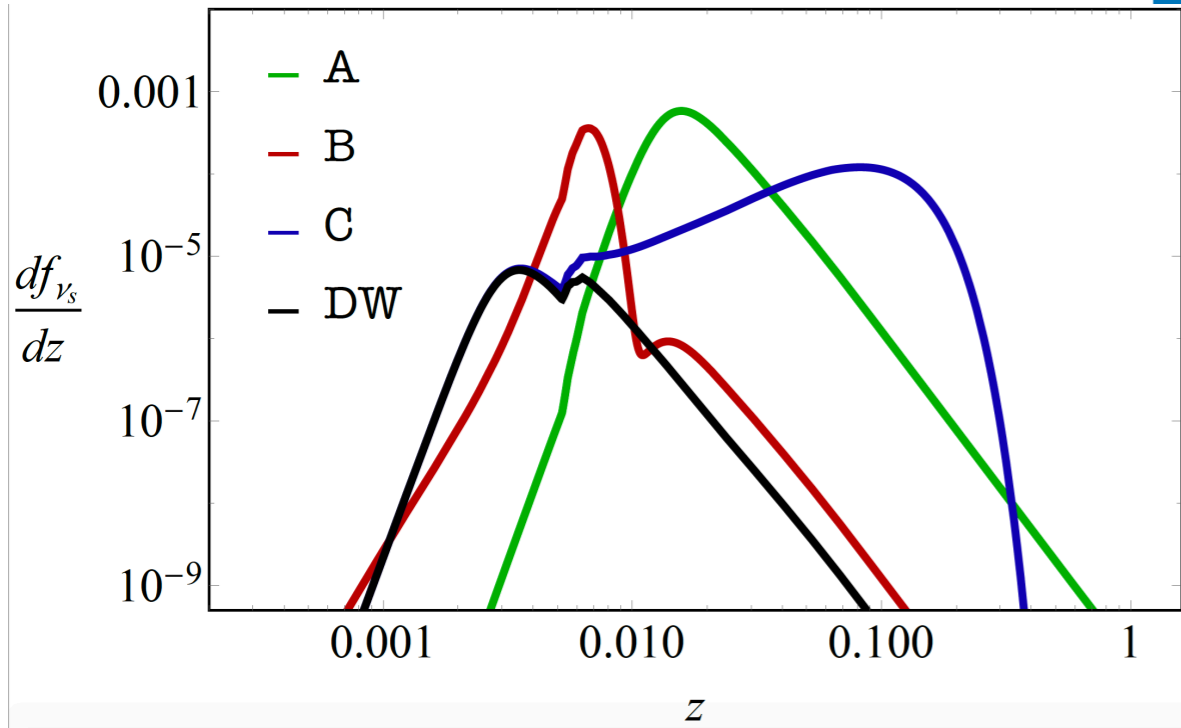


Production peaks at a lower temperature

Neutrino Spectra

$$z = \frac{1 \text{ MeV}}{T}$$

$$x = \frac{p}{T}$$



- Free streaming length: $\lambda_{\text{FS}} = \int_0^t dt \frac{v(t)}{a(t)} \simeq 1.2 \text{ Mpc} \left(\frac{1 \text{ keV}}{m_4} \right) \left(\frac{\langle x \rangle}{3.15} \right)$

Structure formation bounds evaded?

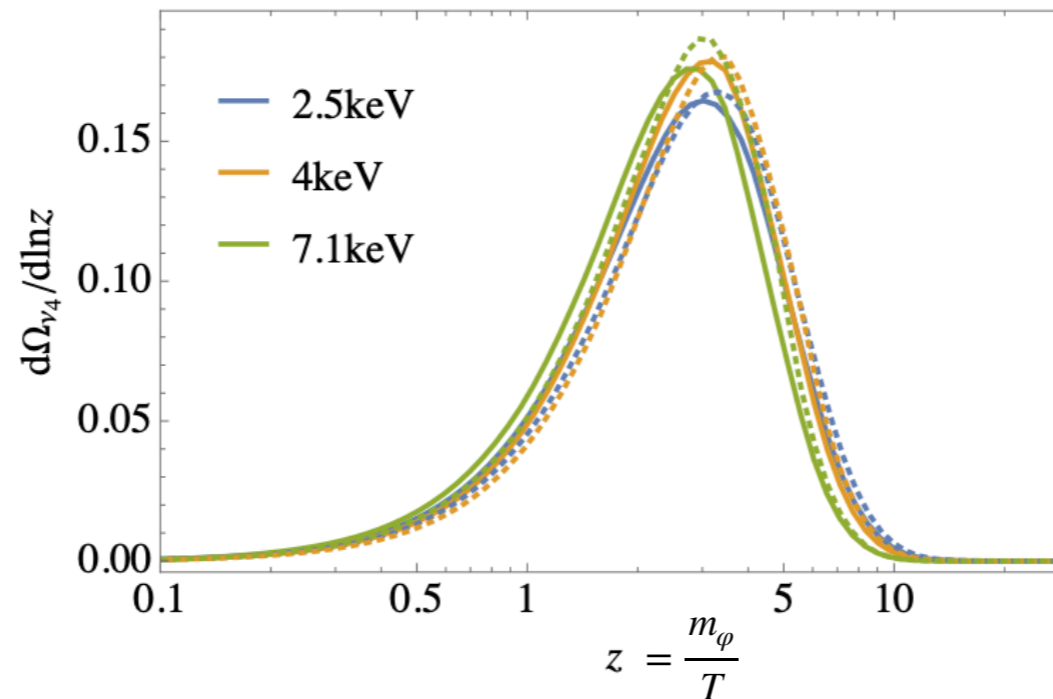


FIG. 5. Time dependence of $S\nu$ DM, for three values of m_4 as labelled. The other parameters are chosen for producing the observed DM relic density. The solid (dashed) curves correspond to real (complex) scalar ϕ case.

The DM is produced when ϕ is non-relativistic and of the same order as the DM mass. Hence this is “colder than warm” DM.

$$L_{\text{fs}} \propto L_{\text{fs}}^0 \times (v_{\text{prod}}/c)$$

More conclusive work needed!

Chemical potential

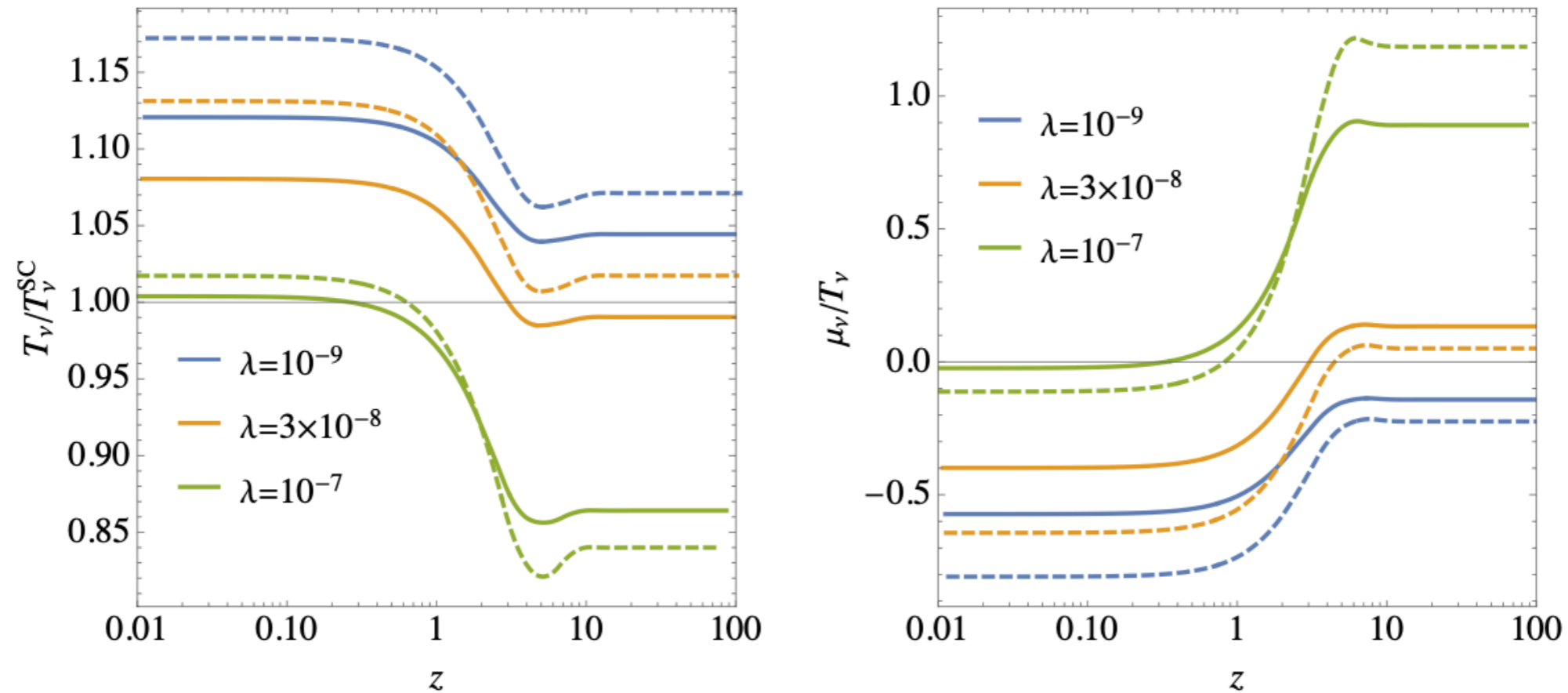


FIG. 4. Evolution of ratios $T_\nu(z)/T_\nu^{\text{SC}}(z)$ and $\mu_\nu(z)/T_\nu(z)$ as functions of z for three values of λ_ϕ and holding $m_\phi = 5$ keV fixed. Solid (dashed) curves correspond to real (complex) scalar ϕ case.

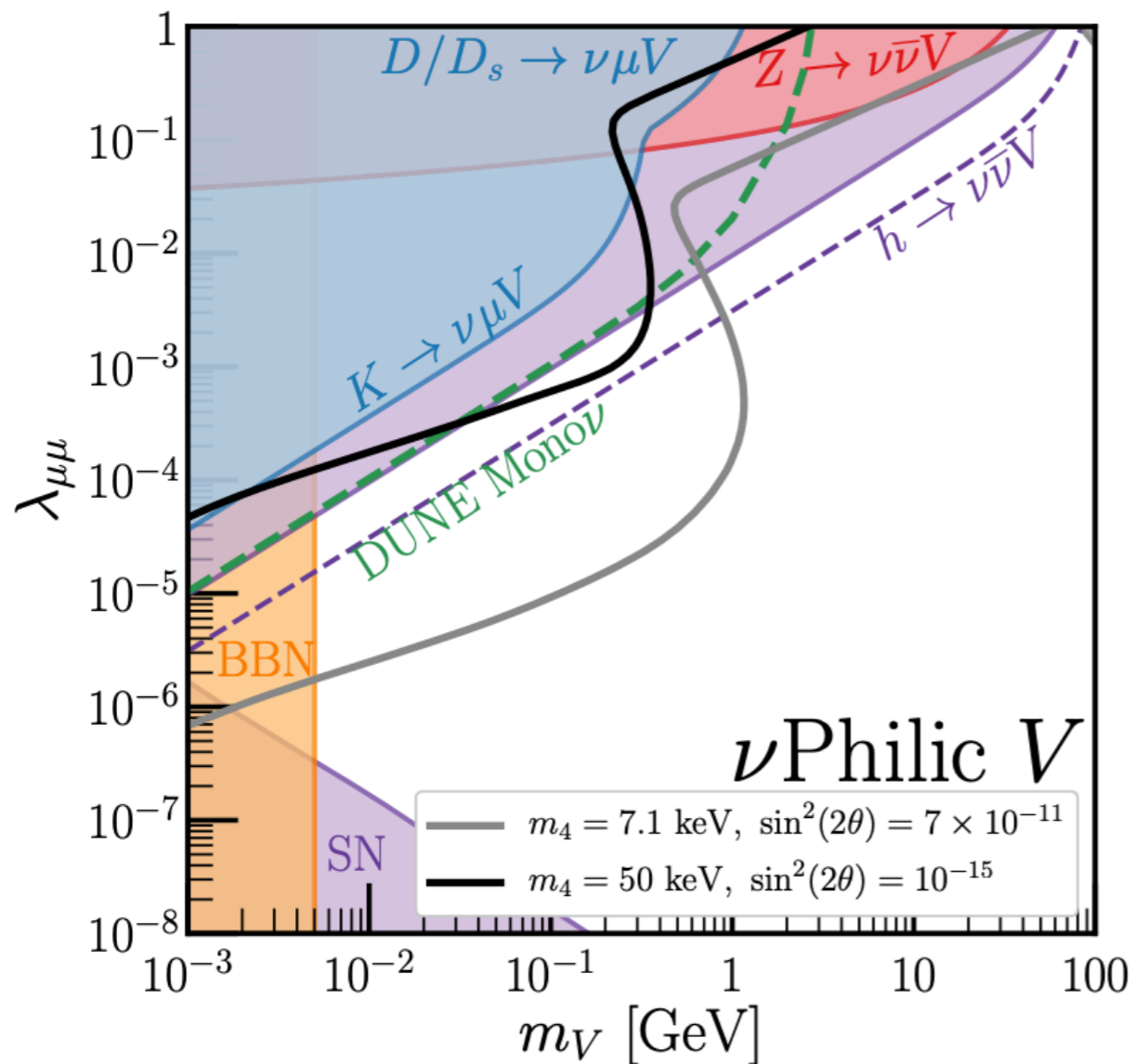
What about vector mediators?

- The same chain of arguments can be used for vector mediators as well.
- Bounds can be stronger, due to presence of longitudinal d.o.f of massive vector boson.
- Here we consider three of the most popular vector models:
 1. Neutrinophilic vector model.
 2. $U(1)_{L_\mu - L_\tau}$
 3. $U(1)_{B-L}$

Neutrinophilic vector

Consider the vector equivalent of the neutrinophilic interaction.

$$\mathcal{L} = \frac{1}{\Lambda^2} (\bar{L}_\alpha i\sigma_2 H^*) \gamma_\mu (H^T i\sigma_2 L_\beta) V^\mu \rightarrow \lambda_{\alpha\beta} \bar{\nu}_\alpha \gamma^\mu \nu_\beta V^\mu$$



Bounds :

1. Invisible Higgs decay.
2. Z boson decay width.
3. Exotic meson decays.
4. SN cooling bounds.
5. Accelerator neutrino bounds.
6. BBN bounds.